

Design and Simulation Analysis of Modal and Harmonic Response of Chained Deep-ploughing Device

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Abstract: In light of complex topography in southern mountain area, a small chained deep-ploughing machine with crawler was developed. Its key part was a chained deep-ploughing device, whose service life could be impacted by vibration frequency as well as strength and rigidity of the material used. This paper presented the design of the chained deep-ploughing device and related kinematics and mechanical analyses. With the help of finite element method and Ansys Workbench, simulation analysis of modal and harmonic response was conducted. Modal and vibration mode of the first six orders concluded verified the fact that the deep ploughing device was able to avoid resonance and meet requirements for deep ploughing. This also provided basis for other dynamic response.

Introduction

Mini tillers were widely used in southern mountain area for many years, in which situation, harden plow pan was formed under shallow plough layer, impacting the deep growth of root system and making it difficult for water and fertilizer to penetrate, among others[1,2]. In recent years, different kinds of improved small deep-ploughing machines have been developed, where two of them are chained deep-ploughing machine, whose intellectual property rights are held by Southwest University (2014) and Zunyi Branch of Guizhou Tobacco Company (2014), respectively. The one held by Southwest University is a small walking deep-ploughing machine with crawler: with help of link span, chained deep-ploughing parts are linked to crawler machinery and fixed to a rectangle frame formed by two crawler units, engine and rack of crawler machinery[3]. The other one is a deep-ploughing machine: rotary cutter is linked to both chains and the largest ploughing depth is determined by the distance and dip angle between main chain wheel and the driven chain wheel[4]. The problem that rests in both of these two chained deep-ploughing machines is that they have complexly structured chained deep-ploughing devices. However, the chained deep-ploughing device applicable for small deep-ploughing machine designed here is simply structured. According to kinematics and mechanical analyses and simulation analysis of modal and harmonic response, the device designed here was able to avoid resonance and meet requirements for deep ploughing[5].

Structure and Performance Parameter of Chained Deep-ploughing Device

Basic Structure of Chained Deep-ploughing Device

Structure of chained deep-ploughing device is indicated in Figure 1. It consists of 1 driving chain wheel, 2 chain, 3 chain cutter, 4 driven chain wheel, 5 work arm, among others. It is an agricultural device that ploughs with multiple chain cutters and is also the core device for small chained deep-ploughing machine with crawler. The engine controls chained deep-ploughing device through gearbox and then gear case and hydraulic control system. When wheels walk towards to the same direction as the chain transmission shaft, the deep ploughing function of this device is on; otherwise, ditching function is on.

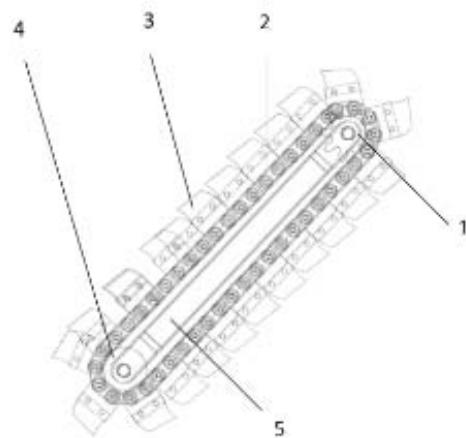


Fig. 1 Structure of Chained Deep-ploughing Device

Parameters Calculation of Chained Deep-ploughing Device

When chained deep-ploughing device performs deep ploughing lengthwise, due to dynamic loading acted on chain cutter and abrasion caused by cutting soil, minor waggle will inevitably happen to chain cutter and impacts the speed. In general, in order to guarantee the quality of operation of chained deep-ploughing device, the minor waggle mentioned herein shall be reduced as far as possible. As a result, linear velocity of chain cutter needs to be limited when it is designed: generally, for mineral soil, the speed V_c is 1.0-2.0m/s and for peat soil, the speed V_c is 3.0-4.0m/s[6].

Based on kinematics and related geometric principles (see Figure 2), the following equation can be developed with the help of relevant literature[7].

