Product Architecture and Trade-in for Managing Sequential Innovation

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Keywords: Product Architecture; Trade-in; Pricing

Abstract. This paper studies the problem of whether the product design framework is modular or integrated when the durable goods are sequential innovation and manufacturers adopt the trade-in policy. It is assumed that consumer preferences for product quality are uniformly heterogeneous. Whether modular or integrated, the design architecture consists of the underlying module and the improvement module. The difference is that the modular architecture has a quality loss when upgrading the replacement module. In order to expand sales, the manufacturers used the trade-in policy to buy back the old products or modules. Through the study found that, when the second generation of products is rapidly improved, manufacturers should first stage sales of the first version product, the second stage the manufacturer to replace the first version product is the second generation of products, rather than the second version product sales. When the second version product is gradually improved, the new product launch time relatively early, manufacturers choose the integrated architecture; new product launch time is relatively late and the second version module quality performance improvement over the threshold, manufacturers choose to design modular architecture.

Introduction

Due to the resistance of products (Durable Product) the cross term service life: the service life of the product is longer than two times sales interval, thus inhibiting the new product sales, durable goods led to the time inconsistency problem Coase\textsuperscript{[1]}. Manufacturers in order to enhance sales of new products, often improve product quality, reduce prices or marketing means to stimulate sales of new products, thereby increasing profits. Among them, the Trade-in is used by many durable goods manufacturers. For example, the automotive industry, household appliances, computers, and consumer electronics in recent years. The trade-in can reduce the cost of the next purchase and stimulate the sales of the next generation.

In this paper, we will focus on the impact of the trade-in strategy on the modular product architecture, under what conditions, select the production of modular architecture products. The modular architecture are made up of two modules: one is Stable Module, and the other is Improving Module. The modular architecture of the product can be modular upgrade (Modular Upgradable) - stable module does not change, only to improve the performance of the module to upgrade and replacement, and there is a loss of quality upgrade. This modular upgrade exists in many industries, such as computer, semiconductor, IBM, Intel, and AMD machines\textsuperscript{[2]}.

When we study that the product is Rapid Sequential Innovation, product pricing, we put the trade-in’s the price discount rate, new product launch time and improve the quality of height together, then study the influence of these factors on product design and architecture. The remainder of the paper consists of the following parts: the second part, summing up the trade-in and product architecture of the literature; the third part, put forward the model assumptions and models; the fourth part, analysis model; the fifth part, numerical analysis; the sixth part, managerial insights and future research direction.
Literature Review

Reviewing two parts of r

Ethiraj et al. [13] researched three product architecture: Modular, Nearly Modular, Nonmodular. We noted literature: (1) Trade-in; (2) Product Architecture.

**Trade-in.** There are three reasons why firm uses the trade-in: first, reducing the cost which consumer supplants the old product for new product; second, closing the secondary market (shift adverse selection); last, increasing the frequency of consumer purchase.

Another point is that pricing new and old product and whether to close secondary market are researched in pricing and consumer demand model in literature. Ackere and Reyniers [3] studied two period monopoly model which the firm provides two discount pattern to consumer in the second period: one is trade-in, another is Introductory offers to consumer who buy new product. Fudenberg and Tirole [4] studied that the firm open or close the secondary market in what conditions in the two stages model that durable product’s quality continuously is improved. Rao et al. [5] found that the profit that the firm obtains in using the strategy of trade-in is more than the firm open the secondary market that adverse selection’s factor in it. Ray, Boyaci and Aras [6] compared three kinds of pricing: Uniform Price, Age-Independent Price Differentiation and Age-dependent Price Differentiation. Authors get conclusion that the firm should choose what kind of pricing in what conditions in numerical experiment. Busse and Silva-Risso [7] found that the margin profit of new car and the margin profit of trade-in have common negative correlation after they empirically study the American auto retailer’s data that from 2005 to 2007. Huang et al. [8] researched the problem that the auto manufacturer and retailer how to deal with the policy of trade-in which the government put forward.

