Finite element analysis of flexural behavior of different fiber reinforced ultra-high-strength concrete beam under different environments

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Abstract. In this paper, finite element simulation of ANSYS was carried out to study initial crack load, ultimate load and load-deflection relationship of ultra-high-strength concrete beam with different ratio of steel fiber and PVA fiber under general environment and corrosive environment respectively. The results show that with the increase of the content of steel fiber, the initial crack load and ultimate load of ultra-high-strength concrete beam are increasing; and with the increase of fiber content, the toughness of the beam is improved; with the increase of the content of PVA fiber, the initial crack load and ultimate load of ultra-high-strength concrete beam increase first and then decrease. The incorporation of the two kind of fibers increases the toughness of the beam to a certain extent and limits the occurrence and development of the crack. When steel fiber mixing rate was 3% in common environment, initial crack load and ultimate load is increased by 155.4% and 7.0% compared with HSC beam, respectively. When PVA fiber mixing rate was 0.5% in the case of easy corrosion, initial crack load and ultimate load is increased by 56.6% and 3.7% compared with HSC beam, respectively, which can effectively improve the flexural performance of the ultra high strength concrete beams.

1. Introduction

In recent years, with the development of the construction industry, the concrete has been developed to ultra high strength and ultra high performance. The ultra high strength concrete of C100 or above has been used in the important project. However, the research data of Sun Chenghui[1], Xincheng Pu[2], Tian Yudong [3] and Ouyang Dong [4] show that, with the strength grade of concrete increases, the material brittleness increases, ultra high strength concrete can appear even burst damage phenomenon when compression. In recent years, research data show that the addition of steel fiber, PVA fiber with high strength and high elastic modulus fiber can effectively improve the brittleness of concrete[5,6,7,8]. However, most researches on ultra-high-strength concrete at home and abroad are confined to material test and research, the experimental research on the fiber reinforced ultra-high-strength concrete applied to the component is less. Therefore, this article mixed with steel fiber and Polyvinyl alcohol fiber (PVA fiber) in the general environment and corrosion environment respectively. The initial cracking load and ultimate load of the ultra -high-strength concrete beams with different ratios of fiber were analyzed by finite element analysis (FEA), which can provide reference for the engineering application of fiber reinforced ultra-high-strength concrete.

2. Test scheme design

In this paper, the ultra-high-strength beams with water-cement ratio of 0.22, respectively, to change the steel fiber mixed rate of 0%, 1%, 2%, 3%, four levels, change the PVA fiber mixing rate of 0%, 0.5%, 1.0%, 1.5%, four levels, a total plan design 7 rectangular section beams. The length of the beam is 1500mm, the net span is 1200mm, the cross-section size is 150mm × 250mm (see Figure 1). The longitudinal tensile reinforcement in the beam adopts 2C25 (HRB400 grade) reinforcement, the reinforcement ratio is 2.62%, Stand reinforced with 2B8 (HRB335 grade)
reinforcement, B8@100 (HRB335 grade) steel bars are used for the stirrups, the elastic modulus of steel bars in the beam is 200GPa. The finite element analysis of 7 ultra-high-strength concrete beams is carried out to analyze the initial crack load, the ultimate load and the load-deflection curve of the beam.

In the ANSYS modeling process, in order to simulate the two points loading of the distribution beam, the beam is loaded at the three equal points of the beam net span. And the concentrated load acting on the third point is replaced by the uniform load. The load area is 100mm × 150mm. A surface constraint of 100 mm × 150 mm is applied at the distance of 150 mm from the edge of the beam to simulate the support form of the rigid plate, So that the simulated beam is closer to the actual force situation.

In this paper, the steel fiber reinforced concrete beam using separate model, fiber reinforced ultra-high-strength concrete selected Solid 65 unit, for the longitudinal force steel and stirrups selected Link8 unit. A 100 mm × 150 mm analog rigid plate was set at the support and loading points. The treatment method of fiber in concrete adopts modified concrete constitutive law, concrete Poisson's ratio is 0.23. The reinforcement of beam is modeled by bilinear isotropic hardening model (BISO), and the Poisson's ratio is 0.3. The stress-strain relationship of the concrete before cracking and crushing is linear, and the William-Warnke failure criterion is adopted after cracking and crushing.

