Fuzzy Evaluation Model Construction of Performance Management

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Abstract. The Performance Evaluation System of functional departments in colleges and universities displays the features like multi-index, multi-attribute, concrete together with fuzzification. To avoid the defect developed by the simple combination of qualitative index and quantitative index in the Performance Evaluation, use universal fuzzy evaluation to construct the evaluation model of performance management, quantifying the index, quantifying the evaluation result by mathematic model, making the evaluation result objective, scientific and specific.

Introduction

Performance evaluation, to an organization, is a suit of methods to smooth the strategy implementation capability, combining dynamically the personal performance, individual development and organization goal together, instantly improving the organization performance through the development of individual performance and group performance, finally guaranteeing the practice of organizational strategy and the realization of professional goal.

Performance evaluation is the fundament of performance management for an organization, performance evaluation index with the features like concreteness and periodicity, easy to be conducted and realized in practice. The aim of this thesis is to employ the quantitative approach to establish a performance evaluation model of functional departments in colleges and universities. Comprehensive fuzzy evaluation is selected as the evaluation methodology, weight identification for each evaluation factor using analytic hierarchy process (AHP) [1], and then identifying the importance of each index in the entire evaluation system.

Principles of Model Establishment

Performance evaluation of functional departments in colleges and universities is very complex, affecting by various factors, referring to the quantitative index evaluation and the qualitative index. Comprehensive fuzzy evaluation is originated from the comprehensive evaluation method of fuzzy mathematics, capable of coping with the issue which is hard to quantize, suitable to settle the uncertainty issues [2] [3]. When set up the index system, the following principles are supposed to be obeyed:

System principle: due to the particularity of the products of colleges and universities, the selected index ought to be with the feature of foresight. Focus on the evaluation aim, which should be able to reflect the output efficiency and benefit of financial investment. Since the relevance universally existing among each factor, the quantity of factors ought to be stressed, reflecting the overall allocation state from multi-level and multi-view.

The combination of precision and fuzziness: some index can be calculated precisely, while some only can be described by tend or direction, the identification of index system, the selection of index and the
derivation of formula all requiring scientific supports.

Comparability principle: the identification of performance evaluation index is not only suitable for one or some colleges and universities, but also for all colleges and universities. Therefore, the index setting of the identical system is supposed to be with the comparability for individual institute.

Maneuverability principle: the index system of performance evaluation aims to be simple, convenient and applicable, with sharp selecting concept and clear definition. It is easy to collect and calculate, and with applicability and maneuverability in terms of practice.

**Construction of Fuzzy Evaluation Model**

From the perspective of the service object and the service content of the functional departments in colleges and universities, the differences among various functional departments are apparently, some focusing on students, some stressing on faculty, and meanwhile some are in charge of the administration of the faculty and the students [4]. Obviously, different types of functional departments ought to be evaluated by different performance evaluation systems. Hereby, taking the functional department, which is in charge of the administration of the faculty and the students, as an instance, illustrate the performance evaluation systems. In this thesis, there are five factors selected as the index in performance evaluation system: the performance of duty, the cooperation with other departments, student training and employment, teacher achievement and training, teaching performance (displayed in Table 1). The mathematical set of performance evaluation factors is $X = \{x_1, x_2, x_3, x_4, x_5\}$.

<table>
<thead>
<tr>
<th>performance evaluation index</th>
<th>Content of index</th>
</tr>
</thead>
<tbody>
<tr>
<td>performance of duty</td>
<td>The completion state of the quantity and quality of the duties, including the administration of the faculty and the students in daily life and the teaching work</td>
</tr>
<tr>
<td>cooperation with other departments</td>
<td>The coordinate sense and team spirit among different departments and the effective communication on management information.</td>
</tr>
<tr>
<td>student training and employment</td>
<td>The investment in training (human resource and financial support and so on) and performance evaluation, employment rate of student and student satisfaction.</td>
</tr>
<tr>
<td>teacher achievement and training</td>
<td>Achievements in scientific research, teaching performance and teacher training.</td>
</tr>
<tr>
<td>teaching performance</td>
<td>The teaching performance and student satisfaction of graduate students and undergraduate students.</td>
</tr>
</tbody>
</table>

In view of the fuzziness existed in our cognations and judgments, the principle employed in this thesis combines the precision and fuzziness together, evaluating each index separately, classifying the results into five ranks, that is, excellent, good, fine, qualified and poor, establishing the set of performance evaluation results $N = \{n_1, n_2, n_3, n_4, n_5\}$. $A = \{a_{ij}\} (i = 1,2,\cdots,5, j = 1,2,\cdots,5)$ is a single
factor evaluation matrix, suggesting that the fuzzy relation from \( M \) to \( N \), \( a_{ij} \) representing the possible result of the \( i \) th evaluation object affected by the \( j \) performance evaluation index. Calculate \( B = MA \), and hereinto \( M = [m_1, m_2, m_3, m_4, m_5] \) is the weight set of performance evaluation index. Then, according to these five performance evaluation index, identify the weight of each one, and then process the comparison evaluation among the overall results of the evaluation object and the results of each index [5].

