A reliability-based approach of fastest routes planning in dynamic traffic network under emergency management situation

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ABSTRACT

In order to establish an available emergency management system, it is important to conduct effective evacuation with reliable and real time optimal route plans. This paper aims at creating a route finding strategy by considering the time dependent factors as well as uncertainties that may be encountered during the emergency management system. To combine dynamic features with the level of reliability in the process of fastest route planning, the speed distribution of typical intercity roads is studied in depth, and the strategy of modifying real time speed to a more reliable value based on speed distribution is proposed. Two algorithms of route planning have been developed to find three optimal routes with the shortest travel time and the reliability of 0.9. In order to validate the new strategy, experimental implementation of the route planning method is conducted based on road speed information acquired by field study. The results show that the proposed strategy might provide more reliable routes in dynamic traffic networks by conservatively treating roads with large speed discretion or with relative extreme real speed value

Key words: algorithm; reliability of route; modified real time speed; depth first search strategy

1. Introduction

Man-made or natural disasters, whether predictable or not, always pose a threat to public safety as well as people’s lives and possessions, thus triggering prolonged public concern and heated discussions among researchers and administrators. Many strategies, both empirical and theoretical, have been put forward to mitigate the calamitous consequences that may be caused by the disasters, and researches in the field of transportation play a significant role in exploring effective ways to alleviate the impact of emergencies. Evacuation is a common strategy in emergency management, where the key issue is the proper way to organize different aid agencies and the relocation of the general public. In the realm of transportation, existing evacuation research has been mostly focused on planning stage, such as research on traffic management policies and origin-destination estimation. Additionally, models designed for various emergency cases have been developed to deal with disparate evacuation scenarios, among which the research of Southworth, Urbina and Wolshon, and Alsnih and Stopher are highly recommended. Transportation systems are always dynamic, which should not be neglected by scientists and people working in related fields. It is generally acknowledged that even in normal situations, the estimation of traffic flow could hardly be accurate, let alone in accidents and emergencies.

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Analyzing and predicting traffic flow based on the concept of dynamic traffic features and uncertain factors are to some extent the most crucial and challenging components in the exploration of emergency management, and failure to do so is always can result in loss of lives as well as public wealth. However, the history of the study of dynamic network is not long. Barrett et al. proposed their study of evacuation management based on real-time dynamic features in 2000, but the solutions and model they proposed are actually based on strategies and techniques which cannot sufficiently satisfy the demand of real dynamic system. Liu et al. proposed a MRAC framework for real-time traffic management, with a prediction model to generate desired traffic states to achieve optimized system objectives, a real-world traffic model to simulate actual evacuation traffic flows, and an adaptive control model to produce actual traffic control schemes. Liu’s work contributed significantly to the improvement of traffic system, but it didn’t take sufficient account of the complexity of real traffic network and the uncertainty during the evacuation procedure.

It is also important to note that the development and realization of the proposed strategies and solution frameworks so far are on a large scale decided by the details contained inside the models. It is fundamental that the crucial steps in the whole evacuation procedure should be taken into consideration and can proceed smoothly when designing the models and frameworks. A great deal of innovative research work has been done to achieve this objective. For instance, a network flow model for lane-based evacuation routing was proposed by Cova, which aimed at alleviating traffic delays in evacuation that occurred frequently at intersections. And undoubtedly, searching for the best route is of crucial significance in conducting aid commands efficiently during evacuation procedure, therefore, the development and improvement of optimal route searching algorithm has become a hot research topic in the field of transportation.

Finding the shortest route system is one of the most fundamental and frequently encountered problems in route planning researches, and numerous algorithms are commonly studied and utilized. Dijkstra algorithm is a classical optimal Label-Setting algorithm to solve the one-to-one shortest route problem in a static traffic network. In 1968, Hart proposed the A* algorithm structured on heuristic function which guides the search towards the destination node, thus contributing a great deal to the improvement on searching efficiency. Depth-first search is a general technique used in Artificial Intelligence for solving a variety of problems in planning, decision making, theorem proving, expert systems, etc. And it can examine all the possible routes from an initial node to the destination in a given area with very little memory requirement. Another widely utilized algorithm is ant colony algorithm initially proposed in 1992 by Marco Dorigoin in his PhD thesis. Inspired by at behavior, the optimization strategy and technique is applied to various field including vehicle routing. However, basic algorithms and route planning strategies are not sufficient for real problems, to tackle the problem commonly confronted due to the dynamic features of real transportation system, algorithms with the capacity to deal with dynamic network are in great demand. Chabini extended the A* methodology to the shortest route problems in dynamic networks, in which arc travel times are time dependent. And Fu introduced a new route planning algorithm in dynamic network and restricted areas, and argued that path-planning algorithm should aim at the fastest path, which means the path with the least travel time, in order to take into consideration the actual condition of a real road.