<table>
<thead>
<tr>
<th>Test number</th>
<th>Water-cement ratio</th>
<th>Steel fiber content/kg⋅m^3</th>
<th>PVA fiber content/kg⋅m^3</th>
<th>f_c/Mpa</th>
<th>f_s/Mpa</th>
<th>E/10^3N⋅mm^2</th>
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<tr>
<td>HSC</td>
<td>0.22</td>
<td>0</td>
<td>0</td>
<td>97.2</td>
<td>6.7</td>
<td>4.970</td>
</tr>
<tr>
<td>HSC-A1</td>
<td>0.22</td>
<td>78</td>
<td>0</td>
<td>105.4</td>
<td>11.4</td>
<td>5.060</td>
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<tr>
<td>HSC-A2</td>
<td>0.22</td>
<td>156</td>
<td>0</td>
<td>109.4</td>
<td>15.8</td>
<td>5.120</td>
</tr>
<tr>
<td>HSC-A3</td>
<td>0.22</td>
<td>234</td>
<td>0</td>
<td>112.0</td>
<td>16.1</td>
<td>5.320</td>
</tr>
<tr>
<td>HSC-B1</td>
<td>0.22</td>
<td>6.5</td>
<td>0</td>
<td>94.1</td>
<td>7.7</td>
<td>5.065</td>
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<tr>
<td>HSC-B2</td>
<td>0.22</td>
<td>13.0</td>
<td>0</td>
<td>91.2</td>
<td>8.4</td>
<td>5.090</td>
</tr>
<tr>
<td>HSC-B3</td>
<td>0.22</td>
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<td>0</td>
<td>88.2</td>
<td>9.0</td>
<td>5.300</td>
</tr>
</tbody>
</table>

Note: The letters in the sample number mean:
1) HSC: ultra-high-strength concrete beams;
2) A, B: the type of fiber, A that the incorporation of steel fibers, B that the incorporation of PVA fibers;
3) 1, 2, 3: Said fiber content (unitkg⋅m^3), for steel fiber on behalf of the content of 78, 156, 234, for PVA fibre on behalf of the content of 6.5, 13.0, 19.5.
3. Finite element results and analysis

3.1 Analysis of flexural behavior of steel fiber reinforced ultra-high-strength concrete beams

3.1.1 Cracking load and ultimate load under different steel fiber content

Figure 2 shows the initial cracking load of ultra-high-strength concrete beams with different steel fiber content. From the data, it can be found that the initial cracking load of ultra-high-strength concrete beams is increased after the incorporation of steel fibers, and the initial cracking load increases with the increase of steel fiber content. With the increase of steel fiber content, the initial cracking load increases by 139.1% ~ 155.4% compared with HSC beam, which is because the incorporation of steel fiber, improve the mechanical properties of concrete, especially the splitting tensile strength.

Figure 3 shows the ultimate load of ultra-high-strength concrete beams with different steel fiber content. It can be seen from the figure, with the increase of steel fiber content, the ultimate load increases by 4.2% to 7.0% compared with HSC beam. When the steel fiber content is 3%, the ultimate bearing capacity reaches the maximum, which is 191.7 kN.

3.1.2 Equivalent von Mises stress

Figure 4 is the equivalent cracking von Mises stress of steel fiber reinforced ultra-high-strength concrete beam. It can be seen from the figure that the maximum compressive stress in the initial cracking phase occurs in the compression zone in the middle and upper part of the beam span. The compressive stress is mainly borne by the concrete in the compression zone and the two longitudinal compressive reinforcement. The maximum compressive stress of concrete is increased with the increase of steel fiber content, and the maximum compressive stress of concrete is 2.5 times of that of HSC beam when the steel fiber content is 2%. This is due to the incorporation of steel fiber, concrete and steel fiber share the stress, enhance the energy absorption of concrete, delayed the initial cracks appear, thus significantly improving the initial cracking strength.

Figure 5 is the equivalent yield von Mises stress of steel fiber reinforced ultra-high-strength concrete beam. It can be seen from the figure, the maximum compressive stress mainly occurs in the upper compression zone during the yield stage. This is mainly because the steel bar exits the work after the steel bar reaches the yield stress, and the concrete in the compression zone alone bears the stress until crushed. The maximum compressive stress of concrete increases with the increase of steel fiber content, that is, the maximum compressive stress is 2.4% ~ 8.8% higher.
than that of HSC beam with the increase of steel fiber content. This is because with the increase of steel fiber content, the steel fiber evenly distributed in the concrete, the fibers across the cracks increased. When the internal forces redistribute, these steel fibers share the same stress, so that the matrix can continue to bear some load after cracking. It shows that the ultra-high-strength concrete beam with steel fiber has bigger load-carrying deformation capacity, the failure mode of the beam changes from brittle failure to ductile failure.

### 3.1.3 Load - deflection curve

Figure 6 is the load-midspan deflection curve of steel fiber reinforced concrete beam. It can be seen from the figure that the load-deflection changes of the concrete beams with different steel fiber ratios are similar before the yield load. The load-deflection curves of concrete beams with different steel fiber ratios are different after beam yield. When the beams yield, the load-deflection curves of concrete beams with different fiber content are different. That is, under the same load, the flexural performance of the ultra-high-strength concrete beam is improved with the increase of the steel fiber content, the toughness is improved and the deflection is small.

