Hybrid Biogeography/Complex-based Optimization

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Abstract—The optimization of complex systems is a very difficult problem in modern engineering technology. It is with multi-subsystems, multi-objectives and multi-constraints. In this paper, a novel solution to the complex systems optimization called HBBO/Complex. HBBO/Complex adapted from biogeography-based optimization (BBO) and combined the simulated annealing (SA). The inferior migrated islands will not be selected unless they pass the Metropolis criterion of SA. This method can prevent the local optimal solution. Compared with typical existing many-objective optimization algorithms, HBBO/complex has better convergence characteristics. The results confirm the HBBO/complex provides the best performance in the benchmark problems.

Keywords—biogeography; SA; many-objectives optimization

I. INTRODUCTION

Multi-objective evolutionary algorithms (MOEAs) are well-suited for solving numerous multi-objective problems with two or three objectives. However, as the number of conflicting objectives increases, the performance of most MOEAs is badly deteriorated [1]. In case of Pareto-based MOEAs, these difficulties are intrinsically related to the fact that as the number of objectives increase, the proportion of non-dominated elements in the population grows, being increasingly difficult to discriminate among solutions using only the dominant relation [2].

Many-objective optimization evolutionary algorithms (MaEAs) refer to optimization problems greater than 4 [3]. Due to minimize and maximize problem can be mutual transformation, therefore, without loss of generality, this article mainly describes minimize multi-objective problem and its related concepts MaEAs can be defined as follows:

Minimize \( F(x) = (f_1(x), f_2(x), \ldots, f_m(x)) \)

Subject to \( x \in \Omega \)

Where \( \Omega \subseteq \mathbb{R}^n \) is the feasible search region, \( x=(x_1, x_2, \ldots, x_n) \) \( T \) is the decision variable vector, \( f_i : \mathbb{R}^n \rightarrow \mathbb{R}, i=1,2,\ldots,m \) are the \( m \) objective functions, and \( R_m \) is the objective space.

Classical optimization methods may fail to do so especially when the objective functions are nondifferentiable and without closed forms. For this reason, people resort to heuristic optimization methods such as evolutionary (EAs). Multi-objective evolutionary algorithms (MOEAs) have been attracting considerable attention. The number of MOEAs can be classified as three categories: (1) the decomposition-based approaches [4], [5] and [6]; (2) the indicator-based approaches [7], [8] and [9]; and (3) the objective aggregation-based approaches [10], [11] and [12].

Biogeography/Complex based optimization algorithm is a kind of adaptive decomposition method. Detailed explanations of BBO/complex are introduced in Section II. However, the performance and convergence rate of BBO/complex is still to be further improved. With the migration flow of \( n \) SIV between rich and poor islands, we need a method to enhance its exploration and evaluate the badly modified whether to be accepted or not, it can prevent the past features always be overwritten by the newly emigrated features from other islands. On the other hand, since there are plenty of targets and constraints in the subsystem, when sharing information in the subsystem, we need a new method to reduce the computation time of the CPU. The simulated annealing (SA) algorithm was presented by Kirkpatrick et al. [13] and Valdo Cerny [14], SA algorithm is an intelligent algorithm that randomly search optimization based on probability. It is having the capacity of probabilistic jumping and it is able to accept non-inferior solutions and inferior solutions. Thus, effectively avoid falling into minimal local solutions. We are inspired here by Metropolis criterion of SA algorithm to solve the problem posed above. Details about SA will be introduced in next section.

II. BBO FOR COMPLEX SYSTEMS AND SIMULATED ANNEALING

A. BBO for Complex Systems

BBO was invented less than a decade ago, but according to [15] to provide competitive optimization performance with ACO [16], differential evolution (DE) [17], particle swarm optimization (PSO) [18], and many other algorithms. Complex systems contain more than one subsystem, each of which is partially independent of the others. BBO/Complex is extending BBO to systems with multi-subsystems, where each subsystem contains multi-objectives and multi-constraints. The environment of BBO/Complex includes \( n \) archipelagos, where \( n \) is the number of subsystems. Every archipelago consists of islands. The islands represent possible solutions to the problem. The structure of BBO/Complex is conceptually different from other typical algorithm. It includes both the framework and the optimization algorithm, as showed in Figure 1. It provides an efficient way to communicate between subsystems and provides a unique migration strategy to share information both within and across subsystems.