**Product Architecture.** Baldwin and Clark [9] discussed the evolutionary path of product architecture of electronics and automotive industry for decades from integrated to modular architecture. Mikkola [10] pointed out four factors which influence performance of modular product: Components, Interfaces, Degree of Coupling and Substitutability. When product is Rapid Sequential Innovation, Kornish [11] found that market will be equilibrium, if monopoly doesn’t use Upgrade Pricing.

Ulrich [12] considered two kinds of product performance: Global Performance is that product performance is decided by all components; Local Performance is that product performance is decided by one or several components. In the three design architectures, what advantage and disadvantage of product innovation and imitation, respectively.

Krishnan and Ramachandran [14] found that product architecture has Design Inconsistency problem: the first version product’s architecture isn’t same as the second version product’s. The authors found that the problem can’t be solved by promising the second version product’s price, only be solved by setting threshold price for the first version product. Ramachandran and Krishnan [2] researched the problem that in the three situations: Proprietary Modular Upgradable Systems, Nonproprietary Modular Upgradable Systems and Proprietary Integral Systems, the speed of improving and the timing of new product introduction influence product architecture. The authors found that the speed of innovation is faster in modular architecture. Ji, Gunasekaran and Lv [15] put the factor that is the cost of service in the process of using into the model.

Ülkü et al. [16] studied the problem that consumers have the value deviation of product in aspect of product architecture in empirical method. Yin et al. [17] compared three product architecture which is modular, integrated and hybrid in Global Performance. The author found that the integrated architecture is better than modular architecture, if Global Performance is high.

Glimstedt [18] reviewed the history which Ericsson outsourced technology from 1980 to 2010 and analyzed cyclical phenomenon between Outsourcing and Re-integration in this period. Ülkü et al. [19] studied the product architecture in the supply chain. Nepal et al. [20] used Multi-objective Optimization model to research how the firm design the product architecture in the supply chain. Feng and Zhang [21] researched the Two-stage Modular Assembly System that the supplier purchased two kinds of components to integrate one module, then sold it to manufacturer. Sanchez [22] proposed several new method and problem, when it combines product architecture and
marketing.

So, there’re few papers that research problem about combine the trade-in and product architecture. This paper is the first one to study the subject.

The Problem Description and the Model

On the assumption, there is a monopoly manufacturer in the market. In the finite period of selling, the manufacturer develops two version of product: the first version of product is launched in the first period, the improved product is launched in the second period by manufacturer. The product is not disruptive innovation products, but is sequential innovation products. The quality of product can be improved by modular upgrading which a module in product can be exchange from improved module. The quality is denoted by $q_t$, where $t \in \{1,2\}$ represents the period. So, the first version product’s quality is denoted by $q_1$, the second version product’s quality is denoted by $q_2$, and $q_1 < q_2$. The product is durable product that the service life of product is longer than time interval of two sales. The consumer who bought the first version product can continue to use the first version product, when the manufacturer launches the second version product.

**Design Assumption.** The product is composed of two modules: the one is stable module, the another is improving module. There is no overlap between these two modules. The product can be function when these two modules make up the product. So, there are two product architectures: modular architecture and integrated architecture. The whole product need to be replaced to new product, when the integral architecture product upgrades. The product’s improving module need to be upgrade and stable module don’t be replaced, when the product is modular architecture. The quality of stable module is denoted by $q_{ts}$, and the quality of improving module is denoted by $q_{ti}$. Whatever the architecture product is modular or integrated architecture, their quality is same [19].

$$q_t = q_{ts} + q_{ti}$$  \hspace{1cm} (1)

So, the first version product’s quality is $q_1 = q_{1s} + q_{1i}$, the second version product’s quality is $q_2 = q_{2s} + q_{2i}$. Because product is durable product, when upgrading product is modular upgradable, the first version product’s stable module is still can be used which make up the second version product, and $0 < q_{2s} < q_{1s}$. The improving module has expression: $0 < q_{1i} < q_{2i}$. The different point is that there is loss of quality because the interface of the old stable module and new improving module isn’t smooth, when the product is modular upgradable. The loss of quality is denoted by $\alpha$, where $\alpha \in [0, 1)$ [2]. $\alpha=0$ expresses that the modular upgradable doesn’t bring about loss of quality to new modular product. In the second period, the consumer who bought the first version product upgrades the old stable module to new module through modular upgradable, then the quality of upgraded product is:

$$q_2^\alpha = (1 - \alpha)(q_{1s}^\prime + q_{2i})$$  \hspace{1cm} (2)

Where $q_{1s}^\prime$ is expressed that the surplus of stable module’s quality after the first period, and $q_2 > q_2^\alpha > q_1$. Defining $A_t$ expresses what the architecture of product is in the t period, where $A_t \in \{I, M\}$. For focusing on the product architecture, we scale production cost to zero [2],[14].