The concept of fastest path in dynamic network is practical, and paves the way for a more direct strategy to analyze optimal path problem. But it is essential to consider uncertainty that exists in the whole process of evacuation process. Even though we can acquire the most current data of traffic flow and the condition of each road we are tracing, we should be aware of the fact that the information we acquire may not be completely reliable, and would change in some way to fit in its own inner regularities. Consequently, we need to examine carefully before the utilization of the currently available figures and resources.

With this understanding, the main objectives of this paper are to develop a new strategy to find three fastest routes from one origin to one destination in a dynamic system, which takes into account the level of reliability of the current data of roads we obtain. The research is set in the background of emergency management procedure, where various aid agencies need the information of reliable fastest route in order to arrive at the incident site as soon as possible. Three paths are searched in this strategy to provide aid agencies with different choices, and enable separate teams from the same origin to perform their tasks.
simultaneously. This paper is structured as follows: the next section presents basic introductions of spot study and speed frequency distributions of typical intercity roads, which is followed by the mathematical model presented to simulate the speed distribution. In section 3, approaching of optimal routes planning is discussed, and two algorithms in the strategy are discussed in detail. After that experimental implementations of the new strategy is conducted based on simulated map of the district selected and statistical data acquired by field study. Finally, some concluding remarks and future work are summarized in brief.

2 Spot speed studies and frequency distribution curve

2.1 Using the normal distribution in analysis of spot speed data

Spot speed has been previously defined as the average speed of vehicles passing a point on a highway. When the speeds of individual vehicles are measured at a given spot or location, the result is a distribution of speeds, as no two vehicles will be travelling at exactly the same speed. Therefore, one of the basic objectives of spot speed study is to clearly describe the distribution of speed, and to determine an adequate mathematical model to analyze the observed distribution.

In a field study, large amounts of samples are collected, and the number of individual vehicles travelling at particular ranges of speed is recorded. Speed data is generally presented as the frequency of occurrence within predetermined ranges of speed, and mathematical descriptions of the distribution are proposed. Most speed distributions are statistically normal (i.e., they can be reasonably represented by a normal distribution), and some other distributions can be described using models modified on the basis of a normal distribution.

In order to use a normal distribution to represent the observed distribution of speed data, some key statistics should be determined, among which the most decisive are the mean and the standard deviation of the distributed speed values, represented by \( \mu \) and \( \sigma \) respectively. In practical terms, the true value, \( \mu \) and \( \sigma \), are unknown. What results from a spot speed study are estimates of true mean and standard deviation of the distribution based on a measured sample, \( s \) and \( \bar{x} \):

\[
\bar{x} = \frac{\sum n_i S_i}{N}, \quad s = \sqrt{\frac{\sum n_i (S_i - \bar{x})^2}{N - 1}}
\]

where \( n_i \) is the frequency of observations in speed group \( i \), \( S_i \) is the middle speed of speed group \( i \), and \( N \) is the total sample size.

It is vital to note that the sample size is of significance importance to the precision of the estimation. Given that the precision or tolerance (\( e \)) of the estimate is the \( \pm \) range around the real mean, and a confidence level of 99.7% is required (i.e. the possibility of \( X \) in the range of \( \mu \pm e \) is 99.7%), the required sample size \( N \) can be calculated by equation below:

\[
e = 3.00 \frac{s}{\sqrt{N}}
\]

Most observed speed distributions have standard deviations that are close to 5, as this represents most driver behavior patterns reasonably well. As a consequence, most field studies yield similar standard deviations (Roger, 2004).

2.2 Conservative planning with 10th percentile speed

Once the mathematical models of spot speed data acquired in a normal condition are established, they can be stored by traffic management authorities to describe common properties of the paths where observation spots are set. Speed distribution model of a particular spot is representative of speed distribution of the path where the spot lies in an intercity network, since intersections are relatively close to each other, and speeds of vehicles on most spots along one path are approximately similar during a small period of time. Admittedly, at intersections speed will fluctuate due to traffic control devices such as traffic lights, but it can be mitigated in a huge traffic network, where influences of various intersections could be neutralized by each other.

