LVRT Strategy -based Multi-controller Switching for DFIG

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Keywords: Doubly-fed induction generation (DFIG), Low voltage ride-through (LVRT), PI controller, Four-level hysteresis current controller (FLHCC), Rotor-side converter (RSC).

Abstract. The RSC is generally controlled by using PI controller, but its narrow bandwidth and slow transient response speed limit the LVRT capability of DFIG. So, a LVRT strategy-based multi-controller switching is proposed in this paper. According to different rotor current setting value, the corresponding control strategy of RSC is implemented. That is, the PI controller is used during normal PCC voltage. However, during PCC voltage sag, the control strategy is switched to FLHCC when the rotor current reaches the first setting value, and a set of resistors is connected into the rotor circuit when the rotor current reaches the second setting value. In addition, the FLHCC implementation, the control strategy switching and the series resistance determination are also introduced in detail. Finally, the feasibility of the proposed LVRT strategy is verified by the dynamic simulation.

1 Introduction

With the continuous progress of wind power generation technology, the variable speed constant frequency (VSCF) wind power generation has become the mainstream, in which the DFIGs are most used in wind power generation system, because of its unique mode of integration into the grid. But it is highly sensitive to the grid disturbance, e.g., grid fault [1]. It will result in the voltage dip of the point of common coupling (PCC), and the result is to cause the rotor overcurrent of DFIG. If the rotor overcurrent is not controlled by taking certain measures, the RSC is extremely easy to be damaged because of over-heat effect caused by the rotor overcurrent [2]. It makes the DFIG disconnect with grid, and this will have a serious impact on the safety and stability of the grid operation. Therefore, how to improve the LVRT capability of DFIG is a subject worthy of further study. Through referring a large number of literatures on this issue, the main research findings in recent years are as follows: (1) Adding some hardware facilities, such as the rotor crowbar circuit [3], the dc-link energy absorption or storage circuit [4], and the voltage compensator or impedance network of stator side or the series resistor of rotor side [5-7]. The above methods can greatly improve the LVRT capability of DFIG, but increase the cost of DFIG system and the complexity of control system to some extent; (2) Improving on conventional control strategies, such as the improved PI control strategy and the transient stator flux weakening method [8-9], which means do not increase the hardware cost of DFIG system. But the transient control performance becomes worse during the PCC voltage dip, and as a result that greatly limits the LVRT capability of DFIG.

Compared with the conventional PI controller, the hysteresis current controller (HCC) has an excellent transient performance, such as the fast transient response speed and strong control robustness. It is often used in an active power filter of power system to reduce or even eliminate the grid harmonic components that are mainly caused by switching operation and nonlinear loads.

Combining excellent steady control performance of PI controller and quick transient response speed of HCC, an improved control strategy in this paper is proposed to improve the LVRT capability of DFIG. The main idea is that the RSC control uses the PI controller during normal PCC voltage, and during the PCC voltage dip, according to the different setting limits of rotor current, a set of resistors is connected into the rotor circuit to limit the initial rotor overcurrent and the
FLHCC is used to rapidly track the rotor command current. After the PCC voltage restores to normal, the PI controller is again used to control the RSC. Therefore, this hybrid control strategy considers the steady performance of DFIG and its transient performance as well.

2 Transient Characteristics of Rotor Voltage and Current during PCC Voltage Dip

For easy to write the dynamic voltage and flux linkage equations of DFIG, the reference directions of voltage, current and flux linkage adopt the motor convention in this paper. Thus, the dynamic equations of voltage and flux linkage vector in an arbitrary reference coordinate can be written out in [1,4,9], in which the rotor-side parameters have been converted to the stator side. These equations are given as follows:

\[
\begin{align*}
    \dot{v}_s &= R_s i_s + p\psi_s + j\omega\psi_s; \\
    \dot{v}_r &= R_i i_r + p\psi_r + j(\omega - \omega_1)\psi_r; \\
    \dot{\psi}_s &= L_s i_s + L_m i_r; \\
    \dot{\psi}_r &= L_m i_s + L_i i_r,
\end{align*}
\]

where \(v, i, \psi\) are voltage, current and flux linkage vectors, respectively; \(R, L\) are resistance and self-inductance, respectively; \(s, r, m\) subscripts denote parameters of the stator, rotor windings and excitation, respectively; \(\omega\) is angular speed of reference frame; \(p\) denotes the differential operator, which has \(p = \frac{d}{dt}\).

