

Modeling of Isotherm Phosphate Adsorption in Laundry Wastewater Using Anion Resin

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Abstract—The excess content of phosphate in laundry wastewater can cause eutrophication. Ion exchange is a method that has been widely used to remove pollutants in wastewater. The study of ion exchange equilibrium is generally carried out by means of adsorption isotherms modelling. The use of adsorption isotherms to model ion exchange systems involves that it is interpreted as a sorption process. The performance of an adsorbent can be studied by adsorption isotherm data which can be obtained by the experimental test in the laboratory. Modeling of adsorption isotherm data is a fundamental way to predict and compare adsorption performance, which is needed for the optimization of the adsorption mechanism pathways, the expression of the adsorbent capacity, and effective design of the adsorption system. This research applied three isotherm models namely Langmuir, Freundlich, and Dubinin-Radushkevich to determine and compare the isotherm models that suits best to remove phosphate on laundry waste using Lewatit MonoPlus MP 500 OH anion resin. The best fitted for phosphate removal using Lewatit MonoPlus MP 500 OH was using the Freundlich isotherm model with 5 ml/minute for the best flow rate and 166 cm³ anion resin volume.

Keywords—Phosphate; adsorption; ion exchange; anion resin; adsorption isotherm data

I. INTRODUCTION

Laundry wastewater that contain of phosphate causes environmental problem, one of the problems is eutrophication [1]. Ion exchange is a method that has been widely used to remove pollutants in wastewater. Removal phosphate can be achieved effectively using ion exchange resins. It can be able to improve pH in the solution and the ion exchange resins can be regenerated thus has a long-term use period [2]. Anion exchange resins effectively reduce anions pollutant in water using ion exchange adsorption methods [3].

Modeling adsorption isotherm is generally implemented for ion exchange equilibrium studies. Sorption reaction is theories in chemistry-physic that can be used to model ion exchange systems [2]. Basically, modeling adsorption isotherms can compare and predict the adsorption reactions that occur. The result from modeling adsorption isotherms can be used for optimization of adsorption reactions, calculating adsorption capacity and effective design of adsorption systems [4].

According to the research conducted by Foo [5], it can be concluded that the commonly used in the modeling of adsorption isotherm systems are Freundlich, Langmuir, Redlich-Peterson, Dubinin-Radushkevich, and Temkin. Chen [6] reported that the Langmuir model has a relatively high correlation coefficient (r^2) of 0.999 in the phosphate removal in wastewater by using Fe(III)-coordinated amino-functionalized mesoporous silica materials as adsorbent. Furthermore, the Freundlich model had better adsorption coefficient than Langmuir model in Rhodamine B adsorption on activated wood of Linggua wood with $r^2 = 0.798$ [7]. The Dubinin-Radushkevich model was applied by Moawed [8] to remove aniline blue and crystal violet from laundry wastewater using iodo polyurethane, the result showed that the crystal violet had $r^2 = 0.9918$ and $r^2 = 0.947$ for aniline blue.

This research was conducted to apply the isotherm models i.e. Langmuir, Freundlich, and Dubinin-Radushkevich to determine and compare the isotherm models that are most suitable for phosphate adsorption on laundry waste using anion resin. Moreover, r^2 and standard error (S.E.) for each parameter were used to evaluate the data. Data retrieval was accomplished by performing tests using a simple adsorption column.

II. RESEARCH METHODS

A. Research Material and Tools

The research was conducted using adsorption column. The adsorption column was a glass cylindrical column which generally had a large ratio of length and diameter. The dimension of the column had internal diameter of 4.2 cm and length of 30 cm. The ion exchange resin used in this research is a particle monodisperse copolymer stirena-divinylbenzene resin strong base anion type I (Lewatit MonoPlus MP500 OH, Germany). Monodisperse particles have high chemical and osmotic stability (Lanxess Product Information). Strong base anion resin has been shown to be effective in removing arsenic anions. Resin is expected to have strong affinity for phosphate anions, because phosphates such as arsenic are specifically adsorbed in iron oxide [9].

B. Research Procedure

Experiments were conducted with inserted the resin into the column and maintained its position during the operation by installing glass fibers at the base of the column. Adsorption was carried out by flowing the waste that treated according to the predetermined discharge, i.e. 5 mL/min, 10 mL/min, and 15 mL/min through resin media. The volume of resin used were 166 cm³, 194 cm³, and 235 cm³. The research was conducted with downflow system.