Although estimated mean value of speed distribution is universally used in assessments of road conditions, it is unsafe to draw the conclusion that the speed of vehicles on the road will stably stay in a range near the estimated mean value. In order to conservatively estimate the condition of a road, a 10th percentile speed is proposed. On a particular road, only 10 percent of vehicles run at a speed smaller than 10th percentile speed of the road (Fig. 1.).
Suppose the frequency distribution function of the speed of a road during a particular time period is $f(x)$, 10th percentile speed ($v_{10}$) is acquired by integration below:

$$\int_{-\infty}^{v_{10}} f(x)dx = 0.1$$  \hspace{1cm} (3)

For a road with a given length ($d$) in a traffic network, when $v_{10}$ is calculated, the 90th percentile travel time ($t_{90}$) can be determined as follow:

$$t_{90} = \frac{d}{v_{10}}$$  \hspace{1cm} (4)

which means that 90 percent of the vehicles can pass the road within the 90th percentile travel time.

The introduction of $v_{10}$ and $t_{90}$ enables us to make route planning in a more conservative way, and optimal route searching algorithm will be more conscious when dealing with paths whose speed distribution are relatively disparate. To distinguish algorithms that use $v_{10}$ and $t_{90}$ in their computing procedure and tradition algorithms, we name the latter ‘algorithms with the reliability of 90 percent’. It is necessary to stress that 90 percent is not a fixed value in the concept of conservative planning, and we can adjust the percentage based on the level of confidence we demand. The more reliability we want, the smaller percentage speed value we assign and utilized in the route planning algorithms.

### 3 Strategy of reliable optimal route planning in a dynamic network

#### 3.1 Fastest path finding algorithm with reliability of 90 percent

This algorithm—we can name it G algorithm for convenience—aims at finding 10 routes with the least length of travel time and reliability of 90 percent in a traffic network based on the average velocity of each road in the network in particular time periods, which is static data resource stored in the database of traffic management authorities. When emergencies are reported, emergency management system could instantly present 10 routes with reliability of ninety percent, which could be conducted in a rapid speed and be realized before the expansion of negative influences caused by emergencies. G algorithm is a modified DFS with concepts of time cost generated from A* algorithm, which is presented in detail as bellow.

In A* algorithm, a cost function is defined as:

$$\hat{F}_q = T_q + \hat{e}_{qD}$$  \hspace{1cm} (5)

where $q$ is the current expending node (current Node), $\hat{F}_q$ is the estimation of the minimum travel cost among all the paths from origin node $O$ to destination node $D$ that go through $q$, $\hat{T}_q$ is the upper bound on the minimum travel cost from origin node $O$ to node $q$, $\hat{e}_{qD}$ is the estimation of the minimum travel cost from node $q$ to destination node $D$.

In order to find out routes with the least travel time, we modify the cost function, which could be presented as follow, measured by the length of time:

$$\tilde{F}_q = \tilde{T}_q + \hat{e}_{qD}$$  \hspace{1cm} (6)

In this function, $\tilde{F}_q$ is the estimation of the minimum travel time among all the paths from origin node $O$ to destination node $D$ that go through $q$, $\tilde{T}_q$ is the travel time (timeCost) with reliability of 90% of current route generated from origin node $O$ to node $q$,

$$\tilde{T}_q = \sum_{i=0}^{q-1} \frac{d_{i,i+1}}{v_{i,i+1}}$$  \hspace{1cm} (7)

where $d_{i,i+1}$ is the Euclidean distance between node $i$ and node $i+1$ on the route connecting origin point O and node q, and $v_{i,i+1}$ is the average velocity on the road whose endpoints are node $i$ and node $i+1$ respectively.