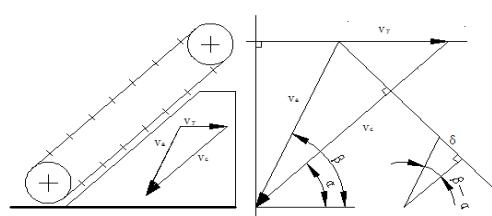


Fig. 2 Kinematics Analysis of Chained Deep-ploughing Device

Horizontal velocity of working parts of chain cutter is determined by the productivity of the machine and the sectional area of the cutting groove.

For equation:

$$V_y = \frac{\eta}{3.6 \times 10^3 b_{gd} Z_c} \quad (\text{m/s}) \quad (1-1)$$

Where η -theoretical productivity (m^3/h);

b_{gd} -ploughing width (m);

Z_c -ploughing depth (m).

Dip angle from the level was set as 45° at design time.

The absolute velocity of chain cutter V_a :

$$V_a = \sqrt{V_c^2 + V_y^2 - 2V_c V_y \cos \alpha} \quad (\text{m/s}) \quad (1-2)$$

Where V_c -velocity of chain cutter (m/s);

V_y -operation velocity of working parts of the chain cutter (m/s);

α -dip angle of the working chain cutter from the level.

The dip angle β of absolute motion velocity vector V_a can be obtained from equation (1-3):

$$\tan \beta = \frac{V_c \sin \alpha}{V_c \cos \alpha - V_y} \quad (1-3)$$

According to equation (1-3), β equals 42° .

Generally, height of chain cutter h_c is 0.1-0.15m. However, if the height increases, the loading of the working parts rises. As a result, the height of chain cutter h_c in this paper is 0.1m.

Preliminary computation can be conducted for cutting thickness δ based on chain cutter pitch L_c :

$$\delta = L_c \sin(\beta - \alpha) \quad (1-4)$$

And the following equation can be used instead under rational soil cutting condition:

$$\delta \approx \frac{b_c}{10 \sim 15} \quad (\text{m}) \quad (1-5)$$

In this paper, chain cutter pitch L_c is 50.8mm and based on equation (1-4), cutting thickness of chain cutter δ is 5.83mm. According to equation (1-5), cutter width b_c is 87.6mm.

Delivery capacity shall be verified for the preselected scraper height and pitch. Choose proper chain cutter height h_c and cutter width b_c .

h_c and b_c shall meet the following requirements:

$$\eta \leq \eta' \frac{1}{k_d} \lambda \quad (1-6)$$

Where η - the given productivity (m^3/h)

η' - productivity of chain cutter-type working parts on basis of discharge capacity (m^3/h)

k_d - loose coefficient of soil

λ - scattering coefficient related to kinematic velocity of chain. See the following table for more details:

V_c (m/s)	0.1	1	1.5	2
λ	0.97	0.92	0.85	0.75

Calculate the productivity η' of chain cutter-type working parts under the following conditions:

$$\alpha \leq \varphi + \arctg \frac{h_c}{L_c}$$

If

Where φ -natural angle of repose of loos soil

h_c - height of chain cutter (m)

L_c - blade pitch (m)

$$\eta' = 3600 b_c h_c V_c [1 - \frac{L_c}{2h_c} \tg(\alpha - \beta)] \quad (\text{m}^3/\text{h}) \quad (1-7)$$

$$\alpha \leq \varphi + \arctg \frac{h_c}{L_c}$$

If $\alpha \leq \varphi$, soil transferred is shaped as triangle

$$\eta' = 3600 b_c h_c V_c \frac{h_c \tg(\alpha - \varphi)}{2L_c} \quad (\text{m}^3/\text{h}) \quad (1-8)$$

If $\alpha \leq \varphi$, chain cutter-type working parts have the maximum productivity:

$$\eta' = 3600 b_c h_c V_c \quad (\text{m}^3/\text{h}) \quad (1-9)$$

Natural angle of repose of loos soil is the maximum dip angle for avoiding slop failure under natural soil conditions. Under actual condition, tester of angle of repose may be used. In light of the actual operation of deep-ploughing machine, the angle of repose was set at 30° . The cross-reference table given below indicates the most commonly used angle of repose for soil[8].

$$\varphi + \arctg \frac{h_c}{L_c} = 30 + \arctg \frac{100}{50.8} \approx 93^\circ$$

In this paper, since $\alpha_s = 45^\circ$, and

$$\alpha_s \leq \varphi + \arctg \frac{h_c}{L_c}$$

i.e. and the rated productivity of chain cutter η' shall be calculated as per equation (1-7).