Selecting stator flux linkage and rotor current as state variables, and eliminating the stator current and rotor flux linkage from Eq.(1), the relationship between rotor voltage and state variables can be derived as follows:

\[
\begin{align*}
    v_r &= k_s[p + j(\omega - \omega_1)]\psi_s + [R_s + \sigma L_s[p + j(\omega - \omega_1)]]i_r = v_{r0} + [R_s + \sigma L_s[p + j(\omega - \omega_1)]]i_r
\end{align*}
\]

where \(v_{r0}\) denotes rotor open-circuit voltage generated by the stator dynamic flux linkage, which has \(v_{r0} = k_s[p + j(\omega - \omega_1)]\); \(k_s\) is defined as the coupling effect coefficient of DFIG stator winding, which has \(k_s = L_m/L_s\); \(\sigma\) is called as the leakage coefficient of DFIG rotor windings, which has \(\sigma = 1 - L_m^2/(L_s L_r)\).

2.1 Symmetrical Dip Case of PCC Voltage

If three-phase short circuit fault occurs in the grid, it will lead to symmetrical PCC voltage dip. Assuming that the voltage amplitude drops from \(V_s\) to \((1-k)V_s\), according to the conservation principle of flux linkage, and neglecting the DFIG stator winding resistance, the stator flux linkage vector in the stator reference coordinate can be derived from Eq.(1), it can be expressed as

\[
\psi_s = \psi_{sf} + \psi_{sn} = (1-k)V_s e^{j\omega_1 t} / j\omega_1 + kV_s e^{-j\tau_s} / j\omega_1
\]

where \(\psi_{sf}, \psi_{sn}\) are steady and transient components of the stator flux linkage vector, respectively; \(k\) denotes the voltage dip degree coefficient; \(\tau_s\) is the stator winding time constant, which has \(\tau_s = L_s/R_s\); \(\omega_1\) is the synchronous angular speed of the grid.

In terms of Eqs.(2) and (3), the rotor voltage vector \(v_r\) in the rotor reference coordinate can be obtained as follows:

\[
v_r = k_s V_s [s(1-k)e^{j\omega_1 t} - k(\omega_1 + 1/\tau_s)e^{-j(1-s)\omega_1 t}] + (R_s + \sigma L_s)p i_r
\]

where \(s\) is slip ratio of DFIG, which has \(s = 1 - \omega_1/\omega_1\).

Considering that the DFIG stator winding resistance \(R_s\) is very small, the influence of \(1/\tau_s\) on the rotor voltage \(v_r\) can be neglected. Therefore, the Eq.(4) can be simplified as

\[
v_r = k_s V_s [s(1-k)e^{j\omega_1 t} - (1-s)ke^{-j(1-s)\omega_1 t}] + (R_s + \sigma L_s)p i_r
\]

Before the PCC voltage drops, the rotor excitation voltage of DFIG is supplied by the RSC, it can be expressed as
\[ v_r = V_r e^{jωt} \]  \( (6) \)

where \( V_r \) is the amplitude of the rotor exciting voltage.

In order to simplify the theoretical analysis, the excitation voltage \( v_r \) remains constant before and after the PCC voltage dip. The rotor current vector can be obtained from Eqs.(5) and (6), it can be described as

\[ i_t = \left\{ \left[ V_r - k_s V_s (1 - k) \right] e^{jωt} + k_s V_s (1 - s) e^{-j(1 - s)ωt} e^{-jτ_r} \right\} / \left( R_s + sL_p \right) \]  \( (7) \)

According to the Laplace and its inverse transform, an rotor current vector expression can be derived from Eq.(7). It consists of three current components: the transient component \( i_{rdc} \) decaying by the time constant \( τ_r \) that has \( τ_r = L_s / R_s \), the periodic component \( i_{r1} \) with the frequency \( (1 - s)ω_1 \) and decaying by the time constant \( τ_s \), and the steady component with the frequency \( sω_1 \).

### 2.2 Asymmetrical Dip Case of PCC Voltage

If asymmetrical short circuit fault occurs in the grid, e.g., single-phase grounding or two-phase short circuit, it will cause the asymmetrical PCC voltage dip. According to the symmetrical component theory, the PCC voltage can be decomposed into positive, negative and zero sequence components [10], it can be expressed as

\[ v_s = \hat{V}_s e^{jωt} + \hat{V}_2 e^{-jωt} + \hat{V}_0 \]  \( (8) \)

where \( \hat{V}_s, \hat{V}_2, \hat{V}_0 \) are the positive, negative and zero sequence voltage phasors.