$\hat{e}_{qD}$ is defined as the minimum possible travel time (minTimeCost), which is determined as

$$\hat{e}_{qD} = \frac{d_{qD}}{v_{10,\text{max}}}$$  \hspace{1cm} (8)

where $d_{qD}$ is the Euclidean distance between node $j$ and node $D$, and $v_{10,\text{max}}$ is the maximum value of average velocity with reliability of 90% among all the roads in the traffic network.
In the depth-first search in $G$ algorithm, the search begins by expanding the initial node (origin node $O$), and at each later step, one of the previously generated node is expanded until the destination node $D$ is found, and nodes generated by the expansion of currentNode is called nextNode. In the searching procedure, DFS use $F_q$ to assess the possibility that a particular node will be on the optimal route by comparing the value of $F_q$ to the calculated time cost ($T_{in}$ for route $i$) of the found routes stored in a set named $PATH$, which is on the basis of the concept of heuristic search. The process $G$ algorithm takes to find the fastest path could be described as pseudo-code below:

Initialization: visited[originNode] = true; currentPath[0] = originNode; searchedDepth = 0;
void DFS(int currentNode) {
  if ( timeCost(currentPath) + minTimeCost(currentNode, destinationNode) > max\{timeCost(PATH) \} ) {
    return;
  }
  if ( currentNode == destinationNode ) {
    if ( number of paths in PATH < 10 or timeCost(currentPath) > max\{timeCost(paths in PATH) \} ) {
      if ( number of paths in PATH < 10 ) {
        copy currentPath into PATH;
      }
      else {
        replace the most time-consuming path in PATH with currentPath;
      }
    }
    return;
  }
  for ( every sibling ‘nextNode’ of currentNode ) {
    if ( nextNode is farther from destinationNode than currentNode and so does the last expansion) {
      // We are very probably in a wrong direction, so drop it
      drop this ‘nextNode’, and turn to the next sibling of currentNode;
    }
    else {
      searchedDepth++;
      currentPath[searchedDeapth] = nextNode; 
      visited[nextNode] = true;
      DFS( nextNode );
      visited[nextNode] = false;
      searchedDepth--;
    }
  }
}

$G$ algorithm is a heuristic algorithm that instructs the system to search the optimal routes in a more efficient way. Since it is required that 10 paths be selected out, the searching procedure becomes more complex than traditional optimal route finding algorithms. To decrease time consumed in computing process, a set of routes named $PATH$ is proposed to store the found routes with relatively small travel time (time cost), which enable the system to give up a particular node $j$ reached from the expansion when $F_j \geq \max\{T_{in}, \forall path \in PATH\}$, thus enhancing the speed when searching for solutions. Meanwhile, it is also of significant importance to point out that the reliability all the paths founded by $G$ algorithm can be guaranteed. We use $v_{in}$ to calculate the length of time, which ensures that for each small block between the intersections, the possibility of real travel time longer than calculated value in $G$ algorithm is only 10%.

### 3.2 Selection of the fastest route based on the modification of current speed value

When 10 routes are found by $G$ algorithm based on the stored data and mathematical model, the paths that aid agencies will probably go along are simultaneously determined. Real time average speed data of these potential paths is acquired by devices that trace the dynamic status of traffic flow, and three optimal routes are then found on the basis of the real time data, and the strategy used to complete this task is named $F$ algorithm in this paper. This step uses real time average speed to determine the optimal routes, which enables the emergency management system to integrate time dependent factors into the properties of the roads which are acquired using statistic strategies in a dynamic traffic network.

It is generally acknowledged that even though we have access to the data of real time average speed, we cannot precisely predict how the figures will change by the flow of time, and it is unlikely that we update data every single
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Consequently, when a real time average speed value is acquired, we should again consider its reliability based on the frequency distribution function and modify the value before applying it to route planning algorithm.

In this paper, we discuss algorithms that modify real time speed values of roads with normal speed distribution and double-peak speed frequency distribution which can be simulated by the superimposition of two normal distribution functions.

Fig. 2. is the bar chart of the speed distribution of a typical road in Beijing from 12PM to 2AM.

Considering the situation when the value of real time average speed is bigger than the estimated mean speed value, the possibility that the speed will drop to a smaller value cannot be ruled out, and it will be more conservative to modify the acquired value downward. Similarly, if we find the real time value smaller than mean value, it is reasonable that we modify it to a bigger value. However, it should also be considered that if the value of real time average speed is so small that it exceeds a tolerance range, it is of all likelihood that the road is suffering from heavy traffic congestion. As a result, we should rule out this road when determining the optimal routes.

The foregoing concept can be realized by a modification function that defines the relationship between real time average speed \( v_r \) and the modified value \( v_m \). In order to satisfy the objectives of modification presented above, let

1) \( v_m = f(v_r) = v_r \), when \( v_r = E \), where \( E \) is the mean speed value.