During the process, ion exchange occurs in resin with ions in laundry wastewater. The part of the bed that contacts first with waste will reach equilibrium first. When the resin has reached equilibrium, the following parts of the bed will be filled with waste ions. Therefore, the process in the adsorption column is a process that depends on time and distance. If the parts of the bed are saturated, the adsorbate concentration at the bed output will increase. Whether the resin is completely saturated, the release process will occur. The release of substances that have been adsorbed makes the pollutant concentration in the influent has the same concentration on the influent. Thus, the resin has lost the ability to conduct ion exchange.

III. RESULT AND DISCUSSION

A. Effect of Flow rate On Phosphate Removal

Flow rate affects the process of phosphate removal [10]. The Fig.1. explained the variation of waste flow rate had a similarity in the decrease of phosphate concentration. Each flow rate variation showed the percent removal that got bigger until the peak and showed the decline after. Percent removal around 91 to 99.9% on each resin volume variation. At 5 mL/min flow rate, it took a longer processing time compared to 10 mL/min flow rate. Percent removal at 5 mL/min flow rate continued to increase until reached its peak. This occurred in the span of 15 to 60 minutes and decreased by the time.

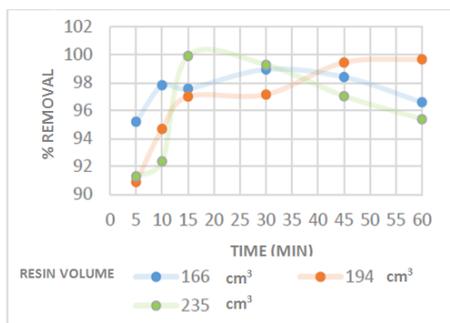


Fig. 1. Correlation of sampling time with percent removal in various resin volume at flow rate of 5 mL/min.

According to Fig. 2., flow rate of 10 mL/min showed a longer saturation point than flow rate of 15 mL/min. Percent removal around 92 to 98% on each resin volume variation. Percent removal at 10 ml/min flow rate continued to increase until reached its peak in a faster time span compared to a flow rate of 5 mL/min which occurred in 10 to 15 minutes. Furthermore, percent removal decreased by the time. This

showed that the greater flow rate of removing phosphate in wastewater is not favorable [10].

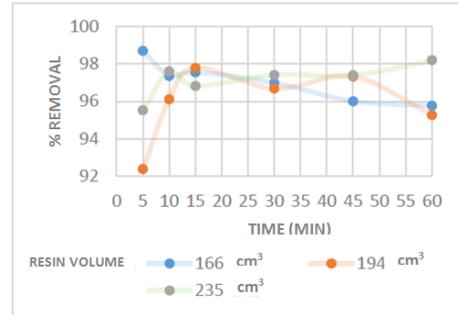


Fig. 2. Correlation of sampling time with percent removal in various resin volume at flow rate of 10 mL/min.

Based on Fig. 3., the percent removal of phosphate at 15 mL/min around 70 to 96% on each resin volume variation. In the resin volume variation of 235 cm³, the percent removal increased at 15 minute of sampling time from 91% to 96% and decreased after its reached the highest peak of removal. However, the resin volume variations in 166 cm³ and 194 cm³ resulted that the percent removal of phosphate decreased without experiencing an increase, due to a short mass transfer zone. Based on study conducted by Fajrianti et al [11] shorter mass transfer zone or faster processing time causes the resin to saturate faster. The condition of saturated anion resin can be seen when percent removal decreased and effluent concentration increased near the initial concentration, so the ion exchange process for phosphate ions did not processed well.

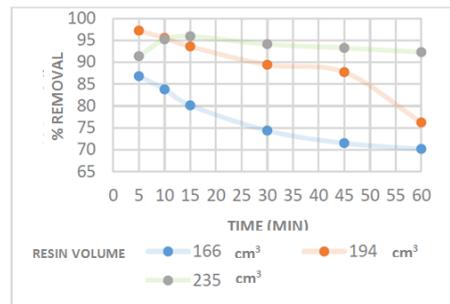
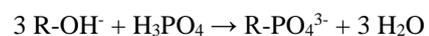


Fig. 3. Correlation of sampling time with percent removal in various resin volume at flow rate of 15 mL/min

According From the research it can be concluded that the phosphate removal was lower at a high flow rate compared to low flow rate. This is due to the rapid contact between the resin and the wastewater, therefore the possibility of phosphate ions being absorbed by the resin is very small. When its compared with a small flow rate, the contact between resin and waste lasts longer, thus the possibility of phosphate ions to be absorbed is greater.

