

Casting Aluminum Fatigue Assessment Correction Method Based on Crack Propagation Prediction

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Abstract. The fatigue requirement of casting aluminum alloy is varied for different industry, however, it is hard to avoid porosity, shrinkage, or slag during the casting process, leading to uneven quality of casting. the fatigue strength will be influenced by casting porosity, DAS length or stress level. This paper takes single reduction gearbox housing (material for AlSi₇Mg_{0.3}) as an example to analyze the prediction algorithm of crack propagation, deduce the key parameters for deciding crack propagation, and carry out a series of experimental studies for casting aluminum fatigue. According to the results of calculation and experiment, the correction coefficient is introduced based on FKM guideline and EN 1999 standard, besides, the evaluation method of fatigue strength has been corrected. As one example, the test results show that if casting aperture diameter more than 0.5 mm, the stress amplitude of fatigue load should not be more than 38.28MPa for 1×10^7 load cycles.

Introduction

Since the casting aluminum alloy has many advantages, such as small density, high strength, corrosion resistant and easy to shape, it can be widely used in aviation, railway, automobile and other industrial fields. With the improvement of alloy smelting process, the performance of aluminum alloy has been improved continually. The mechanical properties, low temperature performance and wear resistance performance have been full played. However, in view of different needs of different industries, the fatigue requirements of casting aluminum alloy are quite different, due to the casting process is hard to avoid porosity, shrinkage or slag, that often cause uneven casting quality although evaluate fatigue limitation base on the same requirements. By contrast, the real life is very different, which will impact fatigue limit including low cycle and high cycle^[1-5]. How to accurately assess the fatigue limit according to the level of casting defects is mainly study content in this article. The FKM guideline did not elaborate the numerical relationship between aperture diameter and fatigue limitation, the parameters such as j_G and j_F need to be adjust appropriately, besides, despite EN1999 standard(Eurocode9:Design of aluminum structures) stipulated the relationship between the aperture diameter levels and the fatigue limitation, but the 10^7 times cycles corresponding to the fatigue limitation was not clearly given.

This article takes the single reduction gearbox housing of China high-speed EMU as example(the housing material is AlSi₇Mg_{0.3}), in view of this type housing existed a batch of cracks, it is necessary to carry out evaluation method research comprehensively, therefore, a series of experimental studies for casting aluminum fatigue have been made, and the predicting methods of casting aluminum crack propagation has also been introduced.

According to the calculation and test results, the fatigue correction coefficients have been forwarded, the fatigue evaluation methods have been amended, the recommended value of fatigue limit for $AlSi_7Mg_{0.3}$ casting aluminum alloy has been introduced.

Problem Statements

As an example, the $AlSi_7Mg_{0.3}$ housing crack fault is shown in figure1, according to fracture analysis, there are obvious fatigue striations, as shown in figure2, according to metallographic analysis, the fracture reason belongs to fatigue crack. Once the crack occurred, the fatigue striations will be the results of high stress intensity. However, due to casting quality and evaluation approach will take a great influence on prospective life of $AlSi_7Mg_{0.3}$ housing, therefore, it is necessary to re-determine fatigue assessment thresholds for housing crack problems.



Fig1. Crack fault of gearbox housing

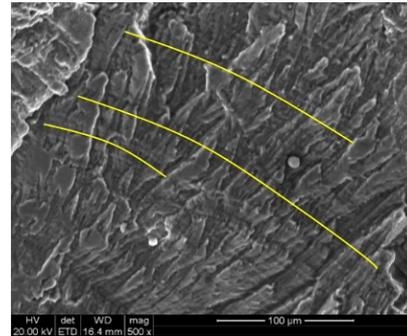


Fig2. Fatigue striations of housing fracture

Prediction method of crack extension

The stress method and strain gauge method have been widely used to predict fatigue life in engineering field, for some complicated structure or complex stress, using the two methods to predict fatigue life is inaccurate. In the early stages of crack extension, the crack tendency T- in the region of total product extension. In this paper, the crack extension life is determined by the crack propagation life. Assume that the $AlSi_7Mg_{0.3}$ materials is elastic solid, a-Al-matrix is elastoplasticity, the Si is rigid elastic solid, the Young's modulus and Poisson's ratio are shown in Table 1.