Let \( v_m < v_r \), when \( v_r > E \), and \( v_m > v_r \), when \( v_r < E \)

2) \( v_m = f(v_r) = v_r \), when \( v_r = E-1.645\sigma \)

Let \( v_m > v_r \), when \( v_r > E-1.645\sigma \).

And when \( v_r < E-1.645\sigma \) (the probability is only 5%), let \( v_m < v_r \), which makes the road unlikely to be selected.

A quadratic function is introduced to describe the relationship between \( v_r \) and \( v_m \):

\[
v_r = Av_r^2 + Bv_r + C
\]

(9)

To simplify the function, let \( B = 0 \), \( A \) and \( C \) can be determined by 1) and 2) stated above. Given the normal distribution model determined by figures in Fig.2., the function curve of \( f(v_r) \) is presented in Fig.3., where \( A = 8.32 \times 10^{-3}, C = 29.83 \).

Fig.4. is the bar chart of the speed distribution of a typical road in Beijing from 6AM to 8AM in October, 2007 (Li, 2007), which can be simulated as two normal distribution models. And the frequency distribution function is presented as below:

\[
f(x) = \lambda \frac{1}{2\pi\sigma_1} e^{-\frac{(x-E_1)^2}{2\sigma_1^2}} + (1-\lambda) \frac{1}{2\pi\sigma_2} e^{-\frac{(x-E_2)^2}{2\sigma_2^2}} , 0 < \lambda < 1
\]

(10)

where \( E_1, E_2 \) are the mean values of the two normal distribution models, and \( \sigma_1, \sigma_2 \) are the standard deviations. It is essential to judge if the two normal distribution models are dependent before defining the modification function.
A reliability-based approach

1) If \( E_1 + \beta \sigma_1 \leq E_2 - \beta \sigma_2 \)

Let \( \beta = 0.84 \), which ensures that the two normal distribution models can be treated as independent. In order to be more conservative, we determine \( v_m \) by the equation below:

\[
22 \min\{ A_1 v_m^2 + C_1, A_2 v_m^2 + C_2 \} \quad (11)
\]

where \( A_1, A_2, C_1, C_2 \) are the coefficients determined by the two dependent normal distributions models.

2) If \( E_1 + \beta \sigma_1 > E_2 - \beta \sigma_2 \)

In this situation, the two normal distribution models are mixed on a relatively large scale, thus cannot be simulated as two independent peaks. We conservatively select the smaller value of determined by two normal distribution models, and if we choose the smaller value when modifying speed value of all the observed roads in the network, it is evident that the error can be mitigated. Thus, \( v_m \) is calculated by the equation below:

\[
22 \max\{ A_1 v_m^2 + C_1, A_2 v_m^2 + C_2 \} \quad (12)
\]

where \( A_1, A_2, C_1, C_2 \) are the coefficients determined by the two dependent normal distributions models.

Fig. 4. Speed distribution of a typical road in Beijing from 6AM to 8AM

Fig. 5. (left) is the function curves of modified speed based on the data provided in Fig.4, before superimposition, and Fig.5. (right) shows the superimposed curves. In this model, \( A_1=8.32 \times 10^{-3}, \quad C_1=29.83, \quad A_2=0.031, \quad C_2=7.601 \). Function curves of \( v_m = v_r \) is also illustrated as a reference of the situation before modification.

When modified speeds of all the potential roads are selected, estimated time cost \( (t_e) \) of each route is calculated as bellow:

\[
t_e = \sum_{i} \frac{d_i}{v_{m,i}} \quad (13)
\]

where \( d_i \) is the distance road \( i \) in the found route provided in G algorithm, which can be regarded as the Euclidean distance between two nearby intersections in a traffic network, and \( v_{m,i} \) is the modified speed of road \( i \).

Based on \( t_e \), emergency management systems can select 3 routes with the shortest travel time among the 10 routes acquired in the previous step, and immediately provide aid agencies with the route information.

4. An experimental study of computer implication based on a real traffic network

4.1 District selected in the experimental study and introduction to the implementation system.

G algorithm and F algorithm discussed in the previous section have been implemented for the purpose of computational test, and traditional DFS strategy using estimated mean speed value is applied as a comparison to the proposed algorithms. To conduct the experimental study, an intercity traffic network in Beijing is selected.
and the map is simulated in AutoCAD. The selected area is
the neighborhood of the Workers Stadium, which is to the
north of Chang’an Avenue, between the east second and
third ring roads, with the total area of 16.92km². The area
selected is typical in downtown Beijing, which ensures
that the transport characteristics of roads in this area are
among the average level, and consequently could be
estimated based on the representative data of road
characteristics in Beijing. Meanwhile, since many public
activities are held in the Workers Stadium, study of route
planning for emergency management is more useful and
practical considering the fact that there is a higher
possibility that emergencies will happen in the area near
the Workers Stadium.