**Trade-in Decision.** The consumer who bought the first version product can use the money that the manufacturer trades in the first version product to deduct the price of the second version product. The deducted price is which consumer reality pay for the second version product. The product’s architecture is modular architecture, the first and second version product’s price are denoted by $p_{1m}$ and $p_{2m}$, respectively. The consumer who bought the first version product modularly upgrades product through trade-in, then the price of second version improving module is $p_{2i}$; When the product’s architecture is integrated architecture, the first and second version product’s price are denoted by $p_{3i}$ and $p_{2i}$, respectively. The consumer who bought the first version product replaces to the second version product through trade-inning, then the price of second version improving module is $p_{3i}$.

**Consumer’s Decisions.** Consumer is strategic consumer who can predicts the price of new product accord to the new product’s information (For example, product’s quality) which access it through all sorts of channel before launching new product. In the two periods, consumer realizes
own maximize surplus utility through comparing current surplus utility with future surplus utility. The consumer’s Willingness to Pay about quality is denoted by θ, where is uniformly distributed on [0,1]. When the quality of product is \( q_t \) and the price of product is \( p_t \), the consumer’s surplus utility is

\[
w(q_t, p_t, \theta) = q_t \theta - p_t \quad (3)
\]

When \( w > 0 \), the consumer buys the product. In every period, the discount factor of consumer and manufacturer is same \( \delta \), where \( \delta \in (0,1) \). When the quality of product is \( q_t \) and the price of product is \( p_t \), the consumer’s surplus utility is

\[
w(q_t, p_t, \theta) = q_t \theta - p_t \quad (3)
\]

When \( w > 0 \), the consumer buys the product. In every period, the discount factor of consumer and manufacturer is same \( \delta \), where \( \delta \in (0,1) \). The consumer’s surplus utility which is acquire by using the second version product through trade-in is:

\[
((1 - \delta)q_1 \theta - p_{1m}) + \delta((1 - \alpha)(q_1s + q_2i)\theta - p_{3m}) \quad (4)
\]

When the product architecture is integrated architecture, after consumer bought the first version product, the consumer’s surplus utility which is acquire by using the second version product through trade-in is:

\[
((1 - \delta)q_1 \theta - p_{1i}) + \delta(q_2 \theta - p_{3i}) \quad (5)
\]

When the product is modular architecture.

In the first period, consumer can only buy the first version product. There are three kinds of consumer to buy product: first, no matter what consumer upgrades product or not, as long as his surplus utility is more than zero and the surplus utility that obtain through using the second version product, the consumer will buy, assume,

\[
q_1 \theta - p_{1m} \geq 0 \quad (6)
\]

\[
q_1 \theta - p_{1m} \geq \delta(q_2 \theta - p_{1m}) \quad (7)
\]

Second, although the consumer obtains the surplus utility which using the first version product is less than zero, the two phase of the total surplus utility which modularly upgrades product in the second period is more than the surplus utility which doesn’t upgrade product,

\[
q_1 \theta - p_{1m} \leq 0 \quad (8)
\]

\[
((1 - \delta)q_1 \theta - p_{1m}) + \delta((1 - \alpha)(q_1s + q_2i)\theta - p_{3m}) \geq q_1 \theta - p_{1m} \quad (9)
\]

Last, although the surplus utility which consumer acquires through using the first version product is less than which consumer acquires through using the second version product, the two phase of total surplus utility which consumer acquires through using the first version product and then upgradable product is more than which consumer acquires through using the second version product,

\[
q_1 \theta - p_{1m} \leq \delta(q_2 \theta - p_{1m}) \quad (10)
\]

\[
((1 - \delta)q_1 \theta - p_{1m}) + \delta((1 - \alpha)(q_1s + q_2i)\theta - p_{3m}) \geq \delta(q_2 \theta - p_{1m}) \quad (11)
\]