Table 1. Property parameter of $AlSi_7Mg_{0.3}$ material

Material	Young modulus (GPa)	Poisson ratio
$AlSi_7Mg_{0.3}$	70	0.3
a-Al-matrix	6089	0.33
Si grain	130	0.28

Life Equation of crack formation according to the aluminum alloy material as Equation (1)^[6-10]:

$$N_i = \frac{C_0}{I_2} \left[\frac{1}{s_a} \left(k_0 + \frac{a}{\sqrt{I_2}} \right) \right]^{\frac{2}{b}} \tag{1}$$

In Equation (1):

I_2 -The length of dendrite arm spacing (DAS);

s_a -stress amplitude;

b -Constant of material properties;

C_0, k_0, a -Constants determined by material properties.

The crack propagation prediction formula as Equation (2).

$$\frac{dL}{dN} = C \left[\left(e_{\max} \frac{s_a}{s_Y} \right)^{-s} L \right]^t \quad (2)$$

In Equation (2):

L - Crack length;

e_{\max} - The maximum strain of cyclic load;

s_Y - Yield stress of material;

s, t, C - Constants;

L_0 -The initial crack length;

L_f -The final crack length;

Under the same loading condition, increase yield stress will reduce speed of crack propagation, because increasing material yield strength is beneficial to reduce the amount and area of plastic deformation in the interior of materials, as results, the displacement reduction among crystal particles in crystallographic orientation region, the possibility of fatigue crack on the crack tips will be reduced. Using the initial crack length L_0 and final crack length L_f to instead of L in Equation (2), it will be translated into Equation (3).

$$N_p = \frac{dL}{dN} = C_1 \left(e_{\max} \frac{s_a}{s_Y} \right)^{-s \times t} (L_0^{-t+1} - L_f^{-t+1}) \quad (3)$$

Assume that the initial crack length L_0 is equal to $2I_2$. In order to find the overall fatigue life, the crack initiation life and crack propagation life have been added, as Equation (4):

$$N_f = N_p + N_i = \frac{C_0}{I_2} \cdot \left[\frac{1}{s_a} \left(k_0 + \frac{a}{\sqrt{I_2}} \right) \right]^{\frac{2}{b}} + C_1 \left(e_{\max} \frac{s_a}{s_Y} \right)^{-s \times t} \cdot (L_i^{-t+1} - L_f^{-t+1}) \quad (4)$$

The fatigue life of housing is mainly affected by pores (shrinkage), DAS length and stress level, according to the specification of gearbox, the fatigue life of housing needs to reach 10^7 loading cycles, combine the data of housing fatigue testing, the crack propagation life N_p is greater than the initial crack formation life N_i , Equation (4) is approximate to Equation (5):

$$N_f \approx N_p = C_1 \left(e_{\max} \frac{s_a}{s_Y} \right)^{-s \times t} (L_0^{-t+1} - L_f^{-t+1}) \quad (5)$$

Assume the L_0 can be expressed by equivalent pore diameter of crack formation (assume $L_0 = 0.5mm$), and the final fatigue failure length $L_f = 5mm$, set constant : $C = 1.04 \times 10^{-5}$, $s = 1.05$, $t = 1.94$, e_{\max} and s_a are abbreviated to $e_{\max} = \frac{s_{\max}}{E}$ and $s_a = \left(\frac{1-R}{2} \right) s_{\max}$ respectively, E is young's modulus of $AlSi_7Mg_{0.3}$ in condition T6, s_Y is material yield strength $AlSi_7Mg_{0.3}$ in condition T6, set $E = 70GPa$, set $s_Y = 190MPa$. s_{\max} and R represent the maximum stress and maximum stress ratio respectively, assume $s_{\max} = s_{w,zd} = 70MPa$, considering the actual case of housing during operation process will undergo tension and compression load, so $R = -1$, and at this time $s_a = s_{\max}$, the calculation method of stress ratio R is defined by the Equation (6):

$$R = \frac{s_m - s_a}{s_m + s_a} \quad (6)$$

In Equation (6): s_m - average stress; s_a - stress amplitude;

Take parameters of Equation 6 into Equation 5, we found out the $N_f \approx 1.04 \times 10^6$ loading cycles. It is easy to see that in Equation (5), the two key parameters affecting crack propagation life

are equivalent aperture diameter L_0 and load stress amplitude s_a . Therefore, in order to achieve expected fatigue life, we need prescribe the allowable stress s_a which corresponding to L_0 .

