Abstract—The promotion of electric vehicles (EVs) has eased the shortage of fossil fuels, but also brings challenges to the grid. Load modeling of EV is an important technical reserve to deal with the challenge. From practical application, this paper built the model of charging system consisting of voltage source PWM rectifier, phase-shift full bridge ZVS DC-DC converter and power battery pack and connected the model built to distribution system containing composite load. Furthermore, the paper calculated the critical clearing time of induction motor and used it as an index to evaluate the transient voltage stability under different EV penetration rate. Then the impact of dynamic characteristics of EV charging station on transient voltage stability of distribution network and its influence factors was analyzed. The results provided useful information for the safe and stability of power system with large-scaled EV accessed.

Keywords-electric vehicle; transient voltage stability; charging station; dynamic model

I. INTRODUCTION

With the increasing popularity of vehicles, environmental pollution and energy crisis it bought has become more and more serious. To develop pollution-free EV has important strategic significance to relieve above problems, but EV charging load is of strong random characteristics, and will always superpose existing peak load curve, then increase peak shaving task. As a result, many scholars have done research on the impact of large-scaled charging load on the power grid and the coordinated charging strategy.

Current research on electric vehicle load modeling focuses on the static load model, including the prediction of daily load curve, to analyze the problems of load balance, harmonic pollution, power loss and voltage drop[1], and further to optimize the dispatching a and location, but do little research on the dynamic process. References [2-3] estimated large-scaled EV charging load data according to the survey data and the development law of EVs; [4] studied its effects aiming at specific EV type and application scenario; [5] study voltage sags under different EV penetration rate taking a typical low-voltage distribution network in British as example. On the other hand, EV charging station is a typical power electronic device of large capacity and high current [6-7], which will bring significant impact on transient voltage stability of power system. Induction motor is an important dynamic load in power system, [8] used the critical clearing time of it as an index to reflect the transient voltage stability of the node with induction motor load. Reference [9] proposed a margin index considering induction motor load to study transient voltage stability with large-scaled EV load accessed, but considering EV load as static load.

The paper chose phase-shift full bridge ZVS DC-DC converter and voltage source PWM rectifier, according to the battery parameters of Tesla Model S 85, to build the dynamic model of EV charging station. Critical clearing time of induction motor in composite load is calculated. Then connected the model and composite load to IEEE33 node distribution system simulation case, setting different scenarios, utilizing the critical clearing time calculated before to evaluate the impact of dynamic process of EV charging station on transient voltage stability of distribution network and analyze the influence factors.

II. DYNAMIC SIMULATION MODEL OF EV CHARGING SYSTEM

Charging system is the core part of an EV charging station. Common DC bus structure has the advantages of managing power quality of grid side easily and needing fewer rectification devices, and is adopted to established the model in this paper.

A. Power Battery Modeling

Among many kinds of battery models, equivalent circuit model has explicit physical meaning and is easy for mathematical analysis [10]. PNGV model shown below is used in this paper. This model can describe the transient process of batteries and relationship between battery performance and state of charge (SOC).

![FIGURE I. THE EQUIVALENT CIRCUIT OF PNGV MODEL.](image-url)
Discretization equation of this circuit can be obtained as below, and through parameters identification test the circuit parameters could be gained.

\[ U_{\text{dc}} = E - \frac{1}{C_1} \sum (I, \Delta t) - R_l I_{\text{dc}} - R_i I_{\text{in}} \]  

(1)

In Tesla Model S battery system, 7623 cells form a battery pack. The circuit model and parameters of the battery pack can be obtained by circuit transformation.

B. DC-DC Converter Modeling

The main circuit topology of phase-shift full bridge ZVS converter is shown as below.

This topology is chosen for the following considerations: It has isolation transformer, which is safer, can guarantee personal security while charging; it includes four power switches so is suitable for high power value occasions; it can achieve ZVS so reduce switching losses.

Small signal modeling methods of Buck can be used to established the model of phase shifted full bridge converter, which is shown above. Using average current mode, the control block diagram of double loop control method of voltage and current is shown in Figure IV.

C. Three-Phase PWM Rectifier

Compared to thyristor phase controlled rectifier and diode rectifier, PWM rectifier circuit can maintain the power factor approximating to unity through control, so three phase VSR is used in this paper to build the model for the AC-DC part of the charger.

There are two aims of the controller: maintaining the voltage of DC bus; realizing unity power factor operation. Double loop strategy of PI regulator, which is extensively used is adopted. The control block diagram is shown below.

III. Transient Voltage Stability Index Considering Induction Motor

In composite load model, dynamic behavior of the load is described by parallel static load and induction motor. The equivalent circuit diagram of induction motor is shown in Figure VI.

Figure VII shows a typical mechanical characteristic curve of three phase induction motor. The one of larger value among the intersections of electromagnetic torque and mechanical torque curves after the fault is the unstable equilibrium point, namely the critical clearing slip. The corresponding critical clearing time could represents transient voltage stability.