In the second period, the manufacturer sells two kinds of product, one is the second version product, another is the second version improving module. The condition which consumer buy the second version product is that surplus utility isn’t less than zero,

\[
q_2 \theta - p_{1m} \geq 0 \quad (12)
\]

And isn’t less than which consumer acquires surplus utility through using the first version product,

\[
q_2 \theta - p_{1m} \leq \delta(q_2 \theta - p_{1m}) \quad (13)
\]

And isn’t less than which consumer acquires surplus utility through using the first version product and modular upgradable product,

\[
((1 - \delta)q_1 \theta - p_{1m}) + \delta((1 - \alpha)(q_1s + q_2i)\theta - p_{3m}) \leq \delta(q_2 \theta - p_{1m}) \quad (14)
\]

Another kind of consumer who buy the first version product can modularly upgrades product in the second period. There are three kinds about the part of consumer: one kind, the consumer who bought the first version product modularly upgrades product because of higher surplus utility. The conditions are Eq. 6, Eq. 7 and Eq. 9.

Second kind, in the condition, the surplus utility which acquire through using the first version product is less than zero, the total surplus utility is more than doesn’t modularly upgrade first
version product. The conditions are Eq. 8 and Eq. 9.

Last kind, the surplus utility which consumer acquires through using the second version product isn’t less than which consumer acquires surplus utility through using the first version product, and the two phase of total surplus utility which consumer acquires through using the first version product and then upgradable product is more than which consumer acquires through using the second version product. The conditions are Eq. 10 and Eq. 11.

When the product is integrated architecture. The classification of consumer is the similar as the modular architecture’s consumer. So, they aren’t shown here.

Model Analysis

To consider the manufacturer’s profit maximization when the manufacturer determines the product’s architecture and price. When the product is modular architecture, then the manufacturer’s second period optimization problem is given by Eq. 15, where the demands $D_2$ and $D_{2T}$ are denoted by the second version product of demand and the trade-in of quantity.

$$\Pi_{2m} = \max_{p_{3m}} p_{1m}D_2 + p_{3m}D_{2T}$$
s.t. $f_i(p_{3m}, p_{3m}) \geq 0$ 

(i = 1,2,..., m)

In the first period, the firm sets its first-period price $p_1$ to maximize the net present value of its revenue stream from the two periods, where $D_1$ is denoted by the first version product’s demand.

$$\Pi_m = \max_{p_{1m}} p_{1m}D_2 + \delta \Pi_{2m}$$
s.t. $f_j(p_{1m}, p_{3m}) \geq 0$ 

(i = 1,2,..., n)

When the product is integrated architecture, the manufacturer’s second period profit function is

$$\Pi_{2i} = \max_{p_{3i}} p_{1i}D_2 + p_{3i}D_{2T}$$

s.t. $f_i(p_{3i}, p_{3i}) \geq 0$ 

(i = 1,2,..., m)

the manufacturer’s whole profit function is

$$\Pi_i = \max_{p_{1i}} p_{1i}D_2 + \delta \Pi_{2i}$$

s.t. $f_j(p_{1i}, p_{3i}) \geq 0$ 

(i = 1,2,..., n)

There’re two kinds of improvement module: rapid improvement $\delta q_2 \geq q_1$ and gradual improvement $\delta q_2 \leq q_1$. Every kind has two kinds: the discount quality of the second version product isn’t lower than the discount quality of modular upgraded product and the discount quality of the second version product isn’t higher than the discount quality of modular upgraded product. We’ll find the optimal solution of every situation, then analyze the property of price function and demand function, at last choose the kind of product architecture in which kind of situations. We’ll use the Karush-Kuhn-Tucker Condition to solve the problem.

When the discount quality of the second version product isn’t lower than the discount quality of modular upgraded product, there’s only rapid improvement.

**Proposition 1**. When $\delta q_2 \geq q_1$, there aren’t optimal solution no matter what the product is modular or integrated architecture.