Correction Algorithm of Fatigue Evaluation

According to the fatigue regulations of casting aluminum alloy material in FKM-2012 guideline and DIN EN-1706 standard, the fatigue strength of AlSi₇Mg_{0.3} as follow Table2^{[11][12]}.

Table2. Fatigue strength of AlSi₇Mg_{0.3} material

Casting process	Material (Condition T6)	Fatigue strength of AlSi ₇ Mg _{0.3}
		Material $s_{w,zd}$ (MPa)
Sand casting	AlSi ₇ Mg _{0.3}	70

The fatigue strength 70MPa of AlSi₇Mg_{0.3} material in Table2 refers to ideal casting quality, however, the reality casting often contains aperture and porosity, see below figure3 and figure4 as examples, we can obviously the see casting porosity and slag produced from figure3 and figure4 due to uneven casting quality. Thus, we need to focus on different fatigue strength corresponding to different casting aperture diameter.

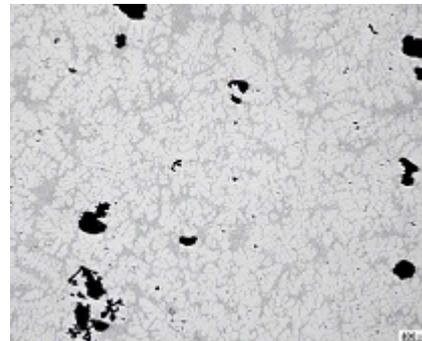
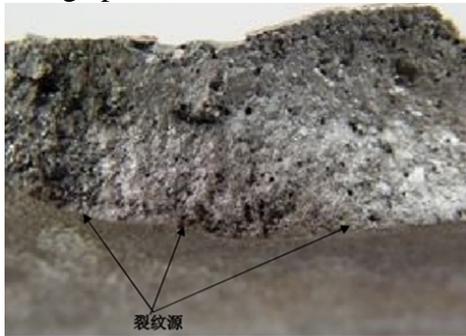


Fig3. Appearance in the fracture area Fig4. metallographic structure in the fracture area

In fact, the EN1999-1-3 standard for casting aluminum alloy aperture grades explained the relationship between casting aperture and fatigue strength, see Table3^[13], but the fatigue strength corresponding to $N_D = 1 \times 10^7$ cycles is not be clearly defined, which is focus of research in this article.

Table3. Fatigue strength of AlSi₇Mg_{0.3} corresponding to different casting aperture diameter base on EN1999-1-3 [Mpa]

Detail Category	Casting Aperture (mm)				
	0.2mm	0.5mm	0.9mm	1.5mm	2.0mm
$N_D = 2 \times 10^6$	71	50	40	32	25
$N_L = 1 \times 10^8$	40.6	28.6	22.9	18.3	14.3

According to FKM guideline, the minimum safety factor (J_D) calculation method is defined by the Equation (7):

$$J_{Di,j} = j_s \cdot \frac{j_{Fi} \cdot j_{Gj}}{k_{T,D}} \quad (7)$$

In Equation (7):

$j_s = 1.0$, loading safety coefficient (recommended value for safety design);

$j_{Fi} = 1.5 \sim 1.3$, material safety coefficient (recommended value refer to table 3, $i = 1 \sim 5$);

$j_{Gj} = 1.0 \sim 1.4$, casting coefficient (recommended value refer to table 3, $j = 1 \sim 5$);

$k_{T,D} = (1 \sim 1.2) \times 10^{-3} (T / ^\circ C - 50)$ (Recommended temperature coefficient, this article set $k_{T,D} = 1$);

For the j_{Gi} and j_{Fj} , this article references EN1999-1-3 standard for casting aluminum alloy porosity grades classification, as Table 4.

Table4. Coefficients Corresponding to Different Casting Aperture Diameter Base on FKM (1×10^7 cycles)

Casting Aperture (mm)	0.2	0.5	0.9	1.5	2.0
Casting Coefficient j_{Gi}	j_{G1}	j_{G2}	j_{G3}	j_{G4}	j_{G5}
material safety coefficient j_{Fj}	j_{F1}	j_{F2}	j_{F3}	j_{F4}	j_{F5}

Set $j_{G1} = 1.0$, $j_{F1} = 1.3$, $j_{G5} = 1.4$, $j_{F5} = 1.5$, according to Equation (7), the $J_{D1,1} = 1.3$ and $J_{D5,5} = 2.1$. Reference the stress calculation methods of FKM corresponding to different loading cycles as figure5, the fatigue strength ΔS_i of AlSi₇Mg_{0.3} can be calculated by Equation (8).