In the above voltage components, only the positive and negative sequence voltage components establish the air gap flux linkage of DFIG. The sum of them constitutes the steady component of air gap flux linkage, but the zero sequence voltage component creates no air gap flux linkage. In terms of the conservation principle of flux linkage and ignoring \( 1/τ_s \), the rotor open circuit voltage \( v_{r0} \) generated by the stator flux linkage \( \psi_s \) similarly can be derived, it can be expressed as

\[ v_{r0} = v_{r1} + v_{r2} + v_m = k_s \left[ \hat{V}_s e^{jωt} - (2 - s) \hat{V}_2 e^{-j(2 - s)ωt} - j(1 - s)ω_1 \hat{ψ}_{n0} e^{-j(1 - s)ωt} e^{-jτ_s} \right] \]  \( (9) \)

where \( v_{r1, r2} \) are the positive and negative sequence steady component of rotor open-circuit voltage; \( v_m \) is the transient component of rotor open-circuit voltage; \( ψ_{n0} \) is the initial value of the stator flux linkage transient component.

Typical asymmetrical grid faults have single-phase grounding fault and two-phase short circuit fault. They will lead to asymmetrical PCC voltage dip. The positive, negative and zero sequence voltage components are shown in Tab.1.

<table>
<thead>
<tr>
<th>Tab.1 Voltage sequence component</th>
</tr>
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<tbody>
<tr>
<td>fault types</td>
</tr>
<tr>
<td>phase a voltage dip</td>
</tr>
<tr>
<td>phases b and c voltage dip</td>
</tr>
</tbody>
</table>

Combining Eqs.(2), (6) and (9), the rotor current vector expression similarly can be derived, and it consists of four current components: the transient component \( i_{rdc} \) decaying by the time constant \( τ_r \), the positive sequence steady component \( i_{r1} \) with the frequency \( sω_1 \), the negative sequence steady component \( i_{r2} \) with the frequency \( (2 - s)ω_1 \), and the periodic component \( i_{rn} \) with the frequency \( (1 - s)ω_1 \) and decaying by the time constant \( τ_s \).

### 2.3 Rotor Current Dynamic Waveforms

In the previous chapter, the rotor current dynamic characteristics during the PCC voltage dip are analyzed in detail. In the following, to verify the correctness of the above theoretical analysis, the dynamic simulations of rotor current are carried out for different voltage dip types. The main DFIG parameters used in the dynamic simulation are shown in the Tab.A1 of the appendix. In this paper,
the case of the PCC voltage dip degree coefficient \( k = 1 \) is only studied. The RSC is still connected with the DFIG rotor circuit during the PCC voltage dip, and the control strategy of RSC adopts the stator flux vector orientation. For different PCC voltage dip types, the phase a rotor current dynamic waveforms are shown in Fig. 1.

![Fig.1 Phase a rotor current dynamic waveforms](image)

It can be seen from Fig.1 that, during the symmetrical voltage dip, the rotor circuit flows through very large overcurrent that exists at the moment of voltage sag and recovery. But during the asymmetrical voltage dip, a larger rotor oscillation current lasts throughout the voltage sag.

3 Proposed FLHCC

3.1 Principle of HCC

Detailed HCC principle analysis is introduced in [11] and [12]. In the stationary \( \alpha - \beta \) reference coordinate, eight discrete space voltage vectors of RSC output can be expressed as [13]

\[
\begin{align*}
\mathbf{v}_c &= 2V_\infty e^{j(\alpha - \beta)\pi/3} / 3 \\
\mathbf{v}_r &= 0
\end{align*}
\]

(10)

If the rotor resistance is neglected, the error equation of rotor current in the rotor reference coordinate can be derived from Eq. (2), it can be described as

\[
\sigma L_r p \Delta i_r = \mathbf{v}_r^* - \mathbf{v}_r
\]

(11)

where \( \Delta i_r \) is the current error that has \( \Delta i_r = i_r^* - i_r \), in which \( i_r^* \) is the rotor command current; \( \mathbf{v}_r^* \) is the rotor command voltage, which has \( \mathbf{v}_r^* = \mathbf{v}_{r0} + \sigma L_r p l_r^* \).

In terms of Eq.(11), the rotor command voltage \( \mathbf{v}_r^* \) must be accurately determined to satisfy the rotor current error\( \Delta i_r \). So, it requires that the rotor open-circuit voltage \( \mathbf{v}_{r0} \) and the rotor command current derivative \( p l_r^* \) are accurately measured, but this is difficult to achieve in actual engineering.