**Proposition 2**. When the product is modular architecture, $\delta B \leq A$, $C < 0$, $\eta_1 = \eta_2 = \eta_3 = \eta_4 = 0$, the optimal price of the manufacturer is

$$p_{1m}^1 = \frac{-2B\delta}{-4C\delta + B}$$

$$p_{3m}^1 = \frac{-C(4B\delta^2 - 2B\delta - 4AC\delta + B)}{2\delta(-4C\delta + B)}$$

Among $\eta_j$, $j \in \{1,2,3,4\}$ is Lagrange multiplier, $A = q_1$, $B = q_2$, $C = \delta q_2 - (1 - \delta)q_1 - \delta(1 - \alpha)(q_{1s} + q_{2s})$, $D = (1 - \alpha)(q_{1s} + q_{2s})$.

**Proposition 3**. When the product is modular architecture, $\delta B \leq A$, $C < 0$, $\eta_1 = \eta_2 = \eta_3 = 0$, $\eta_4 \geq 0$ the optimal price of the manufacturer is

$$p_{1m}^* = \frac{BC(-B\delta + A + B + C)}{2(2BC\delta^2 + A^2 - 2AB + 2AC + B^2 - 2BC + C^2)}$$

$$p_{3m}^* = \frac{-p_{1m}^*(-B\delta + A + C)}{B\delta}$$

Among $\eta_j$, $j \in \{1,2,3,4\}$ is Lagrange multiplier.

**Proposition 4**. When the product is integrated architecture, $\delta B \leq A$, $C < 0$, $\eta_1 = \eta_2 = \eta_3 = 0$, $\eta_4 \geq 0$ the optimal price of the manufacturer is

$$p_{1i}^1 = \frac{-2B\delta}{-4C\delta + B}$$

$$p_{3i}^1 = \frac{-C(4B\delta^2 - 2B\delta - 4AC\delta + B)}{2\delta(-4C\delta + B)}$$

Among $\eta_j$, $j \in \{1,2,3,4\}$ is Lagrange multiplier.
\[ \eta_4 \geq 0 \] the optimal price of the manufacturer is
\[ p_{1i}^* = \frac{AB(\delta^2 - B\delta - B)(\delta - 1)}{2(A^2\delta^2 - A B\delta^2 - A B\delta + B^2)}, \]
\[ p_{3i}^* = \frac{p_{1m}(B - A)}{B}, \]
Among \( \eta_j, j \in \{1,2,3,4\} \) is Lagrange multiplier.

**Numerical Research**

For researching the impact which is the introduction time(\( \delta \)) of the second version product and the quality of the second version improving module influence the manufacturer’s choice of product architecture, we’ll analyze these parameters’ sensibility against manufacture’s profit. The vertical axis is the manufacturer’s profit and horizontal axis is the parameter in all of following figures.

Basis on the previous of analysis, when \( \delta q_2 > q_1 \), there aren’t optimal solution no matter what the product is modular or integrated architecture. We’ll analyze the situation when \( \delta q_2 \leq q_1 \) in numerical experiment. There’re two parts in this: when the second version product launch time is earlier (\( \delta = 0.8 \)), the manufacturer should choose which kind of architecture; when the second version product launch time is later (\( \delta = 0.2 \)), the manufacturer should choose which kind of architecture again.

When the second version product launch time is earlier (\( \delta = 0.8 \)), the manufacturer should choose the integrated architecture. Because the second version product is gradual improvement and the launch time is earlier, so that the quality improvement of improvement module isn’t high. If the product is modular architecture, the quality of product will be lost during upgrades, and the high-end consumer buys the first version product then modular upgrade the product, these will bring the results which consumer hasn’t enough utility. So, the manufacturer only chooses the integrated architecture.

When the second version product launch time is later (\( \delta = 0.2 \)), these’re the eligible conditions: the modular architecture’s profit \( \Pi_{12} \) (\( a \in [0.1,0.3], \ q_{2i} \in [3,3.6] \)), \( \Pi_{23} \) (\( a \in [0.1,0.5], \ q_{2i} \in [0.8,3.2] \)) and the integrated architecture’s profit \( \Pi_{32} \) (\( q_{2i} \in [0.3,2.3] \)). We’ll divide the \( q_{2i} \in [0.3,3.6] \) into three sub areas: \( [0.3,0.8] \cup [0.8,2.3] \cup [2.3,3.6] \), then find the optimal product architecture in these areas.