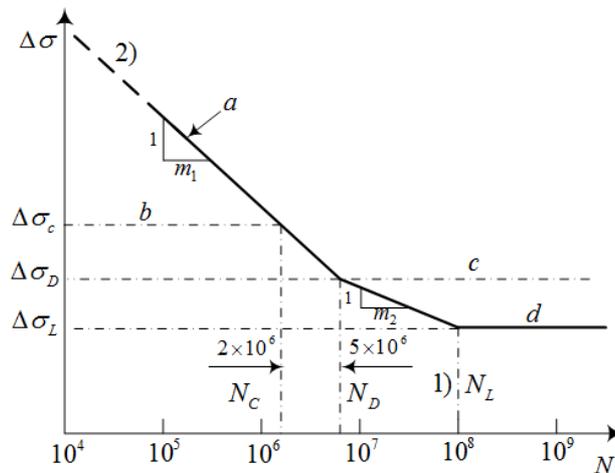


Fig5. Fatigue strength curve of casting of aluminum alloy

Notes: a-fatigue strength curve; b - reference fatigue strength; c – constant amplitude fatigue limit; d – cut off limit; ΔS -nominal stress range; ΔS_c - the stress of N_c times load cycles; ΔS_D -constant amplitude stress; ΔS_L -cut off limit stress; N_c - 2×10^6 times load cycles; N_D - 5×10^6 times load cycles; N_L - 10^8 times load cycles.

In above figure5, when the fatigue load cycles N_i in the range between 5×10^6 to 1×10^8 cycles, the fatigue strength calculate method is defined by the Equation (8):

$$\Delta S_i = \frac{\Delta S_c}{\sqrt{\frac{N_i}{5 \times 10^6}}^{m_2} \cdot \sqrt{\frac{5}{2}}^{m_1} \cdot g_{Ff} \cdot g_{Mf}} \tag{8}$$

In Equation(8) :

N_i —The predicted number of cycles of failure of a stress range ΔS_i (The target cycles $N_i = 1 \times 10^7$);

ΔS_c —Fatigue strength of material ($\Delta S_c = 70MPa$);

ΔS_i —The fatigue strength under N_i load cycles;

g_{Ff} —The density coefficient of fatigue load (in this article ,recommended value is $g_{Ff} = 1.0$);

g_{Mf} —Fatigue strength coefficient (In this article ,recommended value is $g_{Mf} = 1.0$);

m_1 —The inverse slope of $\Delta S - N$ curve (In this article recommended value is $m_1 = 7$);

m_2 —The inverse slope of $\Delta S - N$ curve (In this article recommended value is $m_2 = m_1 + 2$);

So the ΔS_i is defined by the Equation (9) :

$$\Delta S_i = \frac{70 \times \sqrt[7]{\frac{2}{5}}}{\sqrt{2}} = 56.84(MPa) \tag{9}$$

According to Table4, this article revised calculation method of fatigue strength ,as follow Equation (10):

$$\Delta S_i^* = \frac{\Delta S_i}{J_{Di,j}} \tag{10}$$

Consequently, $\Delta S_1^* = 43.72MPa$, $\Delta S_5^* = 27.07MPa$.

Other reference values of AlSi₇Mg_{0.3} fatigue strength corresponding to different casting aperture diameter showing in Table3.

In figure6, it is easily to find out that when the diameter of casting aperture reach to 2.0mm, the fatigue strength (1×10^7) is $\Delta S_5^* = 27.07MPa$,which more than the fatigue strength corresponding to 1×10^8 cycles, obviously, this result is unreasonable for fatigue strength evaluation of AlSi₇Mg_{0.3}. Thus, we should adjust j_{Gi} or j_{Fj} to meet ΔS_i^* between curve 2×10^6 and curve 1×10^8 .

This article suggest $j_{Fi} = 1.7 \sim 1.3$ as well as reallocate the parameters as follow Table5:

Table5. Revised Coefficients Corresponding to Different Casting Aperture Diameter (1×10^7)

Casting Aperture (mm)	0.2	0.5	0.9	1.5	2.0
Casting Coefficient j_{Gi}	1.3	1.35	1.5	1.6	1.7
material safety coefficient j_{Fj}	1.0	1.1	1.2	1.3	1.4

As result, the fatigue curve (1×10^7)with revised coefficients as follow figure7,which is a reasonable result between curve 2×10^6 and curve 1×10^8 .

