The Calculation of Computer Assisted Sun Shift Line Positioning

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Abstract—As the most important marine reserved system, astronomical positioning has incomparable advantages. In this paper, according to the basic principle of the sun shift line positioning, using the spherical triangle derives the mathematical model of the sun shift line positioning by observing the sun on the ship and then using the VB language works out the program of the sun shift line positioning. At last, the computer technique is applied to celestial navigation and is able to calculate the complex equations quickly. Through the practice, computer aided positioning not only meet the need of the navigation requirement, but also shorten the calculation time.

Keywords—celestial navigation, the sun shift line positioning, computer aided positioning

I. INTRODUCTION

The daytime is usually only observing the sun, so the sun shift line positioning is the main method of marine astronomical positioning. However, at present the sun shift line positioning is always used the altitude difference method proposed by French navigator St.Hilair in 1875 and this method needs to look up sailing calendar table and use calculator. Because the altitude difference method itself exists some error, such as mapping trivial, calculation of complex, no timeliness. Traditional astronomical positioning limits the further development of the celestial navigation. In order to overcome these shortcomings, based on theory of astronomical positioning circle and according to the spherical triangle, we could establish mathematical models and works out the computer program. At last when we input observation datas, we can directly look up the ships positioning, latitude \( \phi \) and longitude \( \lambda \) on the computer. With the application of computer technology, the traditional astronomical navigation to get rid of the shackles of height difference method become possible and then realize the automation of navigation.

II. THE THEORY OF THE SUN SHIFT LINE POSITION AND MATHEMATICAL MODEL

A. The basic positioning theory

The sun shift line positioning also is called “the different observation localization of the sun”. In different time, the fore-and-aft observation of the sun positioning line is calculated and then with the shift line principle, we could get the method and process of the ship positioning. In the first observing the sun’s altitude we can map one ship line of the sun and after a period of time, we can get the another shipline of the sun by observing the second altitude of the sun. We should parallelly move the first line of positioning along the ship's path to the second line of positioning in the observating transferring sun position line, and then the second ship line and the first tranfering ship line will make a point of intersection and this point of intersection is the second observation time of astronomical position.

B. Establish mathematical model

Because the ship is sailing on the sea, and each observation has certain time interval, it is necessary to make the ship line correct to the same time. When we are making some correction to celestial body’s position, we can get revised celestial accurate position. At last, the correct mathematical model is established. More importantly, we need a large number of theoretical basis to verify that the mathematical model is accurate or not, so as to realize the sun shift line positioning accuracy. No revised mathematical model is shown in figure 1. Revised mathematical model is shown in figure 2. The target of revised mathematical model is unification of the observation times.
Using the edge cosine formula in the spherical triangle $P_NB_1B_2$:

$$\varphi = \arcsin[\sinh2\sin Dec2 + \cosh2\cos Dec2\cos(C-B)]$$  

$$t = \arccos \frac{\sinh2\sin\varphi\sin Dec2}{\cos\varphi\cos Dec2}$$  

$$t = t_o \pm \lambda$$  

*: East $\lambda$ is “+”, West $\lambda$ is “−”.

C. The realization of the program

How to solve the model $(B_1B_2,B,C)$ is the key. In the spherical triangle $P_NB_1B_2$, $Z_2B_1B_2$:

$$B_1B_2 = \arccos[\sin Dec1\sin Dec2 + \cos Dec1\cos(Dec2)\cos(GHA2-GHA1)]$$

$$B = \arccos \frac{\sin Dec1 - \sin Dec2\sin B_1B_2}{\cos Dec2\sin B_1B_2}$$  

$$C = \arccos \frac{\sin Dec1 - \sin Dec2\sin B_1B_2}{\cos Dec2\sin B_1B_2}$$

Matters should be paid attention:

1) $h_1' = h_1 + \frac{V(zt_1zt_2)\cos(A_1CA)}{60}$

$h_1'$ is the sun position of $B_1$ that is correct to zenith $Z_2$. $A_1$ is the first sun’s measured direction. $ZT_1, ZT_2$ is the observed time. $CA$ is the ship’s course. $V$ is the speed of a ship.

2) The synonym of Dec and latitude $\varphi$, “+”; the different name of Dec and latitude $\varphi$, “−”;

3) Before the upper meridian passage, $t<0$; after the upper meridian passage, $t>0$.

VB is a section of high visual programming language. We can use some simple control to realize the program editor, So we will reduce the calculation of the algorithm. Programming should be paid attention to: In VB there is only general trigonometric function and no inverse trigonometric function, we need to realize conversion through the trigonometric function transformation.

Program instructions in figure 3.
VB basic program interface is shown in figure 4.

III. THE EXAMPLE OF THE SUN SHIFT LINE POSITIONING

Verification: On 2009.02.15, Tianren ship set off from the Tianjin Xingang Port to Inchon Port on the ZT1 12°30’. The course CA99°, the speed V18kn, GMT1 04°30’26’, the first sun altitude hs1 38°17’.0, the solar azimuth A1183°, the height of eye e18m. On ZT14 h 18m, GMT2 06°17’40”, the second sun altitude 31°29’.5. Index error and device difference (i+s)=0’.0. Solving the sun shift line position on ZT14 h 18m?

