Analysis of Three-phase Short Circuit Current by Three Elements Method

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Abstract—In this paper, we use the knowledge of the three elements method to analyze the steady-state and transient conditions of three-phase short-circuit current. The method combines actual power system conditions with the circuit subject knowledge. Compared with the traditional solution of three-phase short circuit current, it avoids solving first-order linear inhomogeneous differential equation, which is a new idea to analyze the problem of three-phase short circuit.

Keywords—three-phase; short circuit; three elements method; steady-state conditions; transient conditions

I. INTRODUCTION

Short circuit fault is a common fault in the power system. It changes the circuit structure, causing changes in power distribution, which will bring energy loss, damage to the stability of the power system, affecting the normal operation of electrical equipment. Three-phase short circuit is one of the most common short-circuit faults. It is of great significance to study the change of current in three-phase sudden short circuit to the power system.

II. ASSUMPTIONS

We assume that the power of the power is infinite, the power change caused by the external circuit is negligible, and so the voltage and frequency remain constant. Infinitely large power can be seen as a combination of multiple finite power supplies in parallel, so the internal impedance is zero. Three-phase short circuit is one of the most common short-circuit faults. It is of great significance to study the change of current in three-phase sudden short circuit to the power system.

III. SHORT CIRCUIT ANALYSIS

Since the three-phase short circuit is symmetrical, we only need to analyze one phase circuit. Here we take a phase as the research object.

According to the three factor method, the full response of the circuit consists of steady-state response and transient response.

\[ f(t) = f_o(t) + (f(0) - f_o(0)) \times e^{-\frac{t}{T}} \]  (1)

The three factor method is applied to the three-phase short circuit, we can see, three-phase short-circuit current also by the periodic components and non-periodic components.

\[ i_a(t) = i_{ae}(t) + (i_a(0) - i_{ae}(\infty)) \times e^{-\frac{t}{T}} \]  (2)

The periodic component is the case when the three-phase short-circuit current is in steady state and can be called the steady-state short-circuit current.

\[ i_{ae}(t) = \frac{U}{Z} \sin(\omega t + \alpha - \varphi) \]  (3)

\( \varphi \) is the impedance angle of the entire line after the short circuit, \( \alpha \) is the initial phase angle of the power supply. Then we analyze the transient process.

\[ i_a(0) = I_{m0} \sin(\omega t + \alpha - \varphi_0) \]  (4)

\( \varphi_0 \) is the power factor angle before short-circuiting, \( \alpha \) is the initial phase angle of the power supply.

\[ i_{ae}(0) = \frac{U}{Z} \sin(\alpha - \varphi_0) = I_m \sin(\alpha - \varphi_0) \]  (5)

Bring (3), (4) and (5) into equation (2), we get the final expression for the three-phase short circuit current

\[ i_a = I_m \sin(\omega t + \alpha - \varphi) + (I_{m0} \sin(\alpha - \varphi_0)) - I_m \sin(\alpha - \varphi) \times e^{-\frac{t}{T}} \]  (6)

Compared with the analytical methods commonly used in power system analysis, the three-element method is more concise and intuitive, avoiding the calculation of differential and integral.

IV. SUMMARY

In this paper, we use the knowledge of the three elements of the equivalent circuit method to analyze the three-phase short-circuit current steady-state and transient conditions. The power system conditions can be combined with the circuit subject knowledge to avoid solving first-order linear inhomogeneous differential equation, which is a new idea to analyze the problem of three-phase short circuit.
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REFERENCES