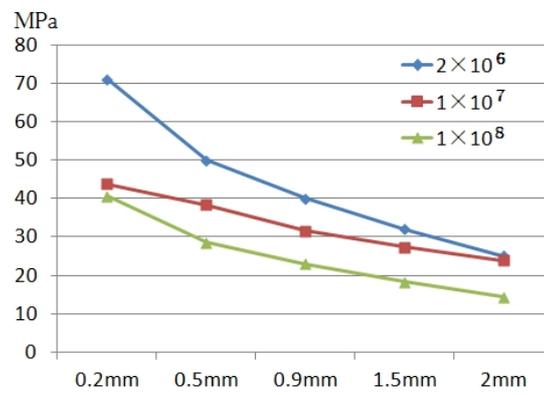
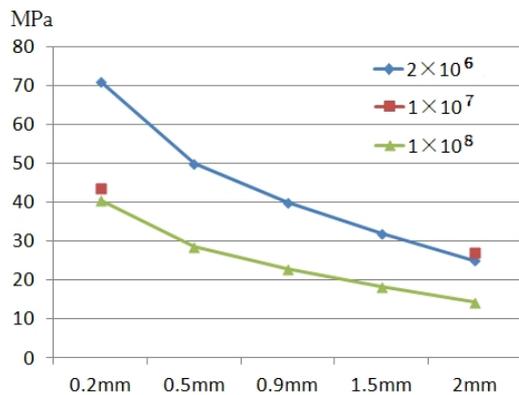


Fig6. Fatigue strength curve of AlSi₇Mg_{0.3} Fig7. The revised fatigue strength curve of AlSi₇Mg_{0.3}

This article corrected fatigue assessment values of AlSi₇Mg_{0.3} casting aluminum alloy, the recommended values for various conditions can be seen in Table6. Considering the minimum safety coefficient should be more than 1.0 for actual product, the special values should be determined according to loading conditions corresponding to different structural positions.

Table6. Recommended values for evaluation of AlSi₇Mg_{0.3} fatigue strength

Casting process	Material (Condition T6)	Fatigue strength of AlSi ₇ Mg _{0.3} Material $S_{w,zd}$ (MPa)	Casting aperture (mm)	The corrected fatigue strength ΔS_i^* (MPa)
				1×10^7
Sand castings	AlSi ₇ Mg _{0.3}	70	0.2	43.72
			0.5	38.28
			0.9	31.58
			1.5	27.33
			2.0	23.88

Testing verification

In order to verify the revised values of fatigue evaluation for $AlSi_7Mg_{0.3}$, we selected a new housing product from the same structure products, the same technique and the same batch to equip strain gauge in the corresponding crack location^[14], we demand the maximum casting aperture diameter (more than 0.5 mm) is not be allowed, besides that, we did vibration simulation test on the test bench, the test conditions simulated actual operation condition between two railway stations, the test case as below figure8.



Fig8. Dynamic stress experiment for housing crack location

Under the vibration condition, the dynamic stress measurement points will be affected by load of tension and compression, the test data is shown in figure9, in which stress data more than $\pm 38.28\text{MPa}$ are shown by oval-ring note.