The simulated map is illustrated in Fig.6. Lines with the
largest width stand for expressways whose average speed
is usually the fastest among other kinds of roads on this
map, and lines with medium width represent trunk roads.
Correspondingly, lines with the smallest width stand for
sub-trunk roads with relatively lowest average speed
among roads showed on the map. As for aid agencies,
three most typical agencies are selected to simulate the
real situation. The circle, triangle and rhombus stand for
fire agency, police station and hospital respectively, which
are marked on the map. In the implementation system,
emergency spot is generated randomly, and is marked by a
star shape sign.

The speed information of expressways, trunk roads and
sub-trunk roads are acquired by a field study conducted in
October, 2007 by a group of transportation research
agency in Tsinghua University (Li, 2007). The field study
investigated speed of all vehicles that passed through
Yuetan North Bridge and Fuchengmen Bridge, and
simulated the distributions of vehicle speed on
expressways, trunk roads and sub trunk roads during the
twelve periods of a day, which is presented in Table 1. The
results are typical for districts between second and third
ring roads in the north part of Beijing.

![Simulated map of selected district in experimental implementation.](image)

**Table 1. Distributions of vehicle speed on expressways, trunk roads and sub trunk roads**

<table>
<thead>
<tr>
<th>Time period</th>
<th>Expressway</th>
<th>Trunk road</th>
<th>Sub-trunk road</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>E1 (12PM-2AM)</td>
<td>E2 (2AM-4AM)</td>
<td>E1 (4AM-6AM)</td>
</tr>
<tr>
<td>12PM-2AM</td>
<td>65 6</td>
<td>45 6</td>
<td>35 6</td>
</tr>
<tr>
<td>2AM-4AM</td>
<td>70 3</td>
<td>50 3</td>
<td>40 3</td>
</tr>
<tr>
<td>4AM-6AM</td>
<td>55 5.5</td>
<td>45 5.5</td>
<td>30 5.5</td>
</tr>
<tr>
<td>6AM-8AM</td>
<td>30 6</td>
<td>30 6</td>
<td>20 6</td>
</tr>
<tr>
<td>8AM-10AM</td>
<td>70 7</td>
<td>30 7</td>
<td>20 7</td>
</tr>
<tr>
<td>10AM-12AM</td>
<td>25 7</td>
<td>25 7</td>
<td>25 7</td>
</tr>
<tr>
<td>12AM-2PM</td>
<td>30 7</td>
<td>30 7</td>
<td>20 7</td>
</tr>
<tr>
<td>2PM-4PM</td>
<td>20 6</td>
<td>20 6</td>
<td>20 6</td>
</tr>
<tr>
<td>4PM-6PM</td>
<td>20 8</td>
<td>20 8</td>
<td>20 8</td>
</tr>
<tr>
<td>6PM-8PM</td>
<td>30 6</td>
<td>30 6</td>
<td>30 6</td>
</tr>
<tr>
<td>8PM-10PM</td>
<td>80 9</td>
<td>60 9</td>
<td>50 9</td>
</tr>
</tbody>
</table>
The implementation system is written in C++ based on MFC (Microsoft Foundation Classes), which is structured by three layers: data layer, logic layer and display layer. The data layer reads information from the map, and transforms it into data that can be recognized by the system. 10th percentile speed ($v_{10}$) and real speed ($v_r$) information of different roads is written in speed.txt and realspeed.txt respectively, which are read by data layer during the path planning procedure. The logic layer realizes the processes of G algorithm and F algorithm. Finally, optimal routes are presented on the map by the display layer. Meanwhile, when the routes are found (both the ten routes acquired by G algorithm and the three routes selected by F algorithm), the system will automatically generate a text file reporting the nodes along the routes as well as the travel time of each route.