### 3.2 Analysis of flexural behavior of PVA fiber reinforced ultra - high - strength concrete beams

#### 3.2.1 Cracking load and ultimate load under different PVA fiber content

Figure 7 shows the initial cracking load of ultra-high-strength concrete beams with different PVA fiber content. It can be seen from the figure that the initial cracking load of the beam first increases with the increase of the PVA fiber content, and the initial cracking load decreases slightly when the fiber volume fraction reaches 0.5%. This is because the tensile strength of PVA fiber is much larger than that of the matrix concrete, and PVA fiber has a good rate of elongation. The incorporation of PVA fibers in the concrete inhibits the generation of cracks and limits the expansion of the base material under external force, which enhances the toughness of the beam. However, with the increase of PVA fiber content, concrete will produce more internal defects. When the reinforcing effect of the fiber on the concrete is less than the weakening effect of the defect, the flexural strength of the concrete beams decreases with the increase of the fiber content.

Figure 8 shows the ultimate load of ultra-high-strength concrete beams with different PVA fiber content. It can be seen from the figure that the effect of fiber content on the ultimate load is the same as that on initial cracking load. When the fiber content is 0.5%, the ultimate load is 3.7% higher than that of HSC beam. However, with the further increase of PVA fiber content, the ultimate load slightly decreased. It is proved that the enhancement effect of PVA fiber is limited.

#### 3.2.2 Equivalent von mises stress

Figure 9 shows the equivalent cracking von Mises stress of PVA fiber reinforced ultra-high-strength concrete beam. It can be seen from the figure, in the initial cracking phase of the beam, the maximum compressive stress of the concrete occurs in the upper compression zone. With the increase of PVA fiber content, the maximum compressive stress of concrete firstly increases and then decreases slightly, the maximum compressive stress of concrete is 56.8% higher than that of HSC beam when the mixing ratio of PVA fiber is...
0.5%, and the maximum stress is 53.3% higher than that of HSC beam when the mixing ratio of fiber is 1.0%.

Figure 10 shows the equivalent yield von Mises stress of PVA fiber reinforced ultra-high-strength concrete beam. It can be seen from the figure that the maximum compressive stress in the beam during the yield stage occurs near the upper loading point of the beam. This is due to the fact that when the beam reaches the yield point, more slanting cracks are created at the loading point by the support. So there is a stress concentration phenomenon near the loading point. The maximum compressive stress of concrete increased by 2.9% ~ 9.0% than that of HSC beam when fiber content changed from 0.5% to 1.5%. This is because when the volume fraction of PVA fibers is small, the internal force redistribution after concrete cracks is not uniform. The fiber under high load momentarily pulls out, making the toughening effect of the fiber limited. However, with the increase of the content of PVA fiber, the fiber across the crack increases, the crack of the fiber reinforced ultra-high-strength concrete beam expands stably, so the PVA fiber plays a good toughening effect.

3.2.3 Load-deflection curve

Figure 11 is the load-midspan deflection curve of PVA fiber reinforced concrete beam. It can be seen from the figure, with the increase of PVA fiber mixing rate, the toughness of the ultra-high-strength concrete beam is improved. Under the same load, the deflection of the fiber reinforced ultra-high-strength concrete beam is reduced. This is because when the concrete beam cracks, the fiber acts as a bridge force, effectively restricting the development of cracks, until the fiber is pulled out or pulled off the beam will be destroyed.

4. Simulation formula of ultimate bearing capacity of fiber reinforced ultra-high-strength concrete beams

In order to make the fiber reinforced ultra-high-strength concrete beam better applied in practical engineering, and at the same time, it is convenient to connect with the calculation formula of normal section bearing capacity of ordinary concrete flexural members. Based on the calculation formula of bearing capacity of high-strength reinforced concrete beams, the formulas for calculating the bearing capacity of steel fiber reinforced concrete beams and PVA fiber reinforced concrete beams are deduced respectively.

According to the specification [9], the normal section bearing capacity of ordinary high-strength concrete beams is calculated according to formula (1):

\[ M_u = f_y A_s (h_0 - \frac{f_y A_y}{2 \alpha_c f_c b}) \]  

In the formula: \( f_y \) is the tensile strength design value of longitudinal tensile steel bar, \( A_s \) is the cross-sectional area of the tensile reinforcement, \( f_c \) is the design value of axial compressive strength of concrete, \( \alpha_c \) is the coefficient, the concrete selects C50 to take 1, selects C80 to take 0.94, during the linear interpolation, \( b \) is the width of the section, \( h_0 \) is the effective height of the beam section.