$$\eta \leq \eta' \frac{1}{k_d} \lambda$$

After computation, equation (1-7) meets the relation

Table 1 Natural angle of repose of soil

Soil type	Degree(s) under wet condition	Degree(s) under humid condition	Degree(s) under dry condition
Coarse sand	27	32	30
Medium sand	25	35	28
Gravel	35	40	40
Scree	35	40	40
Silver sand	20	30	25
Gault	15	35	45
Humus	25	35	45
Light clay	30	40	50
Light loam	20	30	40
Fill soil	27	45	35

Mechanical Analysis of Chained Deep-ploughing Device—Calculation of Cutting Resistance for Chain Cutter

When small chained deep-ploughing machine with crawler is in operation, soil scraps produced by each chain cutter have different shape, which are the basis for calculating ploughing resistance and productivity. The shape of soil scraps are related to the structure of chain cutter of ditcher. For B-type chain cutter, the resistance produced by cutting soil can be computed as follows:

$$F_t' = 9.8I_{tu} \delta^{1.35} (1 + 0.1\delta_c) \left(1 - \frac{90 - \psi}{180}\right) e \quad (N) \quad (1-10)$$

Where I_{tu} - impact value of firmness concluded by the former Soviet Union Road Science Institute (see Table 2)

δ - cutting thickness (mm);

δ_c - thickness of blade (mm);

ψ - cutting angle of blade ($^{\circ}$);

e- coefficient of edge angle γ (see Table 3).

 Table 2 I_{tu} Value

Item	Boggy and peat soil	Sandy soil	Sandy loam	Loam	Heavy loam	Clay	Heavy clay
I_{tu}	1~5	1~4	3~12	5~10	9~18	14~19	18~24

Table 3 γ and e values

γ	$15^\circ - 50^\circ$	60°	90°	120°	180°
e	0.81	0.83	0.90	0.95	1.0

The total resistance for ditching F'_k is calculated based on total cutting force acted on soil simultaneously. The force acted on the chain by F'_k :

$$F'_k = F'_t Z'_t \quad (\text{N}) \quad (1-11)$$

Where F'_t -resistance produced from cutting soil (N);

Z'_t -number of blades acting on soil.

Based on equation (1-10), resistance produced from cutting soil to each chain cutter $F'_t = 341\text{N}$ ($Z'_t = 4$) and the total resistance caused by cutting to the deep-ploughing machine $F'_k = 1364\text{N}$.

Finite Element Model of Chained Deep-ploughing Device

Modal analysis is mainly used for determining the inherent frequency and mode of vibration of the structure[9]. As in small chained deep-ploughing machine with crawler' case, it's the movement of chain wheel that drives the movement of chain of chain cutter. Vibration produced by chain cutter by entering and cutting soil and meshing of chain link and sprocket cause bumpy motion and regular vibration to chain drive. Therefore, for the purpose of keeping chained deep-ploughing device away from the vibrational frequency of deep-ploughing machine, and also for avoiding resonance happening to the structure and improving the structural stability, launching modal analysis and finding out the inherent frequency mentioned herein are very necessary[10].

Modal analysis solving in Ansys Workbench was completed by Pre-Stress Modal within Custom Systems module. For the purpose of modal analysis, Modal Analysis System would be added to the Project Flow in the first place and materials, models and other data were shared with static analysis. When modal analysis was conducted for the overall structure of small chained deep-ploughing machine with crawler in this paper, axle of drive sprocket was fixed on the rack of chained deep-ploughing machine in light of the actual situation and as a result, fixed constraint needed to be added to the work arm near axle of drive sprocket to limit constraints of all directions and add constraint for force. See Figure 3 for more details.

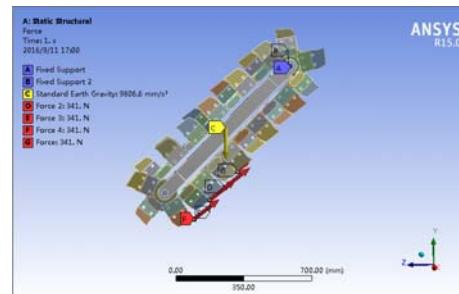


Figure 3 Geometric Model of Modal and Harmonic Response Analysis

Result and Discussion

Finite Element Model of Chained Deep-ploughing Device

Any structure may have many orders for their inherent frequency. However, for large mechanical structure, it is generally low-order inherent frequency that has important impact on the structure and high-order mode has little impact on most structures[11]. This paper analyzes soil cutting process of chained deep-ploughing machine and discusses inherent frequencies of the first six orders.