When \( q_{2i} \in [0.3,0.8] \), the manufacturer should choose the integrated architecture;
When \( q_{2i} \in [2.3,3.6] \), the manufacturer should choose the modular architecture;
When \( q_{2i} \in [0.8,2.3] \) and \( a=0.1 \), we choose \( \Pi_{23} \) and \( \Pi_{32} \) to compare them. It be shown the figure 1.

**Observation 1.** When \( \delta=0.2 \) and \( \delta q_2 \leq q_1 \), if the quality of the second version improvement module is low the threshold, the manufacturer should choose the integrated architecture; if the quality of the second version improvement module is high the threshold, the manufacturer should choose the modular architecture.

When the product is gradual improvement and the quality of the second version improvement module is lower than threshold, the modular architecture of the product due to upgrade quality loss, so if the quality improvement is not high enough, it can not be offset by higher prices, which will make the purchase of the first version product and upgrade product to consumers to reduce their number, to buy second version product. The integrated architecture of the product after the change it can give consumers more utility (because it doesn’t have a modular upgrade, there will be no loss in quality), so when the quality improvement of second version module performance is less than a threshold, the profits of the integration architecture is larger than modular architecture’s profit.
If the quality improvement of second version improvement module to further improve the performance over the threshold, in the integrated architecture, as to improve the quality of price increases will lead to some high-end consumers to buy the second stage of the second version product, because the purchase of second version product can get more utility. The modular architecture of the product due to the modular upgrade on the quality of the loss, so when the quality improvement of second version improvement module to further improve the performance when there is a manufacturer to further improve the modular product sales space. Therefore, when the quality of the second version improvement module is higher than the threshold value, the manufacturer should choose the modular architecture.

Managerial Insights and Future Research Direction

In this paper, we study the choice of product architecture under the policy of trade-in in the series of innovative products in durable goods. Because of the technological innovation speed, durable goods manufacturers in response to consumer demand changes rapidly, at the same time to consolidate the existing market, to design a modular architecture and more products (such as mobile phone and home appliances). The modular product which has the advantages of low cost of the update (basic module can continue to use, only need to upgrade the performance improvement, but the upgrade module) after product quality loss; integrated product is just the opposite. In this paper, we assume that the consumer's quality preference is uniform diversity, whether it is the integration architecture, modular architecture is composed of two modules: the module of basic module and improvement module. The two difference is that the architecture design of the modular architecture, improvement module of product replacement a better performance in the module based on the original, there will be a quality upgrade after the loss (compared to the integrated design of products); integration products are not modular upgrade. In order to promote the sales of new products, manufacturers use trade-in policy from consumers repurchase generation improvement module or products, and give consumers certain subsidies to offset the purchase of new modules or the price of the product. The manufacturer does not generate costs in the manufacturing module, and the price of the first and second version is the same. As a result, the quality of the upgrade, the timing of the new product, the price and quality of the product have a bearing on the design of the product.

What is different from Ramachandran [2] is that through our research found that when the second version product is rapidly improved, the manufacturer should first stage sales of the first version product, the second stage TM to replace the first version product is the second version product, rather than the second version product sales. When the second version product is gradually improved, the new product launch time relatively early, the manufacturer chooses the integrated architecture; new product launch time is relatively late and the second version improvement module’s quality is over the threshold, the manufacturer chooses to design modular architecture.

This article focuses on the product sales process, the product recycling process is not considered in this article. When the consumer products in the trade, because the consumer is the product of the user, so the level of understanding of the use of the product quality after the manufacturer should be higher than the original, the manufacturer how to develop the recycling price and how to determine the recovery and recycling of the quality threshold, this is the recovery of the moral hazard problem
in the process of product. What recycling channels should be chosen for the product to be recycled, whether the manufacturer is directly recycled or recycled through the retailer, does the different recycling channels affect the product design architecture? Also, this article assumes that the price of the first and second version product are the same. What would happen if the manufacturer adopted the dynamic pricing strategy? These issues will be the direction of future research.

Acknowledgments

This research is supported in part by the National Natural Science Foundation of China (No. 71671085)

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