Study of Double-holding Water Tank Liquid Level Control Base on Neural Networks PID Control

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Abstract—Aiming at the problem of the effect of longtime delay and nonlinear of the double-tank's level control, the PID control of BP neural network tuning parameters is studied in this paper. The characteristics of the control system are analyzed minutely, a neural PID controller is designed and its control algorithm is derived. Simulation control program is compiled in MATLAB, and the program is applied to the experimental platform, then a better control effect is obtained after software debugging and parameter optimization. The results show the effectiveness and correctness of the control method.

Keywords—double-holding water tank; liquid level control; BP neural networks; PID control

I. INTRODUCTION

As a typical representative of the process control, level control of the double-tank is one of the hotspots in the research of process control experts. Due to longtime delay, nonlinear characteristics and complexity of the control system, the control effect has been affected by the system’s initial state, control algorithms and parameters directly [1-3]. The classical PID control is difficult to achieve satisfactory control effect, because the parameter optimization is not easy; Fuzzy control is a classical intelligent control method, it can achieve a better control effect as long as the design is reasonable. But fuzzy control is built on the basis of fuzzy logic reasoning, so the demands for designers’ experience are stringent. of course, there are many other control methods that experts and scholars are studying [4,5]. Combined with the characteristics of the process control experimental platform, the application of the neural PID method is studied for the level control of the double-tank in this paper.

II. CHARACTERISTICS OF DOUBLE-HOLDING WATER TANK

This paper is based on the THKGK-1 process control system experimental device. Combining with the upper monitor PC machine which forms a complete and complex control system, and the control system can complete the temperature, pressure, flow, liquid level control and et al, level control of the double-tank is one of them. The double-tank level control is a typical object of the process control, it has the characteristics that its own longtime delay, object’s nonlinear with the parameter variation and complex of the control system, and different control algorithm affects the accuracy of control directly.

System principle is the measured object which is composed of two water tanks with different volume in series, so it is called the two-volume object. The principle of two-link water tanks is cascaded two different volume physical tanks, as shown in Figure I.

The controlled variable in this system is the liquid level of the lower water tank. When the input quantity of the upper water tank has a step increment change, the change curve of liquid level of the two water tank is shown in Figure II. Figure II (a) shows that the response curve of the upper water tank liquid level which is a monotonically increasing exponent curve. However, in Figure II (b), the response curve of the lower water tank liquid level is "S" curve. That is to say, the liquid level response of the lower tank is delayed, it has a great relationship between time delays and characteristics of the system, for instance, the opening size of water inlet valve and water outlet valve are equal.

FIGURE I. THE PRINCIPLE OF TWO-LINK WATER TANKS
The mathematical model of double-tank is the product of mathematical model of two single-container water tank, which can be described as two first-order inertial link. Coupled with system pure time delay, the transfer function can be obtained:

$$
G(s) = G_1(s)G_2(s) = \frac{k}{(T_1s + 1)(T_2s + 1)}e^{-\tau s}
$$

(1)

Where, $k$ is the amplification factor of the double-tank, $T_1$ and $T_2$ are constant time of the double-tank, $\tau$ is the lag time.

Due to the time delays of the system is closely related to the size of the water inlet valve and water outlet valve. After changing the corresponding valve opening, the object may appear some hysterics characteristics with different degrees, so the classical control method is difficult to achieve satisfactory control effect. The fuzzy control has been used to carry on the research, the control effect is improved compared with the traditional PID control (the control algorithm of the experimental system itself), but there are still some disadvantages. For example, overshoot is too large, so this paper attempts to use the neural PID for further study.

### III. DESIGN OF NEURAL PID CONTROL

The better effect of PID control based on the best adjustment parameter of the proportion, integral and differential, it forms

$$
\Delta u(k) = k_p[e(k) - e(k-1)] + k_i\int e(k) + k_d[e(k) - 2e(k-1) + e(k-2)]
$$

(2)

Where, $k_p$, $k_i$, $k_d$ are parameters of proportion, integral and differential respectively.

