A Multi-functional Micro-machined Gyroscope for Rotating Aircraft

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Abstract. In this paper, we present recent work on the design, fabrication, and packaging of a new gyroscope, by silicon micromachining, for the autopilot of rotating aircraft. The multi-functional micro-machined gyroscope generates the gyroscope effect driven by the roll of rotating carrier, and sense the roll frequency in the longitudinal axis direction of rotating carrier and the transverse angular rate in the perpendicular direction of longitudinal axis of rotating carrier. In addition, the transverse angular rate can be decomposed into the yaw angular rate and pitch angular rate with the geographic coordinates of reference. Therefore, multi-functional micro-machined gyroscope can sense angular rate in three directions, and the signal of gyroscope can be calculated into the five parameters, including the transverse angular rate, azimuth angle, yaw angular rate, pitch angular rate and roll frequency. The new gyroscope has the functions of three the general rate gyroscopes mounted vertically and fits for the attitude control of rotating aircraft.

Introduction

Improvement of control and stability system of aircraft largely depends on the improvement of accuracy and reliability of instrument for measuring the space movement of aircraft. Meanwhile the airborne equipment are seriously crowded in the cabin, many attentions are paid on the miniaturization of mechanical and electrical instruments which include gyroscope and stability systems. Therefore a new gyroscope should be small size, light weight, low power consumption and low prices. In 1990s, a wide variety of silicon micro-machined gyroscope appeared with the development of microelectronics technology. But most of the silicon micro-machined gyroscopes use static electrical force to drive the mass and sense the angular rate of the carrier in the sense mode [1, 2]. In general the performance of vibrating rate gyroscope is strongly influenced by two characteristic modes of motion: (i) the first or fundamental mode defining the drive frequency, and (ii) the secondary mode defining the sense motion [3, 4]. Compared with those gyroscopes, a new gyroscope driven by the rotating carrier is presented, which only has sense motion mode [5, 6]. The drive force comes from the roll of the carrier, so the signal of gyroscope contains the information of the roll frequency of the carrier.

Design and Fabrication

The silicon pendulum of the micro-machined gyroscope contains the pendulum with many damping slots suspended by two torsion girders that are anchored to the outer frame, shown in Fig.1. By applying the roll frequency, ϕ, to the outer frame, the silicon pendulum rotates with the outer frame about the Z axis. An angular rate, Ω, applied about the X axis, generates a Coriolis force that acts to push the pendulum in and out of the frame of oscillation, i.e. sense motion.
In general the sense motion is a forced damped vibration and can be described for a rotational angle $\alpha$, torque $K_T$, the moment of inertia $J_X$, $J_Y$, $J_Z$ and damping factor $\zeta$. The roll frequency and transverse angular rate of the carrier is $\dot{\phi}$ and $\dot{\Omega}$.

$$\begin{align*}
    J_Y \ddot{\alpha} + \zeta \dot{\alpha} + \left[ \left( J_Z - J_X \right) \dot{\phi}^2 + K_T \right] \alpha &= \left( J_Z + J_Y - J_X \right) \Omega \dot{\phi} \cos(\dot{\phi} t) \\
    \text{The stationary solution of Eq. 1 is [7]} &= \frac{\left( J_Z + J_Y - J_X \right) \dot{\phi}}{\sqrt{\left[ \left( J_Z - J_y - J_X \right) \dot{\phi}^2 + K_T \right]^2 + (\zeta \dot{\phi})^2}} \Omega \cos(\dot{\phi} t - \beta)
\end{align*}$$

where $\beta$ is the phase difference between the oscillation phase and the direction of the transverse angular rate.

The rotational angle of silicon pendulum is determined by the Coriolis force, and the oscillation frequency of silicon pendulum is equal to the roll frequency of the carrier.

Starting from a standard 4” two-side polished silicon wafer, a thick thermal oxide layers are grown on both sides of the wafer. In the first lithography, silicon oxide etching and silicon etching step, the pendulum thickness and the outer frame are realized. Another thick thermal oxide is grown. Onto this pendulum, the damping slots are opened in the second lithography, silicon oxide etching and silicon etching step. The pendulum is released in the third and fourth lithography, silicon oxide etching and silicon etching step. The third thick thermal oxide is grown. The torsion girders are realized in fifth lithography, silicon oxide etching and silicon etching step. Two electrode plates are glued on the silicon chip encapsulating the whole pendulum element. The shell and lid provide a hermetical sealing, shown in Fig.2.