Whether the OH-ion exchange present in the resin is saturated with phosphate ions, it causes many phosphate ions to pass, according to the ion exchange reaction as follows:



PO₄³⁻ ions will replace OH⁻ ions in resin through to all of OH⁻ ions are replaced by PO₄³⁻ ions thus the ion exchange stops. The greater the flow rate flow rate flowing into the column, the smaller the percentage of ion removal. That happens because the greater the flow rate, the shorter the contact time in the column. Moreover, larger flow rate causes the PO₄³⁻ ions to entering the column is increasing therefore the percentage of removal is decreasing.

B. Effect of Resin Volume on Phosphate removal

The volume of anion resin in the adsorption column influences phosphate removal. Based on Fig. 4., the average percent removal was between 70 to 99%. The figure explained the resin volume of 166 cm³ with a flow rate of 5 mL/ min and 10 mL/min percent removal was more stable with a result of the phosphate removal content around 95 to 99%. On the other hand, result of 15 mL/min flow rate was decreased at each sampling time. The result occurred due to a small resin volume and a large flow rate, thus the effectiveness of resin will decrease faster [12].

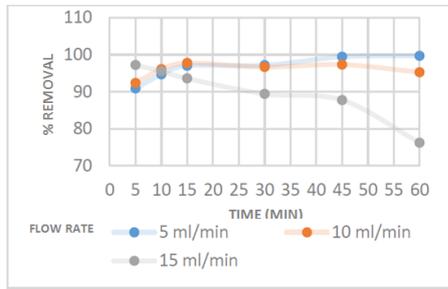


Fig. 4. Correlation of sampling time with percent removal in various flow rate on resin volume of 166 cm³

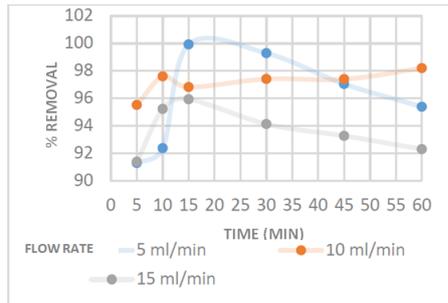


Fig. 5. Correlation of sampling time with percent removal in various flow rate on resin volume of 194 cm³

According to Fig. 5., the average percent removal of phosphate was around 75 to 99%. The figure explained the resin volume of 194 cm³ with a flow rate of 5 mL/min and 10 mL/min showed a stable value of percent removal by resulting removal of phosphate values around 90 to 99%. On the other hand, result of 15 mL/min flow rate was decreased at each sampling time.

Based on Fig. 6., the figure explained that at 5 and 10 mL/min flow rate with the amount of resin less than 235 cm³, phosphate can be removed with a percentage removal around 90 to 99 % and the results were more stable. Whereas if the

process that occurred at 15 mL/min flow rate or greater, a greater amount of resin is needed otherwise the resin will saturate faster. The greater volume of resin in the adsorption column causes the amount of phosphate excreted to be bigger and longer to saturate. This is in accordance with previous studies that the greater the amount of resin used, the number of waste ions that absorbed is greater. Besides that, reference to Nur et al. [12] has the result that the greater amount of resin used, the efficiency of phosphate removal in wastewater is greater. This is due to the increase in the number of active sites available for the adsorption process.

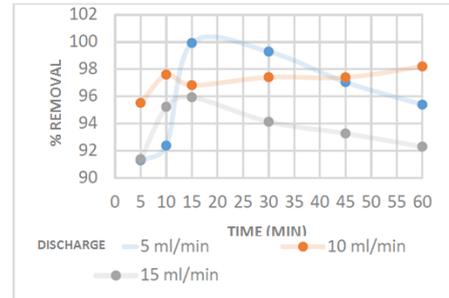


Fig. 6. Correlation of sampling time with percent removal in various flow rate on resin volume of 235 cm³

C. Adsorption Isotherm Modeling

An isotherm model that is fitted for the phosphate removal process in laundry wastewater can be determined by considering at r² which is closest to one. The correlation coefficient (r²) can be calculated by (1):

$$r^2 = \frac{\sum (q_m - \bar{q}_e)^2}{\sum (q_m - \bar{q}_e)^2 + \sum (q_m - \bar{q}_e)^2} \tag{1}$$

Where: q_m = constant of isotherm model
 q_e = the equilibrium capacity obtained from experimental data
 \bar{q}_e = the average of q_e.