**Data Collection**

Randomly select 200 people from the faculty and the students from a university, collecting the data mainly through interview survey and questionnaire, focusing on the performance management states of School of Science, School of Economics and Management and Architectural and Civil Engineering School. There are following five aspects are evaluated, listed in the Table 2. The evaluation result of each index is classified into five ranks, that is, excellent, good, fine, qualified and poor, and the weight of each index is also calculated [6]. Taking School of Science as an example, the evaluation results are as follows (Table 2):

<table>
<thead>
<tr>
<th>School of Science</th>
<th>excellent</th>
<th>good</th>
<th>fine</th>
<th>qualified</th>
<th>poor</th>
</tr>
</thead>
<tbody>
<tr>
<td>performance of duty</td>
<td>35</td>
<td>43</td>
<td>13</td>
<td>7</td>
<td>2</td>
</tr>
<tr>
<td>cooperation with other departments</td>
<td>48</td>
<td>30</td>
<td>15</td>
<td>5</td>
<td>2</td>
</tr>
<tr>
<td>student training and employment</td>
<td>2</td>
<td>5</td>
<td>21</td>
<td>39</td>
<td>33</td>
</tr>
<tr>
<td>teacher achievement and training</td>
<td>27</td>
<td>16</td>
<td>40</td>
<td>7</td>
<td>6</td>
</tr>
<tr>
<td>teaching performance</td>
<td>60</td>
<td>30</td>
<td>10</td>
<td>10</td>
<td>0</td>
</tr>
</tbody>
</table>

The fuzzy evaluation matrix of School of Science can be produced based on the data

\[
A_1 = \begin{bmatrix}
0.35 & 0.48 & 0.02 & 0.27 & 0.60 \\
0.43 & 0.30 & 0.05 & 0.16 & 0.30 \\
0.13 & 0.15 & 0.21 & 0.40 & 0.10 \\
0.07 & 0.05 & 0.39 & 0.07 & 0.10 \\
0.02 & 0.02 & 0.33 & 0.06 & 0.00 \\
\end{bmatrix}
\] (1)

Adopt the same data collection method to obtain the fuzzy evaluation matrixes of School of Economics and Management and Architectural and Civil Engineering School \( A_2 \) and \( A_3 \) respectively.

\[
A_2 = \begin{bmatrix}
0.36 & 0.17 & 0.10 & 0.29 & 0.44 \\
0.28 & 0.31 & 0.32 & 0.23 & 0.32 \\
0.23 & 0.35 & 0.31 & 0.33 & 0.12 \\
0.08 & 0.07 & 0.21 & 0.10 & 0.10 \\
0.05 & 0.10 & 0.06 & 0.05 & 0.02 \\
\end{bmatrix}
\] (2)

\[
A_3 = \begin{bmatrix}
0.21 & 0.31 & 0.50 & 0.38 & 0.46 \\
0.24 & 0.28 & 0.22 & 0.32 & 0.27 \\
0.37 & 0.30 & 0.17 & 0.23 & 0.15 \\
0.08 & 0.07 & 0.11 & 0.05 & 0.12 \\
0.10 & 0.04 & 0.00 & 0.02 & 0.00 \\
\end{bmatrix}
\] (3)
Solution of Model

The value of each rank is as follows, 5, 4, 3, 2, and 1 for excellent, good, fine, qualified and poor respectively in the performance evaluation systems [7], the weight for each grade in the performance evaluation index, as follows:

\[
M = \frac{[m_1, m_2, m_3, m_4, m_5]}{m_1 + m_2 + m_3 + m_4 + m_5} = \frac{[5,4,3,2,1]}{5 + 4 + 3 + 2 + 1} = [0.33, 0.27, 0.20, 0.13, 0.07], \text{ that is, weight vector is } M = [0.33, 0.27, 0.20, 0.13, 0.07].
\]

Evaluation matrix is processed through linear transformation \( M_1 \), the result of linear transformation of School of Science as follows:

\[
B_1 = M_1 = \begin{bmatrix} 0.33 & 0.27 & 0.20 & 0.13 & 0.07 \end{bmatrix} \bullet \begin{bmatrix} 0.35 & 0.48 & 0.02 & 0.27 & 0.60 \\ 0.43 & 0.30 & 0.05 & 0.16 & 0.30 \\ 0.13 & 0.15 & 0.21 & 0.40 & 0.10 \\ 0.07 & 0.05 & 0.39 & 0.07 & 0.10 \\ 0.02 & 0.02 & 0.33 & 0.06 & 0.00 \end{bmatrix} = \begin{bmatrix} 0.27 & 0.28 & 0.14 & 0.23 & 0.31 \end{bmatrix}
\]

(4)