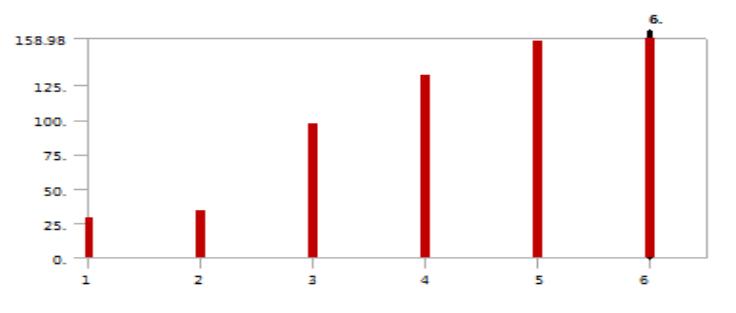
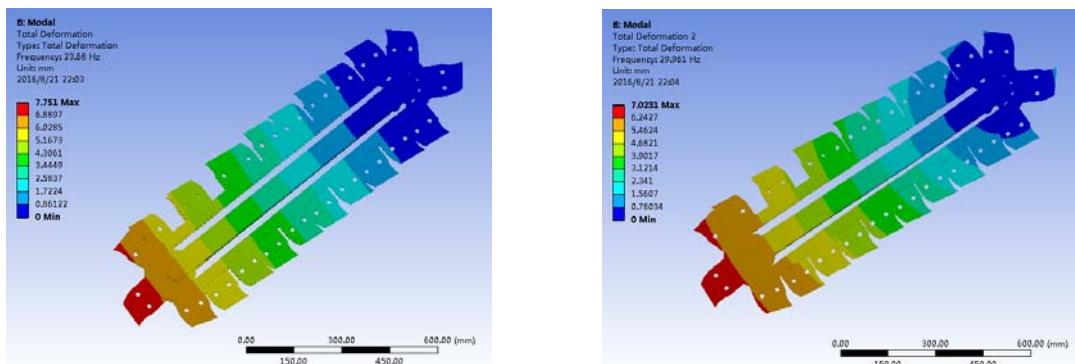
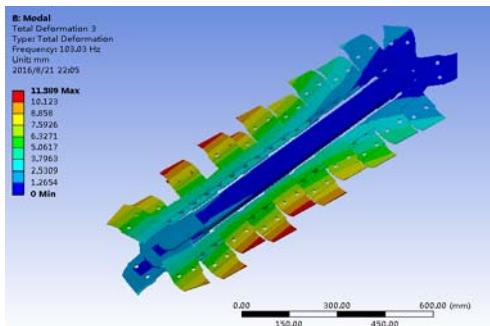


Figure 4 Analysis of inherent frequency of the first six-order modal of deep-ploughing device
Modal frequencies of the first six orders of deep-ploughing machine provided in Figure 4 are 28.578Hz, 33.9271Hz, 96.684Hz, 132.41Hz, 156.83Hz and 158.98Hz.

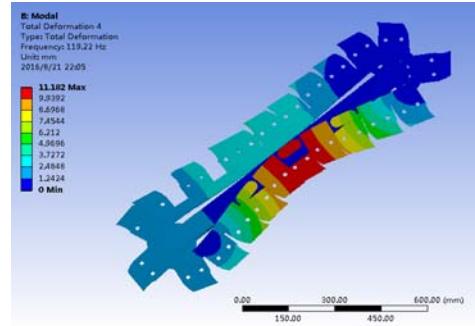


(a) Plot of the first order mode of vibration of chained deep-ploughing machine

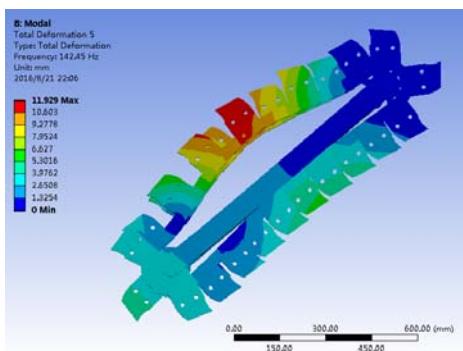
(b) Plot of the second order mode of vibration of chained deep-ploughing machine