Langmuir adsorption isotherm defines that the maximum adsorption capacity occurs due to the presence of a single adsorbate monolayer on the surface of the adsorbent and the entire site surface is homogeneous because each active site can adsorb merely one molecule of adsorbate [13]. Lagmuir isotherm pattern is a strong chemical bond [14]. Langmuir explained that on the surface of the adsorbent there are particular active sites that are proportional to its surface area. The application of Langmuir isotherm assumes that: a) adsorption is solely in the monomolecular, b) localized adsorption, and c) sorption heat does not depend on the surface layer. Langmuir adsorption isotherm can be known by the non-linear formula described in (2) and the linear formula can be expressed in (3-6):

$$q_e = q_m \cdot K_L \cdot \frac{C_e}{1 + K_L \cdot C_e} \tag{2}$$

$$\frac{C_e}{q_e} = \frac{1}{q_m \cdot K_L} + \frac{C_e}{q_m} \tag{3}$$

$$\frac{1}{q_e} = \left[\frac{1}{q_m \cdot K_L} \right] \cdot \frac{1}{C_e} + \frac{1}{q_m} \quad (4)$$

$$q_e = q_m - \left[\frac{1}{K_L} \right] \cdot \frac{q_e}{C_e} \quad (5)$$

$$\frac{q_e}{C_e} = K_L \cdot q_m + K_L \cdot Q_e \quad (6)$$

where C_e = concentration of phosphate solution at equilibrium (mg P/L)

q_e = corresponding adsorption capacity (mg P/g)

q_m = constant of isotherm model (mg P/g)

K_L = constant of net enthalpy of adsorption (L/mg)

TABLE I. ADSORPTION ISOTHERM PARAMETERS OF LANGMUIR, FREUNDLICH AND DUBININ-RADUSHKEVICH

Model	Parameter	Resin Volume (cm ³)		
		166	194	235
Langmuir	q_m (mg P/g)	344.827	322.581	263.158
	K_L (l/mg P)	-3.625	-44.286	-19.000
	r^2	0.499	0.303	0.499
Freundlich	K_f	446.527	338.323	282.958
	N	-9.960	-31.060	-26.880
	r^2	0.879	0.734	0.874
Dubinin-Radushkevich	Q_s (mg P/g)	363.181	323.694	267.736
	K_D (mol ² /kJ ²)	0.073	0.006	0.001
	r^2	0.344	0.264	0.378

Table 1 shows the value of isotherm parameters for each volume resin. In Table 1, the correlation coefficient (r^2) in Langmuir model (0.499, 0.303, and 0.499 for 166 cm³, 194 cm³, and 235 cm³ of volume resin) had small values and all Langmuir adsorption constants were negative (-) number. In the variation of 166 cm³ resin volume had the highest maximum adsorption capacity about 344,8276 mg/gram. Adsorption capacity can be used to determine the volume of reactor needed for the adsorption process. The greater the adsorption capacity, the greater the reactor volume.

The Freundlich's isotherm model can be applied to multilayer and affinities over heterogeneous surface, on the basis of binding energy at each site, where the adsorption process in each layer follows the Langmuir isotherm [13]. Freundlich adsorption isotherms can be known by the non-linear formula described in (7) and the linear formula described in (8):

$$q_e = K_F \cdot C_e^{1/n} \quad (7)$$

$$\ln q_e = \ln K_F + \frac{1}{n} \cdot \ln C_e \quad (8)$$

where K_F = constants of the adsorption capacity

n = constant of the adsorption intensity

As shown in Table 1, the correlation coefficient (r^2) in Freundlich model (0.879, 0.734, and 0.874 for 166 cm³, 194 cm³, and 235 cm³ of volume resin) had greater value compared to Langmuir isotherm. The minus value (-) obtained at the adsorption intensity of (n) is the effect of the small bond energy between the adsorbate and the active site [14].