With the same method, the linear transformation results of evaluation matrixes of School of Economics and Management and Architectural and Civil Engineering School can be obtained as listed:

\[
B_2 = MA_2 = \begin{bmatrix} 0.25 & 0.17 & 0.24 & 0.27 \end{bmatrix} \\
B_3 = MA_3 = \begin{bmatrix} 0.23 & 0.25 & 0.43 & 0.27 \end{bmatrix}
\]

A transformed evaluation matrix can be developed on the basis of the results above:

\[
B = \begin{bmatrix} 0.27 & 0.25 & 0.23 \\ 0.28 & 0.17 & 0.25 \\ 0.14 & 0.21 & 0.43 \\ 0.23 & 0.24 & 0.27 \\ 0.31 & 0.27 & 0.26 \end{bmatrix}
\]

(5)

Assume that the weight of each evaluation index( five indexes) were \( N = [0.2 \ 0.1 \ 0.2 \ 0.2 \ 0.3] \), and then the comprehensive evaluation scores of three schools respective are

\[
C = NB = \begin{bmatrix} 0.27 & 0.25 & 0.23 \\ 0.28 & 0.17 & 0.25 \\ 0.14 & 0.21 & 0.43 \\ 0.23 & 0.24 & 0.27 \\ 0.31 & 0.27 & 0.26 \end{bmatrix} \bullet \begin{bmatrix} 0.2 \ & 0.1 & 0.2 & 0.2 & 0.3 \end{bmatrix} = \begin{bmatrix} 0.249 & 0.238 & 0.289 \end{bmatrix}
\]

(6)

Based on the evaluation matrix \( B \) and the weight of each evaluation index, the score of each evaluation index for three schools can be calculated as following method:

\[
D = B' \bullet \begin{bmatrix} 0.2 \\ 0.1 \\ 0.2 \\ 0.2 \\ 0.3 \end{bmatrix}
\]
$$\begin{bmatrix}
0.27 & 0.28 & 0.14 & 0.23 & 0.31 \\
0.25 & 0.17 & 0.21 & 0.24 & 0.27 \\
0.23 & 0.25 & 0.43 & 0.27 & 0.26
\end{bmatrix} \cdot 
\begin{bmatrix}
0.2 \\
0.1 \\
0.2 \\
0.3
\end{bmatrix} = 
\begin{bmatrix}
0.054 & 0.028 & 0.028 & 0.046 & 0.093 \\
0.050 & 0.017 & 0.042 & 0.048 & 0.081 \\
0.046 & 0.025 & 0.086 & 0.054 & 0.078
\end{bmatrix}$$ (7)

Analysis of Evaluation Result

In accordance with the calculating results, the scores of each index and the overall scores of three schools can be gained in the performance evaluation (Table 3).

<table>
<thead>
<tr>
<th>School</th>
<th>Duty performance</th>
<th>Coordination</th>
<th>Students administration</th>
<th>Faculty administration</th>
<th>Teaching management</th>
<th>Overall score</th>
</tr>
</thead>
<tbody>
<tr>
<td>School of Science</td>
<td>0.054</td>
<td>0.028</td>
<td>0.028</td>
<td>0.046</td>
<td>0.093</td>
<td>0.249</td>
</tr>
<tr>
<td>School of Economics and Management</td>
<td>0.050</td>
<td>0.017</td>
<td>0.042</td>
<td>0.048</td>
<td>0.081</td>
<td>0.238</td>
</tr>
<tr>
<td>Architectural and Civil Engineering School</td>
<td>0.046</td>
<td>0.025</td>
<td>0.086</td>
<td>0.054</td>
<td>0.078</td>
<td>0.289</td>
</tr>
</tbody>
</table>

From the data comparison in the table, the highest score in the comprehensive evaluation is obtained by Architectural and Civil Engineering School, School of Science ranking the second site. For the duty performance, coordination and teaching management, School of Science is better than the others. However, for the students’ administration and faculty administration, Architectural and Civil Engineering School performance better. For student training and employment, Architectural and Civil Engineering School present outstanding advantages than the others. Others aspects related to administration also can employ this method to evaluate.

Conclusion and Suggestion

This model is with strong reliability, able to be used into other positions and organizations. Colleges and universities should scientifically and reasonably adjust the weight of each relevant factor, making the evaluation system grow perfectly.

Comprehensive fuzzy evaluation is capable of evaluating and judging the person or matter that are influenced by multi-factor and multi-object [8]. It is able to objectively reflect the actual state of evaluation object, better for improve the evaluation criteria of performance evaluation in colleges and universities.

The evaluation system combines the qualitative indexes and quantitative indexes together, making up the defect produced by the simple combination of the qualitative indexes and quantitative indexes, improving the precision of comprehensive evaluation [9].

The reliability and precision of the comprehensive evaluation results count on the identification of rational factors, the weight allocation of factors and the composition operator of comprehensive evaluation and so on. Therefore, when the model is applied into the practice, the weight of each index ought to be adjusted according to the specific situation, making the evaluation much more objective, scientific and specific [10].
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References


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