By T-equivalent circuit of Figure VI., it is easy to get the mechanical torque \( T_e \):

\[ T_e = \frac{R_1}{s} \frac{V^2}{(s + R_1 Z_1) + (X_1 + X_2)^2} \]  

(2)

In which

\[ \dot{y}_i = \frac{Z_{an}}{Z_{an} + Z_i} \]  

(3)

\[ R_i + jX_i = \frac{Z_{an} Z_v}{Z_{an} + Z_i} \]  

(4)

From above equation, the critical clearing slip could be solved:

\[ s_c = \frac{R_1 V_1^2 - 2T_e R_1 \sqrt{V_1^2 - 4V_1^2 T_e R_1 - 4V_1^2 (X_1 + X_2)^2}}{2 T_e (R_1^2 + (X_1 + X_2)^2)} \]  

(5)

Corresponding critical clearing time:

\[ t_c = \frac{2H(s_c - s_0)}{T_{an}} \]  

(6)
In which $s_m$ is the initial slip of the motor. In actual dynamic process, there is a period of transient time of the rotor for recovery after the fault is removed, which will have a negative impact on the critical clearing time. When considering the rotor’s transient time, the result should be amended as:

$$t_{on} = t_s \frac{S_{dm}}{T_m}$$  \hspace{1cm} (7)$$

In which $S_{dm}$ is the deceleration area during the transient process, i.e., the area of which the electromagnetic torque is lower than mechanical torque, and it can be obtained by time domain simulation.

![Equivalent Circuit of Induction Motor](image)

**FIGURE VI. EQUIVALENT CIRCUIT OF INDUCTION MOTOR.**

![Torque-Slip Curves](image)

**FIGURE VII. TORQUE-SLIP CURVES OF A GENERAL MOTOR.**

### IV. SIMULATION AND ANALYSIS OF IMPACT OF EV CHARGING STATION ON TRANSIENT VOLTAGE STABILITY OF DISTRIBUTION NETWORK

#### A. Simulation Configuration

Simulation model was built on MATLAB/Simulink platform. Taking lithium battery pack of Tesla Model 85 as an example, its main parameters are shown in the following.

**TABLE I. PARAMETERS OF BATTERY PACK IN TESLA MODEL S 85**

<table>
<thead>
<tr>
<th>Capacity (kWh)</th>
<th>Rated Voltage(V)</th>
<th>Cell Voltage(V)</th>
<th>Cell Cut-off Voltage(V)</th>
<th>Cell Capacity (Ah)</th>
</tr>
</thead>
<tbody>
<tr>
<td>85</td>
<td>356</td>
<td>3.6</td>
<td>4.2</td>
<td>3.1</td>
</tr>
</tbody>
</table>

The paper adopted constant-voltage limiter-current(CVLC) mode and set output voltage of single charging pile to be 416V, which is the charging cut-off voltage. The other main parameters of the charger model is shown in table II and table III.

**TABLE II. MAIN PARAMETERS OF THREE PHASE VOLTAGE SOURCE PWM RECTIFIER**

<table>
<thead>
<tr>
<th>Input Voltage (kV)</th>
<th>DC Bus Voltage (V)</th>
<th>Capacity (kW)</th>
<th>De Capacitor (μF)</th>
<th>Switching Frequency (Hz)</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.38</td>
<td>650</td>
<td>500</td>
<td>7500*2</td>
<td>1350</td>
</tr>
</tbody>
</table>

**TABLE III. MAIN PARAMETERS OF PHASE-SHIFT FULL BRIDGE ZVS DC-DC CONVERTER**

<table>
<thead>
<tr>
<th>Capacity (kW)</th>
<th>Switch Frequency (kHz)</th>
<th>Filter Capacitor (μF)</th>
<th>Filter Inductor (μH)</th>
<th>Resonant Capacitor (μF)</th>
<th>Resonant Inductor (μH)</th>
<th>Turns Ratio</th>
</tr>
</thead>
<tbody>
<tr>
<td>35</td>
<td>20</td>
<td>4500</td>
<td>400</td>
<td>5</td>
<td>9</td>
<td>0.87</td>
</tr>
</tbody>
</table>

In IEEE33 node radial distribution network, several representative nodes was selected to access the dynamic model of EV charging station and composite load model, in order to analyze the impact of dynamic process of EV charging station on transient voltage stability of distribution network and its influence factors.

#### B. Impact of Different EV Penetration rate on Transient Voltage Stability of Distribution Network

Set the proportion of induction motor load to be 30%, parameters of which are shown in table IV. When the EV load penetration rate is 25%, the number of EVs charging in every station, whose SOC, charging power and other parameters are shown in table V.