Dubinin-Radushkevich formulated an isotherm model based on the pore filling mechanism. This is generally applied to express the adsorption process occurs on homogeneous and heterogeneous surfaces [6]. Dubinin-Radushkevich adsorption isotherm can be known by the non-linear formula described in (9,10) and the linear formula described in (11):

$$Q_e = q_s \cdot \exp(-K_{DR} \cdot \epsilon^2) \quad (9)$$

$$\epsilon = RT \cdot \ln\left(1 + \frac{1}{C_e}\right) \quad (10)$$

$$\ln q_e = \ln q_s - K_{DR} \cdot \epsilon^2 \quad (11)$$

where q_s = constant in the Dubinin-Radushkevich isotherm model which are related to adsorption capacity (mg P/g)

K_{DR} = constant in related to the mean free energy of

adsorption (mol²/kJ²)

R = the gas constant (J/mol K)

T = the absolute temperature (K)

Based on Table 1, it is known that the correlation coefficient (r^2) in Dubinin-Radushkevich model (0.344, 0.264, and 0.378 for 166 cm³, 194 cm³, and 235 cm³ of volume resin) had the smallest value compared to Langmuir and Freundlich isotherms. According to the result, the highest value of saturation capacity was obtained by using variations of volume resin of 166 cm³ with 363,1805 mg / gram.

Fig. 7-9 shows the Langmuir, Freundlich, and Dubinin-Radushkevich adsorption isotherms by linear analysis. Correlation coefficient (r^2) generated from each equation has different values due to different assumptions about the adsorption mechanism that occurs between adsorbent and adsorbate on each equation of isotherm [11]. The correlation coefficient (r^2) which is closest to one will determine the most suitable model as a model for phosphate adsorption in laundry wastewater using anion resin. Table 1 showed that the biggest r^2 value was Freundlich Isoterm Model ($r^2 > 0.7341$), while the Langmuir and Dubinin-Radushkevich Isoterm Models had low r^2 value ($r^2 > 0.303$ and $r^2 > 0.2637$).

In table 1, the largest r^2 value were resulted from the freundlich model on 166 cm² anion resin volume in each variation flow rate ($r^2 = 0.8788$). The result suggested that the freundlich isotherm can describe a better adsorption mechanism compared to other isotherm equations. Based on this, the equation to be chosen as the adsorption model is the freundlich isotherm model. With the selection of the freundlich isotherm as the adsorption model, the phosphate adsorption process in laundry wastewater occurs multilayer,

which will form more from one layer on the surface of the adsorbent.