3.2 Proposed FLHCC

The structure of FLHCC in the stationary \( \alpha - \beta \) reference coordinate is shown in Fig.2, in which the bandwidth of two HCCs is \( \delta + \Delta \delta \).

![Fig.2 Structure of FLHCC](image)

The FLHCC proposed in this paper canceled the outer loop of the double HCC introduced in [11], in which the outer loop is used to detect the command voltage section. Furthermore, the FLHCC solved the judgment of the RSC output voltage uncertainty presented in [12]. The spatial position of the command voltage vector of FLHCC is automatically determined and updated by two HCCs. According to the status values \( d_\alpha, d_\beta \) of two HCCs, the optimum voltage vector of RSC output is...
directly obtained by querying the switch table, and the pulse width modulation (PWM) unit is eliminated. Therefore, the FLHCC has a very fast transient response tracking speed.

The switch table of FLHCC can be derived from Fig.2, and it is shown in Tab.2.

<table>
<thead>
<tr>
<th>$d_\alpha$</th>
<th>$d_\beta$</th>
<th>$d_\alpha$</th>
<th>$d_\beta$</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>$v_5$</td>
<td>1</td>
<td>$v_2$</td>
</tr>
<tr>
<td>1</td>
<td>$v_5$</td>
<td>2</td>
<td>$v_1$</td>
</tr>
<tr>
<td></td>
<td>$v_4$</td>
<td></td>
<td>$v_7$</td>
</tr>
<tr>
<td></td>
<td>$v_3$</td>
<td></td>
<td>$v_6$</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>$v_0$</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>$v_4$</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>$v_3$</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>$v_6$</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>$v_1$</td>
</tr>
</tbody>
</table>

In order to reduce the switch frequency of RSC, it is very necessary to properly introduce zero voltage vectors. It can be seen from Tab.3 that the selection logic of zero voltage vectors $v_0(v_7)$ is $S_aS_b+S_bS_c+S_cS_a$. The principle diagram of FLHCC is shown in Fig.3.

Fig.3 Principle diagram of FLHCC

4 Proposed LVRT Control Strategy

Combining the superior steady performance of PI controller and the fast transient response speed of FLHCC, a LVRT control strategy-based multi-controller switching is proposed in this paper. When the PCC voltage is normal, the PI controller is used to satisfy the steady performance of rotor current. During the PCC voltage sag, the control strategy of RSC is switched to the FLHCC that it ensures the fast transient tracking performance of rotor current. In addition, in the moment of PCC voltage fall and recovery, a set of resistors that acts as the roles of the current limiter and voltage divider over the overcurrent and overvoltage are connected into the DFIG rotor circuit. This purpose is to make sure the RSC doesn’t run out of control.

4.1 Resistance Determination of Series Resistor

It can be seen from Fig.1 that a very high rotor current is induced in the moment of PCC voltage fall and recovery. Therefore, the resistance determination basis of series resistor is that the PCC voltage symmetrically drops to zero. Namely, the PCC voltage dip degree coefficient $k = 1$. The maximum amplitude of rotor current can be derived from Eq.(7), it can be expressed as

$$i_{\text{max}} = i_{ra}(0_-) + \frac{k_s(1-s)V_r\tau}{\sigma L_s[1+(\omega_\tau)^2][1-\frac{1}{1+(\alpha_\tau)^2}]} + \frac{V_r}{\sigma L_s[1+(\alpha_\tau)^2]}$$

(12)

where $i_{ra}(0_-)$ is the phase a rotor current of the moment before the PCC voltage sags; $\tau_r$ is the rotor winding time constant with considering the series resistor, which has $\tau_r = \sigma L_s/(R_r + R_{SR})$; $\tau$ is a composite time constant, which has $\tau = \tau_s/(\tau_s - \tau_r)$.

Then, according to the safety limits of rotor current and voltage $I_{r,\text{lim}}$ and $V_{r,\text{lim}}$, and combining the time constant $\tau_r$, the resistance of series resistor can be calculated.

4.2 Controller Switching Strategy

When the PCC voltage is normal, the PI controller is used to adjust the rotor current. But during the PCC voltage dip, according to the setting rotor current $I_{r,\text{th,FLHCC}}$, the PCC voltage monitoring unit activates the FLHCC. If the rotor current continues to rise and reaches the setting rotor current
$I_{th,SR}$, a set of resistors is connected into the rotor circuit, and is removed until the rotor current is less than the setting value $I_{th,SR}$. After simulation analysis, the current limit $I_{th,FLHCC}$ is 1.25p.u. to not trigger the FLHCC under moderate voltage dip. The other one $I_{th,SR}$ is 1.5p.u. to not frequently activate the series resistor under deep voltage dip. The controller switching strategy proposed in this paper is shown in Fig.4.