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distribution. It means if a system is maintained in a thermal equilibrium at temperature T, then the probability distribution p of its energy E can be achieved by [26]:

\[ P(E) = e^{-\frac{\Delta E}{k_B T}} \]

Where KB is a Boltzmann's constant. The difference in energy \( \Delta E \) means the difference in cost function between the past and current iterations, which can be determined as follows:

\[ \Delta E = f(x_n) - f(x_o) \]

For minimization problems, \( \Delta E \leq 0 \) means \( f(x_n) \leq f(x_o) \), so the new design point is directly accepted. Otherwise, the Metropolis criterion will be enabled to decide whether to accept or reject \( x_o \). For this case where \( \Delta E > 0 \), the acceptance probability is treated probabilistically according with the relation

\[ P = \frac{1}{1 + \exp(\Delta E / k_B T)} \]

It can be viewed the influence of temperature in the acceptance process. For the highest magnitudes of T, The acceptance probability to choose a worse state is likewise higher. This process will avoid trapping into local optima. As the temperature decrease, the SA algorithm accepts only states which minimize the FO cost. Therefore, the way that temperature decreases during the iteration of the algorithm is an important parameter, this parameter is named cooling schedule [26].

III. THE HYBRID BBO/COMPLEX ALGORITHM

The proposed hybrid BBO/complex (HBBO/complex) is described by Algorithm 3. When the migration stage is completed, the features (n SIV) of the islands will not be directly overwritten with the new values that come from the probabilistically selected source islands. Instead, there n SIV of the islands is saved in two temporary matrices. Each row of their matrices represents one individual. The old independent variables are used again if and only if the modified individual shows lower solution quality and does not meet the Metropolis criterion. With this restriction on the migration stage, the overall performance of the HBBO/Complex algorithm can be enhanced. By this method, the exploration of the BBO/complex algorithm is greatly improved.
IV. SIMULATION RESULTS

In this section, we compare the performance of HBBO/Complex in real-world benchmark problems with Original BBO/Complex and Collaborative optimization (CO). The benchmark problems are obtained from [22] and include the speed reducer problem. It contains several subsystems and multi-constraints. The speed reducer problem is a gear box design problem. The objective is to minimize the gear box weight and the von Mises stresses for shafts 1 and 2. It contains 3 objectives, 11 constraints, and 7 design variables. This problem is defined as follows:

Min $F_1 = 0.7854X_1X_2^2(3.3333X_3^2 + 14.9334X_4 - 43.0934) - 1.05079X_1(X_6^2 + X_7^2) + 7.477(X_6^3 + X_7^3) + 0.7845(X_4X_6^2 + X_5X_7^2)$,

Min $F_2 = \sqrt{\frac{(745X_4)}{X_2X_3}} + 1.69 \times 10^7$,

Min $F_3 = \sqrt{\frac{(745X_2)}{X_2X_3}} + 1.575 \times 10^8$.

Such that the following constraints hold:

\begin{align*}
g_1 &= \frac{27}{x_1x_2^2x_3} - 1 \leq 0 \\
g_2 &= \frac{397.5}{x_1x_2^2X_3} - 1 \leq 0 \\
g_3 &= \frac{1.93x_4^3}{x_2x_3x_6^4} - 1 \leq 0 \\
g_4 &= \frac{1.93x_3^3}{x_2x_3x_7^4} - 1 \leq 0 \\
g_5 &= \sqrt{\frac{(745X_4)}{X_2X_3}} + 1.69 \times 10^7 - 1100 \leq 0 \\
g_6 &= \sqrt{\frac{(745X_2)}{X_2X_3}} + 1.575 \times 10^8 - 850 \leq 0 \\
g_7 &= x_2x_3 - 40 \leq 0 \\
g_8 &= \frac{x_1}{x_2} - 12 \leq 0 \\
g_9 &= \frac{-x_1}{x_2} + 4 \leq 0 \\
g_{10} &= \frac{1.5x_6 + 1.9}{x_4} - 1 \leq 0 \\
g_{11} &= \frac{1.1x_7 + 1.9}{x_5} - 1 \leq 0
\end{align*}

Table 1 shows the parameters used in the HBBO/Complex.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
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</thead>
<tbody>
<tr>
<td>Population</td>
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<tr>
<td>$P_{migrate}$</td>
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</tr>
<tr>
<td>$P_{mutate}$</td>
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<tr>
<td>$q$</td>
<td>0.9</td>
</tr>
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</table>

Table 1: Simulation parameters of the HBBO/Complex algorithms
Fig 2: The original BBO/Complex algorithm feasibility and cost of each objective for the speed reducer problem.

Fig 3: The CO algorithm feasibility and cost of each objective for the speed reducer problem.
In this paper, we propose a novel complex system solution called HBBO/Complex. We compare the HBBO/Complex, CO and original BBO/Complex algorithm. The figures also show that the performance of HBBO/Complex is superior to other two algorithms. With this process, the old features will not always be overwritten by the newly emigrated features from other islands. Instead, the Metropolis criterion is used to evaluate the badly modified populations whether they can be accepted or not. It has more flexible decomposition optimization options compared to CO and original BBO/Complex algorithm.

The obtained results show the performance of HBBO/Complex is markedly affected by introduced the SA algorithm. In general, aiming at many subsystems, many-constraints problems for complex systems this hybrid algorithm raises the algorithm's immunity level against trapping into local optima.

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REFERENCES