Use mapping method:

\[
\begin{align*}
GHA_1 &= 244°04’6 \\
\lambda_c_1 &= 118°06’0E \\
LHA_1 &= 362°10’6 \\
002°10’6 &= 029°35’2
\end{align*}
\]

Use the following formula:

\[
\begin{align*}
h &= \sin^{-1}\left(\sin\phi \cos\delta + \cos\phi \cos\delta \cos\phi\right) \\
A &= \cos^{-1}\left(\tan\delta \cos\phi \cot\phi - \sin\phi \cot\phi\right)
\end{align*}
\]

Solution is obtained:

\[
\begin{align*}
h_1 &= 38°24’.6 \\
h_2 &= 31°35’.5 \\
h_{c1} &= 38°28’.2 \\
h_{c2} &= 31°31’.9 \\
\Delta h_1 &= 3’.4 \\
\Delta h_2 &= 3’.6
\end{align*}
\]

In the chart mapping the sun shift line position in figure 5.

From the above figure:

\[
\phi = 38°49’.2N, \quad \lambda = 118°47’.2E
\]

Use computer aided positioning:

Input data: After correction, observation height h, draw true height h. According to the Greenwich mean time, we could check the nautical almanac to get the sun coordinates, Declination(Dec) and Greenwich hour angle(GHA):

\[
\begin{align*}
hs_1 &= 38°24’.6 \quad Dec_1 = 12°38’.4S \quad GHA_1 = 244°04’.6 \\
hs_2 &= 31°36’.8 \quad Dec_2 = 12°36’.9S \quad GHA_2 = 270°53’.1
\end{align*}
\]

The above 11 data( ZT1, ZT2, V, CA, hs1, hs2, Dec1, Dec2, GHA1, GHA2, A1 ) input program interface, and we should click the calculate button, some calculation results will be shown in figure 6.

On ZT14 h 18m the sun shift line position:

\[
\phi = 38.478007723 \approx 38°28’.68N \\
\lambda = 119.34358195\approx 119°20’.61E
\]
GPS showing the ship position:

\[ \varphi = 38^\circ 24' .7N, \lambda = 119^\circ 15' .9E. \]

Data comparison in table 1:

<table>
<thead>
<tr>
<th></th>
<th>mapping</th>
<th>computer</th>
<th>GPS</th>
</tr>
</thead>
<tbody>
<tr>
<td>data</td>
<td>( \varphi = 38^\circ 49' .2N )</td>
<td>( \varphi = 38^\circ 28' .68N )</td>
<td>( \varphi = 38^\circ 23' .7N )</td>
</tr>
<tr>
<td></td>
<td>( \lambda = 118^\circ 47' .2E )</td>
<td>( \lambda = 119^\circ 20' .61E )</td>
<td>( \lambda = 119^\circ 15' .9E )</td>
</tr>
<tr>
<td>error</td>
<td>26'</td>
<td>4'</td>
<td>0</td>
</tr>
</tbody>
</table>

Through the comparison among three datas, accuracy of GPS position is the highest, that is used as the benchmark. Accuracy of the mapping method is the Iwoest, its error area is about 26', that is about 26 kn. Chart of the location area is within a position circle of the radius of 26 kn. Accuracy of the computer aided positioning method is smaller than mapping method, its error area is only 4’, that is about 4 kn. Computer aided positioning of the location area is within a position circle of the radius of 4 kn positioning and precision meet the requirements. Computer aided astronomical positioning can get close to actual position more accurately, error can be controlled in the acceptable range and positioning accuracy has been greatly improved. It will take about 15minute to finish position by mapping position method and few second to finish position by computer aided positioning method. We can realize rapid positioning.

IV. CONCLUSION

The importance of computer technology to astronomical navigation development:

1) Greatly improve the efficiency and accuracy of calculation: Inputting data only 1 minute can complete the sun shift line positioning, calculation and mapping error does not need to consider and the computer calculation accuracy completely satisfy the navigation requirements.

2) The complicated astronomical calculation is completed by the computer, so traditional astronomical positioning won’t make crew flinch and easily increase the crew interest. Since using computer calculation, the sun shift line positioning accuracy depends on the observation error of the solar altitude. As long as we practice more, the crew’s personal capacity will gradually improve.

3) Through the comparison with GPS, the sun shift line positioning system error can gradually be mastered and finally eliminated. Within the stable scope of the permission of astronomical position error (smaller random error ), we even can use astronomical position to insteal of GPS when GPS does not work well. Maybe this is why astronomical navigation still be widely used today even modern ship equipment GPS.

The huge advantage of astronomical positioning has gotten the attention. However, computer hardware and software are ever improving and the requirements for positioning accuracy becomes more and more strict. In order to make the ship safety, marine technology must make use of the benefits of computer revolution, and realize constant localization and truly realize marine automation.

REFERENCES