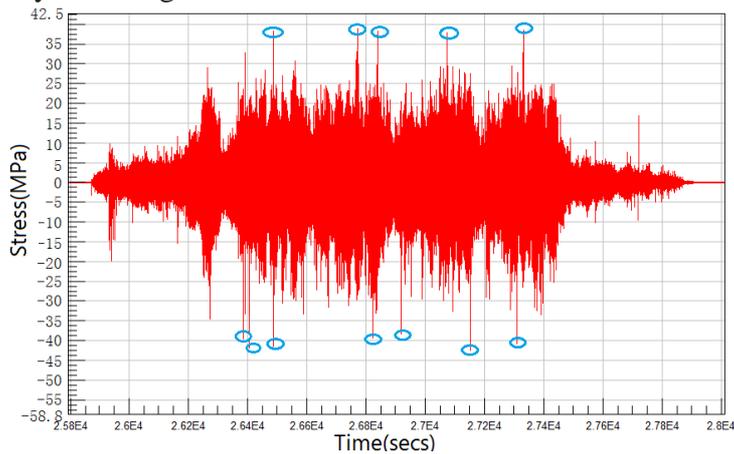


Fig9. Data of dynamic stress experiment

Reference the table 6 and figure9, it is not difficult to understand that if the casting aperture diameter bigger than 0.5 mm in crack position the fatigue fracture can be caused by vibration load easily when stress reach to 38.28MPa and above. In addition, we selected five new housing products to extract five pieces of samples, which in corresponding to crack position, as well as we did bending fatigue test on the fatigue test bench, the test method as figure10.

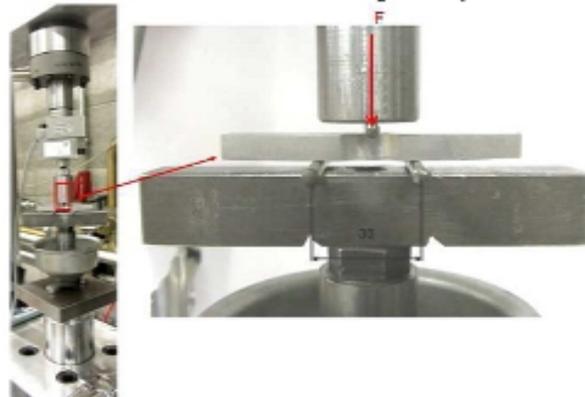


Fig10. Fatigue test of samples for $AlSi_7Mg_{0.3}$ housing

Based on test results, the S-N curve scatter diagram of test results from extracted five pieces samples as shown in figure11, the red curve represents FKM specified curve of $AlSi_7Mg_{0.3}$, when the fatigue loading cycles reached to 1×10^7 cycles, there are two pieces of samples stress lower than 38.28MPa.

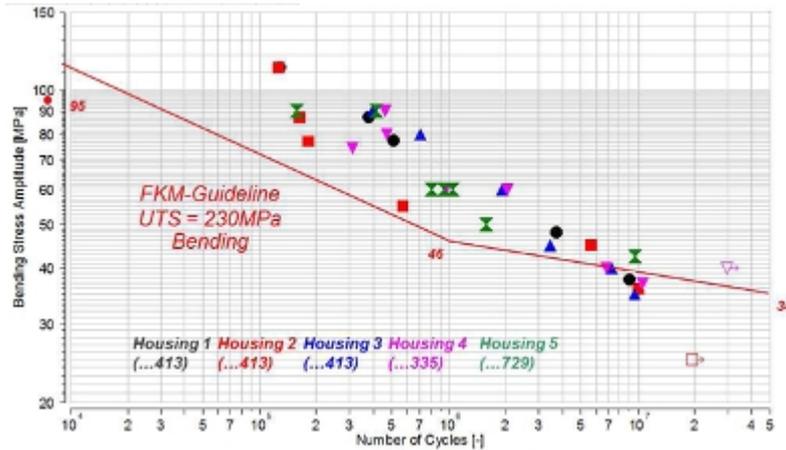


Fig11. Fatigue curve of samples

In above figure11, stress amplitude corresponding to the approximate 1×10^7 load cycles has been summarized into Table7.

Table7. Stress amplitude corresponding to 10^7 load cycles

Samples	Signs	Stress Amplitude (MPa)
Housing1	●	38.9
Housing2	■	36.4
Housing3	▲	35.0
Housing4	▼	38.5
Housing5	⊗	44.6

Conclusions

Since the casting process of aluminum alloy can not avoid porosity, shrinkage or slag completely, casting quality has a obvious effects on fatigue life, thus, it often leads to a big difference between theory life and real life for same batch casting housings. In this article, according to the crack characteristics of $AlSi_7Mg_{0.3}$ housings, the crack propagation prediction algorithm is deduced based on $AlSi_7Mg_{0.3}$ casting aluminum alloy properties, a calculation example is given based on the revised parameters, as well as the key determinants of crack propagation parameters is deduced. In order to verify the accuracy of the recommended values in this article, the dynamic stress of housing has been test on test bench, and samples fatigue test has been done. As one example, the test results show that if casting aperture diameter more than 0.5 mm, the stress amplitude of fatigue load should not be more than 38.28MPa for 1×10^7 load cycles.

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