As shown in Table 1.1, the level of discretion is the same for the three different kinds of road ($\sigma$ equals). Consequently, when considering the 10th percentile speed, the disparity of the three speed values corresponds with the mean speed. Since the traffic situation is relatively stable, $v_r$ is close to the mean value. As a result, the modified speed values approximately equal to the acquired real speed. In this situation, the found optimal routes (Fig.7.) are almost the same as those found by traditional DFS using $v_{50}$ (Fig.6.). The nodes that the three found route go through are listed in Table 1.2, which also presents the Path Cost. In this and the following two examples, Route1, Route2 and Route3 are listed by the order of their Time Cost, from the smallest to the largest, and Route0 is the route found by traditional DFS.

<table>
<thead>
<tr>
<th>12PM-2AM</th>
<th>Expressway</th>
<th>Trunk road</th>
<th>Sub-trunk road</th>
</tr>
</thead>
<tbody>
<tr>
<td>$v_{50}$</td>
<td>65</td>
<td>45</td>
<td>35</td>
</tr>
<tr>
<td>$v_{10}$</td>
<td>52.284</td>
<td>37.284</td>
<td>27.284</td>
</tr>
<tr>
<td>$v_r$</td>
<td>64.75</td>
<td>45.12</td>
<td>34.94</td>
</tr>
<tr>
<td>$v_m$</td>
<td>64.77</td>
<td>45.11</td>
<td>34.95</td>
</tr>
</tbody>
</table>

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4.2.2 Experiments of the routes finding considering roads with discrete speed distribution.

This experiment is set under a situation when one particular type of road has discrete speed discretion. Consider the traffic network during peak hours (4PM-6PM) in the afternoon, when three types of roads are in a relatively ultra saturated condition. An emergency happened on the block in the south east part of the selected area, and ambulances are in urgent demand, which calls for immediate route planning from emergency spot to the hospital. At this time, situation on expressways is a complexity, where vehicles’ speed fluctuates in a considerable range. Speed information in this example is shown in Table 2.1.

Table 2.1. Speed information in experiment 2

<table>
<thead>
<tr>
<th>Time</th>
<th>Expressway</th>
<th>Trunk road</th>
<th>Sub-trunk road</th>
</tr>
</thead>
<tbody>
<tr>
<td>50</td>
<td>21.91</td>
<td>20</td>
<td>20</td>
</tr>
<tr>
<td>v_{10}</td>
<td>10.80</td>
<td>13.58</td>
<td>13.58</td>
</tr>
<tr>
<td>v_r</td>
<td>23.00</td>
<td>21.12</td>
<td>22.87</td>
</tr>
<tr>
<td>v_m</td>
<td>21.92</td>
<td>22.03</td>
<td>22.16</td>
</tr>
</tbody>
</table>

As shown in Table 2.1, from 4pm to 6pm, the frequency distribution of average speed on expressways is discrete, which can be simulated by the model of two independent normal distributions. We can infer from the value of 10th percentile speed that conservatively thinking, expressways are not the priority for optimal path planning since their average speed may easily drop to the lowest value. The experiment results are shown in Fig.9. and Table 2.2, as compared to route found by traditional DFS (Fig.8.), it is illustrated that expressways are on a large scale avoided. It may sound beyond common sense when the results are acquired, but it reasonably accounts for uncertainties in the dynamic traffic network, and presents more reliable routes for the aid agencies.

Table 2.2. Nodes that the three found route go through in experiment 2

<table>
<thead>
<tr>
<th>Route</th>
<th>Nodes</th>
<th>PathCost</th>
</tr>
</thead>
<tbody>
<tr>
<td>Route1</td>
<td>362 363 365 366 40 25 39 353 354 296 295 299 298 301 300 357 174.156</td>
<td></td>
</tr>
<tr>
<td>Route0</td>
<td>362 363 365 366 40 25 24 26 27 28 29 30 31 32 33 20 54 53 52 51 50 166.82</td>
<td></td>
</tr>
</tbody>
</table>

Fig. 8. Route found by traditional DFS in experiment 2.

Fig. 9. Route found by G algorithm and F algorithm in experiment 2.
4.2.3 Experiments of the routes finding with acquired real speed of extreme value.

This experiment is set under a situation when the real speed value acquired of one particular type of road is extremely large or small. Based on the frequency distribution function of a road, we can easily find out the proportion of situations when the average vehicle speed on this road is smaller or larger than the real time value, thus determining if the lately obtained value is sufficiently reliable. If a real time speed data acquired is too optimistic or pessimistic, it is highly recommended that we modify the value to a more eclectic value, which makes the obtained value safer to utilize. Consider the traffic network during early hours of the day (4AM-6AM) in the morning, when an accident happened and the police station received the command to reach the accident spot as soon as possible. When obtained real time traffic information shows that the vehicles on a particular trunk road are currently running at an extremely high speed, we should not neglect the fact that this situation may not remain stable in a dynamic network.