**Fig.4 Controller switching strategy**

### 4.3 Dynamic Simulation Research

To validate the feasibility of the LVRT proposed in this paper, a dynamic simulation model is constructed in Simulink platform, in which the main DFIG parameters are shown in Tab.A1 of the appendix. In the process of dynamic simulation, the power and speed of DFIG are kept constant. The schematic diagram of the proposed LVRT control strategy is shown in Fig.5.

**Fig.5 Schematic diagram of LVRT control strategy**

Before the PCC voltage sags, the DFIG operates at the slip $s = -0.2$ and the power factor $\cos \phi = 0.9$. The PCC voltage drops at $t = 0.1s$, and the duration is $0.1s$. In this paper, the deep dip of PCC voltage is studied, i.e., the PCC voltage dip degree coefficient $k = 0.9$. For different PCC voltage dip types, the DFIG rotor current and the dc-link capacitor voltage are researched, and their dynamic waveforms are shown in the Fig.6. For comparative analysis, the rotor current and dc-link voltage waveforms under the conventional PI control strategy are also given in Fig.A1 of the appendix.

(a) symmetrical voltage dip

(b) phase b and c voltage dip
By comparing Fig.6 and Fig.A1, it can be seen that the LVRT strategy proposed in this paper improves the LVRT capability of DFIG to a certain extent. The detailed result comparison is shown in the Tab.3.

<table>
<thead>
<tr>
<th>fault types</th>
<th>PI strategy</th>
<th>proposed strategy</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>$I_{r_{\text{max}}}$ [p.u.]</td>
<td>$V_{d_{\text{dc}_{\text{max}}}}$ [p.u.]</td>
</tr>
<tr>
<td>symmetrical dip</td>
<td>1.68</td>
<td>1.24</td>
</tr>
<tr>
<td>phase b and c dip</td>
<td>1.67</td>
<td>1.13</td>
</tr>
<tr>
<td>phase a dip</td>
<td>1.72</td>
<td>1.10</td>
</tr>
</tbody>
</table>

5 Conclusion
The conventional PI control strategy has a poor transient control performance, to improve the LVRT ability of DFIG, a control strategy-based multi-controller switching is proposed in this paper. The proposed FLHCC further improves and optimize to the HCC introduced in [13] and [14]. In addition, according to the given rotor current and voltage limits $I_{r_{\text{lim}}}$ and $V_{r_{\text{lim}}}$, the resistance of series resistor is determined. Finally, the dynamic simulation of the proposed LVRT strategy is implemented, and the simulation results verify its feasibility. Meanwhile, LVRT capability of the proposed control strategy is compared with the conventional PI control strategy, and the results demonstrate the proposed LVRT control strategy can effectively restrain the rotor overcurrent and dc-link overvoltage and improves the LVRT capability of DFIG to a certain extent.

Acknowledgement
This work was supported in part by the Project of National Natural Science Foundation of China under Grant 46251277083.

References

Appendix

The main parameters of DFIG are as follows:

<table>
<thead>
<tr>
<th>parameters</th>
<th>value</th>
<th>parameters</th>
<th>value</th>
</tr>
</thead>
<tbody>
<tr>
<td>rated power</td>
<td>2[MW]</td>
<td>stator leakage inductance</td>
<td>0.105[p.u.]</td>
</tr>
<tr>
<td>rated stator voltage</td>
<td>690[V]</td>
<td>rotor resistance</td>
<td>0.0055[p.u.]</td>
</tr>
<tr>
<td>( \frac{r}{o} )-ratio of stator to rotor</td>
<td>0.63</td>
<td>rotor leakage inductance</td>
<td>0.1[p.u.]</td>
</tr>
<tr>
<td>rated frequency</td>
<td>50[Hz]</td>
<td>magnetizing inductance</td>
<td>3.953[p.u.]</td>
</tr>
<tr>
<td>stator resistance</td>
<td>0.005[p.u.]</td>
<td>pole pairs</td>
<td>2</td>
</tr>
</tbody>
</table>

The dynamic waveforms of \( i_{rabc} \) and \( V_{dc} \) under conventional PI control strategy

(a) symmetrical voltage dip

(b) phase b and c voltage dip

(c) phase a voltage dip

Fig.A1 Dynamic waveforms of \( i_{rabc} \) and \( V_{dc} \)