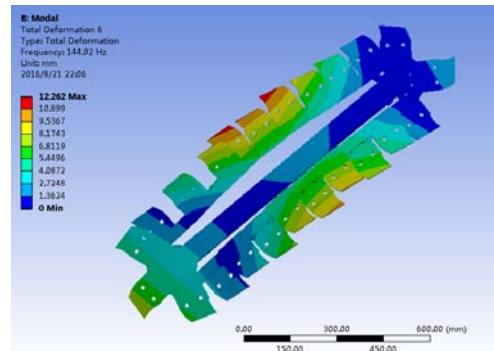
(c) Plot of the third order mode of vibration of chained deep-ploughing machine



(d) Plot of the fourth order mode of vibration of chained deep-ploughing machine



(e) Plot of the fifth order mode of vibration of chained deep-ploughing machine



(f) Plot of the sixth order mode of vibration of chained deep-ploughing machine

Fig. 5 Plots of inherent frequency of each order mode

After modal analysis of chained seep-ploughing device of small chained deep-ploughing machine with crawler, plots of inherent frequencies of the first six orders for chained deep-ploughing machine are obtained. See Figure 5 for more details.

Modes of vibration of chained deep-ploughing device are now presented as follows:

The first order mode of vibration of chained deep-ploughing device is indicated in Figure (5a). Drive sprocket is taken as the center of chained deep-ploughing device in this case with the end of work arm as the maximum swing. The maximum deformation is found at the chain cutter at the end of driven sprocket.

The second order mode of vibration of chained deep-ploughing device is indicated in Figure (5b). In this case, the maximum swing is found at the end of work arm of chained deep-ploughing device. Same as the first order mode of vibration, the maximum deformation is found at the chain cutter at the end of driven sprocket.

The third order mode of vibration of chained deep-ploughing device is indicated in Figure (5c). In this case, the mode of vibration is the axial wobble of the whole chained deep-ploughing device. The maximum deformation is found in between the up and down chain links in the middle of chain drive.

The fourth order mode of vibration of chained deep-ploughing device is indicated in Figure (5d). The mode of vibration is the transverse vibration of the lower chain. The maximum deformation is found in the middle of the lower chain of chain drive.

The fifth order mode of vibration of chained deep-ploughing device is indicated in Figure (5e).

The mode of vibration is the transverse vibration of the upper chain. The maximum deformation is found in the middle of the upper chain of chain drive.

The sixth order mode of vibration of chained deep-ploughing device is indicated in Figure (5f). The mode of vibration is the axial wobble of the whole chained deep-ploughing device. The maximum deformation is found in between the up and down chain links in the middle of chain drive, mainly at the upper part.

The design requirements for chained deep-ploughing device of small chained deep-ploughing machine with crawler are that modal frequency of chained deep-ploughing device shall be kept away from the excitation frequency of load. Generally, lots of excitation vibration sources may cause vibration to chained deep-ploughing device, where the main sources are unbalanced wheels of walking tractor and unbalanced load exerted on chained deep-ploughing device, among others.

According to relevant research data, excitation frequency caused by unbalanced wheel of walking tractor is very low, most of them lower than 10Hz. Therefore, the impact imposed by it is overlooked in this paper. Vibration caused by the unbalanced load carried by chain cutter of chained deep-ploughing device is the main excitation source. As a result, the inherent frequency of chained deep-ploughing device designed should stay away from excitation frequency in order to achieve good dynamic behavior for chained deep-ploughing device.