**Signal Demodulation Method**
The gyroscope signal is the amplitude modulation ware. The change of signal amplitude reflects the change of input angular rate, and the change of signal frequency reflects the change of the roll frequency of the rotating aircraft.

The signal of micro-machined gyroscope is

\[
U = \frac{K_2\left(J_2 + J_4 - J_6\right)\phi}{\sqrt{\left(J_2 - J_4 - J_6\right)\dot{\phi}^2 + \left(K_J + J_7\right)^2 + (\dot{\phi})^2}} \Omega \cos(\dot{\phi} - \beta) \tag{3}
\]

where \(K_2\) is the capacitance pick-up factor. Eq. 3 can be simplified into

\[
U = K(\phi) \Omega \cos(\dot{\phi} - \beta) \tag{4}
\]

where \(K(\phi)\) is the scale factor of micro-machined gyroscope, which is measured with different roll frequency and different transverse angular rate. Therefore \(K(\dot{\phi})\) is the polynomial of the roll frequency.

\[
K(\phi) = a_0 + a_1 \phi + a_2 \phi^2 + a_3 \phi^3 \ldots \tag{5}
\]

The Hilbert transform of Eq. (4) is

\[
\hat{U}(t) = K(\phi) \Omega \sin(\dot{\phi} - \beta) \tag{6}
\]

where \(\hat{U}\) is Hilbert transform of \(U\).

The roll angle of the carrier is obtained by divide Eq. (6) by Eq. (4). The roll frequency of the carrier is the differential of the roll angle.

\[
\dot{\phi} - \beta = \arctan\left(\frac{\hat{U}}{U}\right) \tag{7}
\]

The transverse angular rate \(\Omega\) is

\[
U_\phi^2(t) + U_\beta^2(t) = K^2(\phi) \hat{\Omega}^2 \cos^2(\dot{\phi} - \beta) + K^2(\dot{\phi}) \hat{\Omega}^2 \sin^2(\dot{\phi} - \beta) \tag{8}
\]

\[
\Omega = \frac{1}{K(\dot{\phi})} \sqrt{U_\phi^2(t) + U_\beta^2(t)} \tag{9}
\]

The transverse angular rate can be decomposed into the yaw angular rate and pitch angular rate with the geographic coordinates of reference. A micro-machined accelerometer is an ideal geographic coordinates of reference, because it can sense the direction of gravity and not be influenced by the angular rate. The signal of accelerometer is

\[
U_a(t) = A \sin(\dot{\phi} - \chi) \tag{10}
\]

where \(A\) is a constant amplitude of signal which is only related with the gravity; \(\chi\) is the phrase of signal which induces the direction of the gravity and is used as the geographic coordinates of reference.

The azimuth angle of transverse angular rate is

\[
\theta = \beta - \chi \tag{11}
\]

The yaw angular rate is

\[
\Omega_\phi = \Omega \sin(\theta) \tag{12}
\]

The pitch angular rate is

\[
\Omega_\beta = \Omega \cos(\theta) \tag{12}
\]

**Experiments and Results**

Normally the movement of rotating aircraft is the coning motion, which the rotating aircraft rolls about its longitudinal axis and its head moves in eclipse, shown in Fig. 3.
The ground simulation experiments use the three-axis turntable to simulate the coning motion. The micro-gyroscope is mounted on the plate of the inner loop of the turntable. The inner loop rolls at the specific speed, the middle loop oscillates in the pitch direction, and the outer loop oscillates in the yaw direction.

In this experiment, the roll frequency of the inner loop is set at 15Hz. The middle and outer loops are set at 1Hz, 5°. The results show in Fig.4 and the insert (a), (b), (c), (d) and (F) illustrate the signal of transverse angular rate, the signal of azimuth angle, the signal of yaw angular rate, the signal of pitch angular rate and the signal of roll frequency which are demodulated from the signal of gyroscope.

![Fig.3 Coning motion of micro-machined gyroscope](image)

![Fig.4 Signal demodulation result of micro-machined gyroscope](image)

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Conclusion

This new gyroscope was designed to meet the requirement of rotating aircraft. The gyroscope can sense the roll of rotating aircraft and the transverse angular rate in 360 degree space. The gyroscope signal can be demodulated into the transverse angular rate, azimuth angle, yaw angular rate, pitch angular rate and roll frequency. The yaw and pitch angle error of demodulation is 6.43%.

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