According to the running state of the system, adjusting the parameters of the PID controller can achieve the optimization of a certain performance index. The output state of the output layer neuron corresponds to the three adjustable PID controller’s parameters $k_p$, $k_i$, $k_d$. By the neural network learning itself and the adjustment of weighting coefficients, the output of the neural network is corresponding to the PID controller’s parameters with some optimal control law. The specific network algorithm [8] is as follows:

The input of the network input layer is: $x(j)$;

The output the network input layer is: $o^{(1)}_j = x(j)$, $j=1$;

The input of the network hidden layer is: $net^{(2)}_i(k) = o^{(2)}_i$;

The output of network hidden layer is: $o^{(2)}_j(k) = f(net^{(2)}_j(k))$, $i=1,2,3$;

The input of the network output layer is:

$$
net^{(3)}_p(k) = \sum_{j=1}^{3} o^{(3)}_j(k)
$$

The output is: $o^{(3)}_p(k) = f(net^{(3)}_p(k))$, $p=1,2,3$;

In the above formulas, $o^{(1)}_j$ is weighted coefficient; the superscript(1), (2), (3) are input layer, hidden layer and output layer respectively.
layer respectively. The activation function of the hidden layer and the output layer are all the S function, which is 
\[ y = f(s) = 1/(1 + e^{-s}) \].

The output nodes of the output layer correspond to the three adjustable parameters, which are \( o_{i}^{(3)} = k_{p}, o_{2}^{(3)} = k_{i}, o_{3}^{(3)} = k_{d} \).

Performance index function: 
\[ E(k) = [(r(k) - y(k))^2 / 2] \].

With the improved BP network learning algorithm, the weights of the network are modified according to the negative gradient descent method:

\[ \Delta w_{pi}^{(3)}(k) = -\eta \frac{\partial E(k)}{\partial w_{pi}^{(3)}} + \alpha \Delta w_{pi}^{(3)}(k - 1) \quad (3) \]

\[ \Delta w_{pi}^{(3)}(k) = \alpha \Delta w_{pi}^{(3)}(k - 1) - \eta \frac{\partial E(k)}{\partial y(k)} \cdot \frac{\partial y(k)}{\partial u(k)} \cdot \frac{\partial u(k)}{\partial o_{p}^{(3)}(k)} \cdot \frac{\partial o_{p}^{(3)}(k)}{\partial \Delta u(k)} \cdot \frac{\partial \Delta u(k)}{\partial \Delta w_{pi}^{(3)}} \cdot \delta_{i}(k) \]

\[ = \alpha \Delta w_{pi}^{(3)}(k - 1) - \eta \cdot e(k) \cdot \frac{\partial y(k)}{\partial u(k)} \cdot \frac{\partial u(k)}{\partial o_{p}^{(3)}(k)} \cdot f(\text{net}_{p}^{(3)}(k))(1 - f(\text{net}_{p}^{(3)}(k)))o_{i}^{(2)}(k) \quad (5) \]

Similarly, the learning algorithm of the hidden layer weight coefficient can be get:

\[ \Delta w_{ij}^{(2)}(k) = -\eta \frac{\partial E(k)}{\partial w_{ij}^{(2)}} + \alpha \Delta w_{ij}^{(2)}(k - 1) \quad (6) \]

Where,
\[ \lambda = e(k) \cdot \frac{\partial y(k)}{\partial u(k)} \cdot \frac{\partial u(k)}{\partial o_{p}^{(3)}(k)} \cdot f(\text{net}_{p}^{(3)}(k))(1 - f(\text{net}_{p}^{(3)}(k))) \]

IV. EXPERIMENTAL STUDY

According to the characteristics of the controlled object and the analysis of the learning algorithm, system learning rate \( \eta = 0.12 \), inertia coefficient \( \alpha = 0.035 \), the initial value of the weighted coefficient takes the random number\[9\] that based on the \(-0.5~0.5\). Write the control program in MATLAB\[7\], the program is applied to the experimental system, and its running results are shown in Figure V. In order to compare the control effect, the classical PID control results and fuzzy control results are given (In the same condition, the results of three kinds control method), as is shown in Figure VI and Figure VII.

From the results it can be conclude that the neural PID control improves the speediness and overshoot greatly, so its control effect is best, and the fuzzy control effect is better, and single PID control effect is poor.

V. CONCLUSION

In the view of control system of double-tank, the neural PID control is studied, the results are compared with the single PID control or single fuzzy control, the control effect is improved obviously. Although the control structure and algorithm are more complex, the experimental results show that it is a best control effect can be achieved by using the parameter adaptive neural PID control.
REFERENCES