**TABLE IV. MAIN PARAMETERS OF INDUCTION MOTORS OF THE LOAD NODES**

<table>
<thead>
<tr>
<th>Steady Slip (pu)</th>
<th>$R_1$ (pu)</th>
<th>$X_1$ (pu)</th>
<th>$R_2$ (pu)</th>
<th>$X_2$ (pu)</th>
<th>$X_m$ (pu)</th>
<th>$2H(s)$</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.0473</td>
<td>0.05</td>
<td>0.09</td>
<td>0.0486</td>
<td>0.0618</td>
<td>2.1153</td>
<td>0.2854</td>
</tr>
</tbody>
</table>

**TABLE V. PARAMETERS OF EV CHARGING LOAD**

<table>
<thead>
<tr>
<th>Node</th>
<th>Number of EVs</th>
<th>SOC(%)</th>
<th>Charging power (kW)</th>
<th>Total power(kW)</th>
</tr>
</thead>
<tbody>
<tr>
<td>2</td>
<td>2</td>
<td>85</td>
<td>15</td>
<td>25</td>
</tr>
<tr>
<td>3</td>
<td>1</td>
<td>66</td>
<td>22.5</td>
<td>22.5</td>
</tr>
<tr>
<td>4</td>
<td>2</td>
<td>82</td>
<td>17.4</td>
<td>30</td>
</tr>
<tr>
<td>7</td>
<td>3</td>
<td>89</td>
<td>12.6</td>
<td>2.1</td>
</tr>
<tr>
<td>14</td>
<td>1</td>
<td>69</td>
<td>22.5</td>
<td>105</td>
</tr>
<tr>
<td>18</td>
<td>4</td>
<td>12</td>
<td>30</td>
<td>105</td>
</tr>
<tr>
<td>25</td>
<td>4</td>
<td>58</td>
<td>25</td>
<td>105</td>
</tr>
<tr>
<td>33</td>
<td>1</td>
<td>85</td>
<td>15</td>
<td>15</td>
</tr>
</tbody>
</table>

Set the fault at the outlet of the source(node 1), from 0.6s to 0.7s. Taking node 2 as an example, When the EV load penetration rate is 50% and 25%, voltage curve of the load bus and slip curve of the induction motor is shown in Figure VIII.
It can be seen that with the increase of EV load penetration rate, the recovery speed of the bus voltage is slowed down, which is against the stability of voltage. In the following, the critical clearing time will be used as an index to evaluate the transient voltage stability of each node quantitatively. Calculation results are shown as below.

![Figure VIII. Voltage and Induction Motor’s Slip Change Tendency of Node 2 During Short Circuit](image)

**FIGURE VIII.** VOLTAGE AND INDUCTION MOTOR’S SLIP CHANGE TENDENCY OF NODE 2 DURING SHORT CIRCUIT.

Obviously, as EV penetration rate increases, the transient voltage stability level of the nodes first increases and then decreases. While the penetration rate is small, compared with the scenario without EV load, the transient voltage stability level slightly improves. This point is more evident in the nodes with load of higher value. The nodes containing less load(node 2) almost remains even, while the nodes with lowest load level (3, 18) did not even rises.

The reason is that after the clearing of the fault, rapid response ability of the rectifier played a certain role in promoting voltage recovery. Figure X(A) shows that after clearing the fault at 0.7s, reactive power of the rectifier is negative in the recovery process, so that the bus voltage is promoting voltage recovery. Figure X(B) shows that after the transient voltage stability slightly improves. This point is more evident in the nodes with load of higher value. The nodes containing less load(node 2) almost remains even, while the nodes with lowest load level (3, 18) did not even rises.

![Figure IX. Comparison of Critical Clearing Time Under Different EV Load Penetration Rate](image)

**FIGURE IX.** COMPARISON OF CRITICAL CLEARING TIME UNDER DIFFERENT EV LOAD PENETRATION RATE.

C. Influence Factors Analysis

1) The distance from the root node: As can be seen from Figure IX, node 4, 14 and node 3, 18, respectively have the same value of load, under each penetration rate, the nodes further from the source, i.e. 14,18 has smaller critical clearing time.

2) Reactive power capacity of each node: Taking EV penetration rate of 25% as an example, it can be seen from Figure X(B) obviously that for a node, the higher the reactive power capacity is, the higher the transient voltage stability is, the smaller the impact EV charging stations dynamic characteristics could bring.

V. Conclusion

The simulation results showed that: with low EV load penetration rate, the rectifier can quickly respond to generate reactive power, transient voltage stability would slightly increase relative to that of no EV load accessed, which is more evident in the nodes with load of higher value. However, when the penetration rate reaches higher, EV charging load begins to have a negative impact on transient voltage stability. By Comparing each access node, it can be found that the impact of charging station dynamic process on transient voltage stability has much to do with reactive power capacity of the access node and the distance from the source, which should be paid enough attention to in charging station site selection and construction. Combining the probability nature of EV charging distribution to study the dynamic characteristics of charging stations, will be the direction of further studies.

**REFERENCES**


[9] Yanxia Chen, Peiwenn Zheng, “Study on the influence of large-scaled electric vehicle dispersed charging on transient voltage stability of...