Harmonic Response Analysis

The inherent modal frequency and mode of vibration of the first six orders of chained deep-ploughing device were concluded through modal analysis of finite element model of chained deep-ploughing device of small chained deep-ploughing machined with crawler. When deep-ploughing machine is in operation, due to the meshing of roller chain and chain wheel caused by chain transmission, impact effect can be generated regularly. When meshing frequency is almost the same as the inherent frequency of chained deep-ploughing device, resonance happens[12]. And for this reason, when kinetic study is conducted for chained deep-ploughing device of deep-ploughing machine, the all-sided kinetic characteristics of chained deep-ploughing device cannot be achieved only through modal analysis and the harmonic response of chained deep-ploughing device shall also be studied. The relationship between dynamic response and frequency of chained deep-ploughing device will be analyzed to find out if chained deep-ploughing device of deep-ploughing machine can avoid resonance when it's in operation.

Computation of Working Frequency

Periodical impact force, i.e. the excitation force acted on chain drive, is determined by amplitude, phase position and forced vibration frequency. Namely, when chained deep-ploughing machine is in operation, the chain cutter will generate impact effect and its frequency is:

$$f = \frac{V_c}{P} = \frac{1500}{50 \cdot 8} = 29.5 \text{ Hz} \quad (2-1)$$

Where V_c - linear velocity of chain (mm/s); P -pitch of links chains (mm).

Process Before Harmonic Response Analysis

Harmonic response analysis was conducted by Harmonic Response within Mechanical module of ANSYS Workbench. For the purpose of harmonic response analysis, Harmonic Response Analysis System would be added to the Project Flow in the first place and materials, models and modal analysis results were shared with modal analysis.

Forcing frequency range of structural system must be designated when harmonic response analysis is conducted. In this paper, according to modal analysis results, frequencies of chained deep-ploughing device of the first six orders were lower than 160Hz and therefore, the forcing frequency range shall be designated at 0-160 Hz when harmonic response was conducted and set 40 solutions.

Results of Harmonic Response Analysis

Mode superposition method was used for model solving after set based on parameters mentioned above. This way, harmonic response analysis results of chained deep-ploughing device of chained deep-ploughing machine were reached.

Figure 6 and Figure 7 show the stress-frequency response curve of chained deep-ploughing device and deformation-frequency curve of chained deep-ploughing device, respectively. Big stress responses and deformation responses can be seen when the frequencies are 30Hz, 95Hz, 135Hz and 156Hz, which are close to the inherent frequencies of chained deep-ploughing device. Given the fact that 30Hz, 95Hz, 135Hz and 156Hz are close to the inherent frequencies of the first, the second, the third, the fourth and the fifth orders, it agrees with the results of modal analysis.

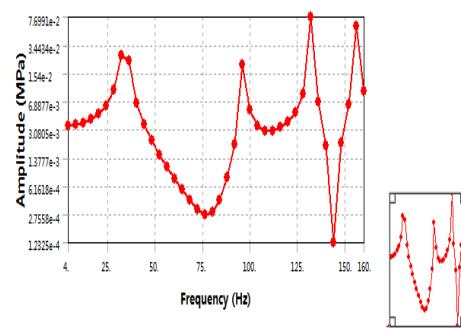


Fig.6 Stress-frequency Curve of Deep-ploughing Device

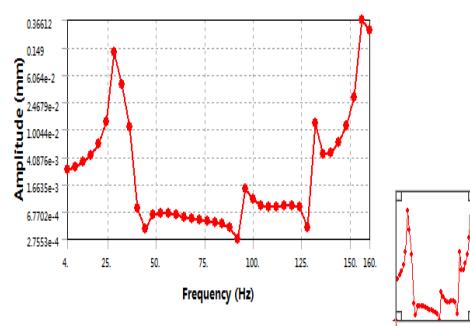


Fig.7 Deformation-frequency Response of Deep-ploughing Device

Note that antiresonance point of chained deep-ploughing device appeared at around 140Hz. This was antiresonance caused by superposition of excitation force and inherent frequency of chained deep-ploughing device. When the device was at this frequency, the resonance effect of chained deep-ploughing device could be avoided.

The inherent frequency of chained deep-ploughing device used in this paper was 29.5Hz and based on analysis above, it could be concluded that the chained deep-ploughing device avoided the inherent frequency at this point, which prevented the appearance of resonance.