The speed information is shown in Table 3.1, and results of generated routes are presented in Table 3.2 and Fig.11.

<table>
<thead>
<tr>
<th>Time</th>
<th>Expressway</th>
<th>Trunk road</th>
<th>Sub-trunk road</th>
</tr>
</thead>
<tbody>
<tr>
<td>v50</td>
<td>55</td>
<td>45</td>
<td>30</td>
</tr>
<tr>
<td>v10</td>
<td>47.93</td>
<td>37.93</td>
<td>22.93</td>
</tr>
<tr>
<td>v_r</td>
<td>55.20</td>
<td>55.32</td>
<td>34.74</td>
</tr>
<tr>
<td>v_m</td>
<td>55.18</td>
<td>53.50</td>
<td>33.78</td>
</tr>
</tbody>
</table>

It is shown in the results that not all the paths selected from east to west are trunk roads whose real speed value is extremely high (approximately 97th percentile speed). Besides route found by traditional DFS (Figure 10), the found optimal route of the new strategy with the smallest Time Cost is formed still mainly by expressways, whose high real speed value is more reliable when considering the dynamic feature of the traffic network. When referring to the modified speed, it is important to see that the modified speed value of trunk roads is smaller (53.50km/h) than that of expressways (55.18km/h), although the reverse is true for real speed value.

<table>
<thead>
<tr>
<th>Nodes</th>
<th>PathCost</th>
</tr>
</thead>
<tbody>
<tr>
<td>Route1</td>
<td>262 32 31 30 29 28 2 1</td>
</tr>
<tr>
<td>Route2</td>
<td>262 264 263 106 28 2 1</td>
</tr>
<tr>
<td>Route3</td>
<td>262 264 31 30 29 28 2 1</td>
</tr>
<tr>
<td>Route0</td>
<td>262 32 31 30 29 28 2 1</td>
</tr>
</tbody>
</table>

Fig.10. Route found by traditional DFS in experiment 3

Table 3.2. Nodes that the three found route go through in experiment 3

![Fig.11. Route found by G algorithm and F algorithm in experiment 3](image-url)
## 5. Concluding remarks and future work

Dynamic features of traffic network have long been the focus of research concern, and uncertain factors are essential issues that cannot be neglected in route planning strategies, especially when an emergency happens. This paper has proposed a strategy that simultaneously takes into account the dynamic characteristics and the level reliability for optimal route finding against the background of emergency management. Definitions or routes with reliability of 90 percent as well as a recommended mathematical model simulating speed distribution are first presented. In this process, G algorithm is introduced to determine 10 optimal routes with reliability of 90 percent, and F algorithm is utilized to select 3 routes from the 10 found routes based on the obtained real time speed values. The reliability of speed value and the modification of real time value are determined fundamentally by the speed frequency distribution models of various roads, which are established on the basis of the statistical data obtained by field studies. Meanwhile, experimental implementation of the route planning strategy is conducted, with regarding to three disparate set situations. It is shown in the results that under normal situations, routes found by the new strategy are approximately similar to that found by traditional DFS algorithms. However, the new strategy is more conservative when calculating the time cost of routes with discrete speed distributions and with extreme low or high real time speed values, thus guaranteeing the level of reliability. The strategy is presented in this paper with the level of reliability of 90 percent. It is essential to note that the level is not supposed to be fixed, and it can be determined based on real demands.

This paper has presented a concept of modified speed value in order to take into account the uncertainties that may be encountered during the emergency management procedure. The modification function is established based on several empirical concepts presented in 3.3, which indicates that improvements can be made by studying and simulating the regulations of speed changes with disparate lengths of time, and presenting a more adequate and precise modification function. Meanwhile, in the experimental implementation system, simplifications are made to acquire a fast calculation speed, but it is evident that speed information of the same types of roads cannot be exactly the same. Consequently, more complex situations should be considered, and speed information of each road should be distinguished and used separately to validate the strategy. Additionally, the route planning strategy in this paper didn’t account for traffic flow on intersections that can actually exert substantial influence on the time cost calculated in the algorithms, and future work should investigate the feature of intersections and combine them with dynamic and uncertain factors as well.

## References

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