Study on Energy Band-gap Calculation of CuGaS$_2$

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Abstract: CuGaS$_2$ as a ternary semiconductor with chalcopyrite structure has a direct bang-gap of 2.43 eV at room temperature corresponding to the wavelength of 0.51 $\mu$m, it is a promising absorption layer for photovoltaic material. In this work, convergence of the plane wave cut-off energy and the K-mesh were carried out based on first-principle of density functional theory, using VASP package. Lattice constants were optimized by convergence parameters, and the energy band-gap under generalized gradient approximation was calculated by setting convergence parameters and optimized lattice constants. The results indicate that CuGaS$_2$ has an energy band-gap of 0.784 eV. The calculating results play a guiding role in doping Ga to CuInS$_2$ to adjust energy band-gap.

Introduction

In recent years, application of ternary chalcopyrite semiconductors in solar cell technology has aroused great interest, especially in CuInS$_2$ and CuGaS$_2$. Both CuInS$_2$ and CuGaS$_2$ are semiconductors with a direct band-gap, the band-gap of CuInS$_2$ is 1.55 eV and band-gap of CuGaS$_2$ is 2.43eV [1-3].

First-principle calculations in the density functional theory, according to the principle of the atomic nucleus and electron interaction and the basic motion law, using quantum mechanics principle, basing on the specific requirements and a number of approximate treatment, it directly solves the Schrodinger equation to obtain the information of material structure and performance that we need [4].

Electronic structure and optical properties of CuGaS$_2$ have been widely studied by experts and scholars in recent years. S. Laksariet et al calculated the band-gap of CuGaS$_2$ as 0.903 eV using a hybrid full-potential linear augmented plane-wave pluslocal orbitals (L/APW+lo) method [5], taking the local density approximation (LDA) for the exchange-correlation potentials. Amit Soniet et al separately used the linear combination of atomic orbitals (LCAO) and FP-LAPW method [6], the band-gaps value of CuGaS$_2$ is 2.15 eV based on LCAO-GGA while that from FP-LAPW method is 0.86 eV. Bin Xu et al figured out the band-gap of CGS as 0.818 eV by using Wien2k package, based on method of FPAPW [7].

In this work, we used the generalized gradient approximation as the exchange-correlation and carried out the convergence of the plane wave cut-off energy and K-mesh of CuGaS$_2$ by using the VASP package [8]. The lattice constants of CuGaS$_2$ were optimized according to the convergence parameters, thus the band-gap of CuGaS$_2$ was calculated.

Construction model

It constructs the crystal cell model data taken from the ICSD database and reference [7], CuGaS$_2$ is a ternary compound with chalcopyrite structure, which belongs to tetragonal system, whose corresponding space group number is 122, I-42d. The lattice constants of CGS were selected as $a=b=5.35\text{Å}$, $c=10.47\text{Å}$, $\alpha=\beta=\gamma=90^\circ$. The corresponding crystal structure model was built in MS as shown in Fig.1.
Parameters convergence and band-gap calculation

Plane wave cut-off energy, K-mesh and lattice constants have effects on the calculation of the band-gap. So the convergence of the plane wave cut-off energy and K-mesh, and the optimization of the lattice constants were carried out firstly. After that, the band-gap of CuGaS$_2$ can be calculated.

Convergence of plane wave cut-off energy

The convergence of plane wave cut-off energy was carried out under PBE pseudo potential of the generalized gradient approximation. K-mesh of CuGaS$_2$ was chosen at $4 \times 4 \times 2$, $6 \times 6 \times 3$, $8 \times 8 \times 4$, $10 \times 10 \times 5$, $12 \times 12 \times 6$, then the parameters of plane wave cut-off energy were selected at 290 eV, 300 eV, 310 eV, 320 eV, 330 eV, 340 eV, 350 eV and 360 eV. Running the calculation script, after the completion of the calculation to check the result (the difference between two energy value is less than $10^{-3}$ eV), it is found that CuGaS$_2$ in the above K-mesh, all the convergence values are 340 eV. Plane wave cut-off energy convergence of CuGaS$_2$ which selected as $6 \times 6 \times 3$ of K-mesh was shown in Fig.2.

Convergence of K-mesh

K-mesh convergence of CuGaS$_2$ was also carried out under PBE pseudo potential of the generalized gradient approximation. In the convergence of plane wave cut-off energy, we measured the value of 340 eV, and then the K-mesh was selected at $4 \times 4 \times 2$, $6 \times 6 \times 3$, $8 \times 8 \times 4$, $10 \times 10 \times 5$, $12 \times 12 \times 6$. Running the calculation script, after the completion of the calculation to check the results (the difference between two energy value is less than $10^{-3}$ eV), when the plane wave cut-off energy of CuGaS$_2$ is 340 eV, the convergence of K-mesh is $4 \times 4 \times 2$. The convergence of K-mesh is shown in Fig.3. However, it exceeds the range of calculation when K-mesh of CuGaS$_2$ is chosen at $4 \times 4 \times 2$, so K-mesh of CuGaS$_2$ is chosen at $6 \times 6 \times 3$.

Optimization of lattice constants a and b

After the convergence of plane wave cut-off energy and K-mesh were completed, the lattice constants of CuGaS$_2$ need to be optimized. We fixed the position of atoms to optimize the lattice constants and volume of the unit cell. The optimization of lattice constant a (a=b) of CuGaS$_2$ is shown in Fig.4. By analysis, the lattice constant a (a=b) under the lowest energy value was 5.40Å.
After optimization of the lattice constants \(a\) and \(b\), we need to optimize the lattice constant \(c\). Fixing the position of atoms to optimize the lattice constant and volume of the unit cell. The optimization of lattice constant \(c\) is shown in Fig. 5. After analysis, the lattice constant \(c\) under the lowest energy value was 10.47Å.

**Calculated of band-gap**

The band-gap of CuGaS\(_2\) is calculated using VASP package, we need four files including INCAR, KPOINTS, POSCAR, POTCAR. In which the INCAR and KPOINTS parameters convergence have been completed, POSCAR file provides the atomic information and atomic positions that derived from the crystal model after optimizing the lattice constants, POTCAR is the pseudo potential file, which chooses the PBE pseudo potential of the generalized gradient approximation for calculation. Firstly, we carried out a static self-consistent calculation to get the correct charge density, then modified parameters to calculate band-gap. Here in the KPOINTS file we select the high symmetry point of the Brillouin zone, in this paper, \(Z, A, M, G, Z, R, X, G\) [9] were selected as high symmetry point through calculate and analysis, the energy band-gap diagram...
of the CGS is obtained as shown in Fig.6 [10]. It can be seen from Fig.6, the top of the valence bands and the bottom of the conduction bands lie along the Gamma indicating that CuGaS$_2$ is a direct band-gap semiconductor, and band-gap is 0.784 eV, which has difference with the theoretical values. The calculated values are affected by lattice constants selection of pseudo potential and selection of exchange-correlation.

![Fig. 6 Energy band diagram of CuGaS$_2$](image)

Conclusions

The band-gap of CuGaS$_2$ was calculated based on first-principle of density functional theory, using VASP package. Through the convergence, the plane wave cut-off energy could be determined to be 340 eV, and K-mesh was 6×6×3. The optimized lattice constant a (a=b) was 5.40Å and c was 10.47Å. And then calculation of the CuGaS$_2$ band-gap was carried out. It is shown that CuGaS$_2$ is a direct band-gap semiconductor material and the band-gap is 0.784 eV. The calculating results of CuGaS$_2$ energy band-gap play a guiding role in doping Ga to CuInS$_2$ to adjust energy band-gap.

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References