Considering the reinforcing effect of steel fiber and PVA fiber on the normal section of ultra-high-strength concrete beam. This paper assumes the following two formulas:

\[ M_{u_1} = (1 + k_f A_f) M_u \]  
\[ M_{u_2} = (1 + k_p A_p) M_u \]

In the formula, \( M_u \) is the ultimate bearing capacity of ordinary high-strength concrete beam, its value is 179 kN; \( M_{u_1} \) is the maximum bending moment of steel fiber reinforced ultra-high-strength
concrete beam; \(k_s\) is the enhancement coefficient of the steel fiber; \(k_p\) is the enhancement coefficient of the PVA fiber; \(\lambda_s\) is the characteristic value of steel fiber content; \(\lambda_p\) is the characteristic value of PVA fiber content; The coefficients \(k_s\) and \(k_p\) are derived by calculation. The bending moment of the beam cross section is calculated as \(M = P \times L\). All the test beams in this paper have the same size and loading position, that is, \(L = 0.4m\). Therefore, the ultimate load \(P\) can be used instead of \(M\) to derive \(k_s\) and \(k_p\).

Firstly, the steel fiber reinforced coefficient \(k_s\) is deduced. Taking the ultra-high-strength concrete beam with 1% steel fiber volume fraction (HSC-A1) as an example, According to the physical properties of steel fiber, steel fiber length \(l_f = 30mm\), diameter \(d_f = 0.55mm\), \(\lambda_s\) is defined as \(\rho_s l_f / d_f = 1.0\% \times 54.5 = 0.55\). Bringing \(M_u = 179.1kN\) and \(M_{ul} = 186.7kN\) into formula (2), obtained \(k_s = 0.077\). Similarly, The beam HSC-A2 can be obtained \(k_s = 0.043\). The beam HSC-A3 can be obtained \(k_s = 0.043\). Take the average of three beams, get \(k_s = 0.054\). So the ultimate bearing capacity of the steel fiber reinforced ultra-high-strength concrete beam can be calculated as:

\[M_{u1} = (1 + 0.054\lambda_s)M_u\] (4)

Secondly, the PVA fiber reinforced coefficient \(k_p\) is deduced. Taking the ultra-high-strength concrete beam with 0.5% PVA fiber volume fraction (HSC-B1) as an example, According to the physical properties of PVA fiber, PVA fiber length \(l_f = 12mm\), diameter \(d_f = 0.1mm\), \(\lambda_p\) is defined as \(\rho_p l_f / d_f = 0.5\% \times 120 = 0.6\). Bringing \(M_u = 179.1kN\) and \(M_{ul} = 185.7kN\) into formula (3), obtained \(k_p = 0.061\). Similarly, The beam HSC-B2 can be obtained \(k_p = 0.023\). The beam HSC-B3 can be obtained \(k_p = 0.013\). Take the average of three beams, get \(k_p = 0.032\). So the ultimate bearing capacity of the PVA fiber reinforced ultra-high-strength concrete beam can be calculated as:

\[M_{u2} = (1 + 0.032\lambda_p)M_u\] (5)

4.1 Comparison of calculated values and simulated values

Fig.12 and Fig.13 are the scatter diagram of the calculated values and simulated values of the flexural capacity of the steel fiber reinforced concrete beams and the PVA fiber reinforced concrete beams, respectively. From the figure, it can be seen that the difference between the calculated value and the simulated value is within the range of 5%, so the formula deduced in this paper can meet the practical application requirements.

5. Conclusion

In this paper, the influence of steel fiber and PVA fiber on the initial cracking load and ultimate load of ultra-high-strength concrete beam under different mixing rates are studied by ANSYS finite element simulation. The results show that:

(1) With the increase of steel fiber content, the initial cracking load and ultimate load of the ultra-high-strength concrete beam are increased. When the steel fiber content is 3%, the initial cracking load and ultimate load of the beam reach the maximum value. With the increase of the steel fiber content, the deflection of the beam under the same load gradually decreases.

(2) With the increase of PVA fiber content, the initial
cracking load and ultimate load of the ultra-high-strength concrete beam increase first and then decrease, but they are higher than HSC beam. When the fiber content is 0.5%, the initial cracking load and the ultimate load of the beam reach the maximum.

(3) Based on the calculation formula of flexural capacity of ordinary reinforced concrete beams, the formula for calculating the flexural capacity of steel fiber reinforced ultra-high-strength concrete beams and PVA fiber reinforced ultra-high-strength concrete beams is presented in this paper.

References