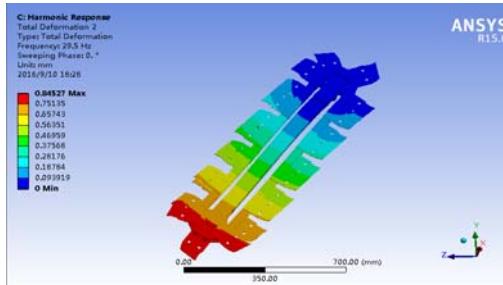


Fig.8 Deformation Analysis under Working Frequency

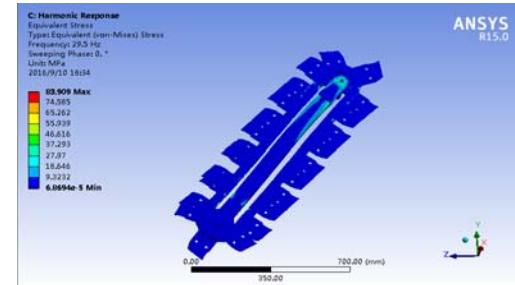


Fig. 9 Stress Analysis under Working Frequency

Figure 8 shows the deformation analysis of chained deep-ploughing device at frequency of 29.5Hz. According to Figure 8, the maximum deformation for the working frequency of chained deep-ploughing device was 0.84527mm, which had no impact on deep ploughing. Figure 9 shows the stress analysis of chained deep-ploughing device at frequency of 29.5Hz. According to Figure 9, the maximum stress for the working frequency of chained deep-ploughing device was 83.909Mpa.

Theoretical Analysis of Strength and Stiffness of Deep-ploughing Device

Intensity examination of deep-ploughing device: the maximum stress of chained deep-ploughing device at working frequency was 83.909Mpa. The main materials used for the deep-ploughing device of deep-ploughing machine were 45 steel and 45Mn and their yield limit were 355MPa and 375Mpa, respectively. According to analysis results, the maximum stress for the working frequency of chained deep-ploughing device was far lower than the yield limit of materials used. Therefore, the deep-ploughing device designed in this paper agreed with strength requirements.

Stiffness examination of deep-ploughing device: the whole deep-ploughing device could be taken as a cantilever beam structure when displacement analysis was conducted. Given that the total length of the beam L=920mm and based on the following equation[13]:

$$y = \left| \frac{FL^3}{3EI} \right| \quad (2-2)$$

$$F=P/V \quad (2-3)$$

y- deflection (mm);

E- elasticity modulus of material E=210GPa;

$$I = \frac{hb^3}{12}$$

I- inertia moment of rectangular steel (h and b are the height and width of the rectangular steel);

P- engine power (w);

V- walking velocity of deep-ploughing machine (m/s);

F-Traction of deep-ploughing machine, i.e. force acted on the cantilever beam (N).

Based on equation (3-2) and (3-3), deflections y are 0.8472mm and 0.0009L, which are close to the maximum deformation of chained deep-ploughing device at working frequency and verified the reliability of simulation. Given the allowable deflection of cantilever beam [y]=0.002L, it can be

concluded that the deflection of deep-ploughing device is lower than the allowable one. In another word, deep-ploughing device meets stiffness requirements.

Given that the excitation frequency of chained deep-ploughing device designed avoided its own inherent frequency, resonance of the structure could be kept away effectively. No major stress and deformation might appear at the working frequency of chained deep-ploughing device and the strength and stiffness of the structure had enough allowance, which met requirements for deep ploughing.

Conclusions

Based on analyses above, the following conclusions can be reached:

(1)Based on the modal analysis of chained deep-ploughing device of small chained deep-ploughing machine with crawler, inherent frequencies of the first six orders were obtained, which were helpful for the deep-ploughing device to achieve good dynamic behavior.

(2)Based on harmonic response analysis, the stress-frequency and deformation-frequency curves of chained deep-ploughing device were obtained and the frequencies that had big impact on chained deep-ploughing device were found out, which were helpful for deep-ploughing machine to avoid these frequencies and provided powerful basis for the improvement and optimization of chained deep-ploughing device. It was at working frequency of 29.5Hz that the chained deep-ploughing device of small chained deep-ploughing machine with crawler avoided resonance. Also at this working frequency, the maximum stress and the deformation of the device was 83.909Mpa and 0.84527mm respectively, meeting requirements for deep ploughing.

(3)This paper provided new thoughts for the development of small chained deep-ploughing machine and basis for seeking for sensitive position and structure optimization for chained deep-ploughing device[14].

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