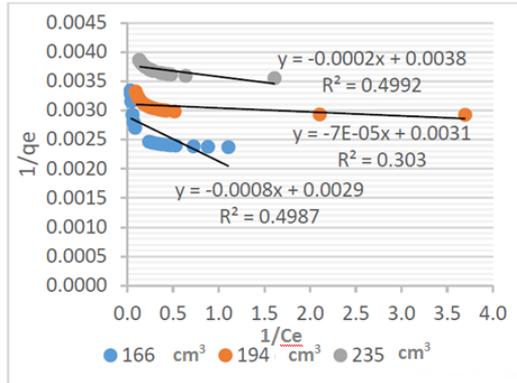


Fig.7. Linear fitting plot of Langmuir adsorption isotherm

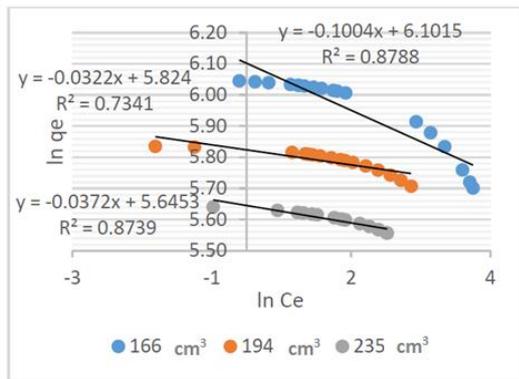


Fig. 8. Linear fitting plot of Freundlich adsorption isotherm

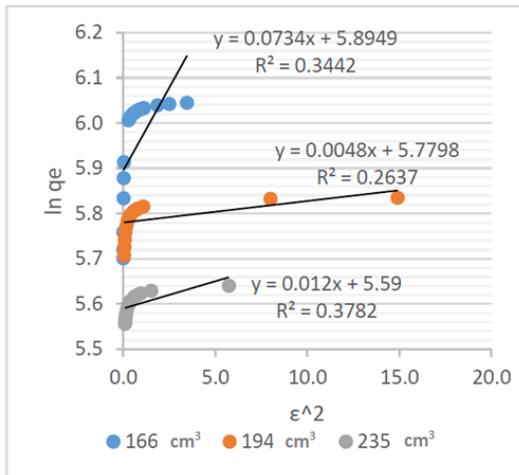


Fig. 9. Linear fitting plot of Dubinin-Raduhkevich adsorption isotherm

Freundlich's isotherm model assumes that there are more than one-layer surface (multilayer) where the adsorption process in each layer follows the Langmuir isotherm and the side is heterogeneous, based on the difference in binding energy on each side of the adsorbent [13]. However, according to Dron's [2] study that all research carried out on ionic-shaped materials and similar adsorbents with anionic resin

should not have an impact on surface heterogeneity. Determination of the maximum adsorption power of anion resin in the phosphate ion adsorption process in the Freundlich model is calculated using the Langmuir isotherm adsorption equation [14]. The calculation results showed that the maximum adsorption capacity of the Lewatit MonoPlus MP500 OH of 166 cm³ resin volume in flow rate (5, 10, and 15 mL/min) was 344.828 mg/gram. This means that every gram of weight of Lewatit MonoPlus MP500 OH anion resin has the ability to remove about 344.828 mg of pollutant weight.

D. One Way ANOVA Test

One Way ANOVA is used for analyze one-way ANOVA model, where the response data structure is written in a column (stacked) and another column as a sub-script of each treatment. One Way ANOVA do the similarity test on the mean of several population classified according to variables or factors. Each variable or factor has a level (treatment). The result of One Way ANOVA statistical analysis using Minitab 2017 software according to the variables in the study explained that The One-Way ANOVA output was obtained p-value = 0.000. The output means that p-value > 0.05 then the result concluded that there is sufficient evidence to say that every treatment will not have same average Phosphate concentrations.

Based on the results of the One-Way ANOVA test defined the difference in the average concentration of phosphate after going through the treatment process. In treatment 1 (Q = 5 mL/min; volume = 166 cm³) showed the smallest average effluent phosphate concentration when compared to other treatments, this means that treatment 1 had efficiency optimal processing. On the other hand, in treatment 7 (Q = 15 mL/min) showed the highest concentration of phosphate effluent when compared to other treatments, meaning that efficiency processing in treatment 7 is the least effective.

TABLE II. TUKEY TEST

Treatment	Mean	Grouping
7 (15 ml.min; 166 cm ²)	19.24	A
8 (15 ml/min; 194 cm ²)	8.7	B
9 (15 ml/min; 235 cm ²)	5.455	BC
3 (5 ml/min; 194 cm ²)	3.57	BC
5 (10 ml/min; 194 cm ²)	3.537	BC
2 (5 ml/min; 194 cm ²)	3.05	BC
4 (10 ml/min; 166 cm ²)	2.552	BC
6 (10 ml/min; 235 cm ²)	2.464	BC
1 (5 ml/min; 166 cm ²)	2.225	C

Based on the Tukey Test that shown in Table 2, on treatments 1, 7, and 8 resulted significantly different effluent phosphate concentration, meaning that the process that carried out with a discharge of 5 mL/min and 15 mL/min had a significant difference in efficiency process. However, in

treatments 2, 3, 4, 5, 6, and 9 showed the identical phosphate concentration effluent.

IV. CONCLUSION

Based from the results of research and discussion conducted, then got the following conclusion:

1. The optimum discharge and volume of resin anion was at discharge of 5 mL/min with variations in volume of 166 cm³ resin.
2. The higher of the flow rate flowing into the column then the percentage ion removal were getting smaller. The increasing flow rate causes the contact time in the column become shorter and makes the ions PO₄³⁻ that goes into the column were abundant. High ions content resulted low removal percentage.
3. The amount of anion resin affects the removal efficiency of phosphate concentration in wastewater.
4. The fitted model for phosphate removal on laundry wastewater using anion resin was the Freundlich isotherm model with the linear equation $y = -0,1004x + 6,1015$ has a value of $r^2 = 0.8788$, Freundlich coefficient (Kf) = 446,527 and maximum adsorption capacity 344,8276 mg / gram.

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