

# A Hybrid TD-AD Algorithm Based Electromagnetic Spectrum Assignment Method

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**Abstract**—The object of spectrum assignment is to build its own ordered spectrum environment and maintain uninterruptedly spectrum resource control. In this article, we build a mathematical model and put forward the hybrid TD (table dispatching method) and the AD (auxiliary decision method) algorithm. The results show that this method is contributed to minimize the allocation time, reduce the technical background demand and improve the decision veracity.

**Keywords**—spectrum assignment; auxiliary decision; optimization allocation

## I. INTRODUCTION

It is a paradox in the area of wireless communication that total frequency spectrum available has been exhaust while much of them have been fairly underutilized [1]. But to the best of our knowledge, there exist only a few literatures— which focused on spectrum decision, among which few take both of short-term and long-term information into consideration. Nowadays, due to the booming informationized weapon industry and the comprehensive strengthen of equipment informationization, the spectrum environment of vessel formation is more and more complicate. To solve the problem of artificial spectrum shortage and deployable difficulty, we analysis two aspect problems: build the mathematical model and combine the table dispatching method and the auxiliary decision to solve the allocation question [2].

## II. THE SPECTRUM ALLOCATION PROJECT DESIGN

Due to the development of the mode of operations, it is the common view that frequency is as important as bullet. We characterize the mathematical model as follows: (1) The vessel formation scenes are divided into several different scene; (2) We analysis the interference pattern and spectrum management demand of specific scene, then we get the optimal spectrum management program and put the scene and spectrum management program to the CBR (Case-Based Reasoning) library ;(3) The spectrum allocation question of the vessel formation will be seen as a new scene. If there is no same scene, we will use the suggested arithmetic to get the solution.

The spectrum allocation mathematical model is characterized as follows: how to find the best spectrum allocation matrix  $A$  to let the benefit  $U(R)$  be maximum for the

spectrum matrix  $L$ , benefit matrix  $B$ , spectrum interference matrix  $C$  have be known [3].

Suppose there is  $N$  equipment and  $M$  frequency band. We define the spectrum matrix  $L$ , benefit matrix  $B$ , spectrum interference matrix  $L$ , best spectrum allocation matrix  $A$  and the benefit  $U(R)$ :

Available spectrum matrix  $L$ :

$$L = \{l_{m,n} | l_{m,n} \in \{0,1\}\}_{N \times M} \quad (1)$$

$l_{m,n} = 1$  denotes the equipment  $n$  ( $1 \leq n \leq N$ ) can use spectrum  $m$  ( $1 \leq m \leq M$ )

Benefit matrix  $B$ :

$$B = \{b_{m,n}\}_{N \times M} \quad (2)$$

$B = \{b_{m,n}\}_{N \times M}$  is the benefit when equipment  $n$  ( $1 \leq n \leq N$ ) use spectrum  $m$  ( $1 \leq m \leq M$ ), of cause,  $b_{m,n} = 0$  when  $l_{m,n} = 0$ .

Spectrum interference matrix  $C$ :

$$C = \{c_{n,k,m} | c_{n,k,m} \in \{0,1\}\}_{N \times N \times M} \quad (3)$$

$C_{n,k,m} = 1$  shows interference exist when equipment  $n$  and  $k$  ( $1 \leq n, k \leq n$ ) use spectrum  $m$  ( $1 \leq m \leq M$ ) at the same time.

No interference matrix  $A$ :

$$A = \{a_{n,m} | a_{n,m} \in \{0,1\}\}_{N \times M} \quad (4)$$

$a_{n,m} = 1$  shows the equipment  $n$  ( $1 \leq n \leq N$ ) use spectrum  $m$  ( $1 \leq m \leq M$ ).

The whole benefit can describe by:

$$R = \left\{ r_n = \sum_{m=1}^M a_{n,m} \times b_{m,n} \right\}. \quad (5)$$

So we can easily get that the spectrum allocation question can transform into the following optimization problem:

$$A^* = \arg \max U(R) \quad (6)$$

### III. THE MATHEMATICAL MODEL

#### A. Table Dispatching Method to Solve Spectrum Allocation Question

In the case of interference, the objective of spectrum allocation of vessel formation is to guarantee that the equipments which have priority can use the spectrum by the means of reasonable spectrum allocation [4]. It is contain two problems: first, get the priority of this equipment; second, confirm the spectrum allocation as effective as possible.

Suppose there is  $N$  equipment and  $M$  frequency band. The priority weight of the equipment in different spectrum band can be described as the following matrix:

$$\omega = \begin{bmatrix} \omega_{11} & \omega_{12} & \cdots & \omega_{1N} \\ \omega_{21} & \omega_{22} & \cdots & \omega_{2N} \\ \cdots & \cdots & \cdots & \cdots \\ \omega_{M1} & \omega_{M2} & \cdots & \omega_{MN} \end{bmatrix} \quad (7)$$

where  $\omega_{ij}$  is the priority weight of  $j$  equipment when it use  $i$ th spectrum band.

We translate the priority weight matrix  $\omega$  into cost matrix  $Z$ .  $Z_{ij} = 1 - \omega_{ij}$ .

$$Z = \begin{bmatrix} z_{11} & z_{12} & \cdots & z_{1N} \\ z_{21} & z_{22} & \cdots & z_{2N} \\ \cdots & \cdots & \cdots & \cdots \\ z_{M1} & z_{M2} & \cdots & z_{MN} \end{bmatrix} \quad (8)$$

For example, suppose there is five equipment and three frequency band. The priority weight matrix is:

$$\omega = \begin{bmatrix} 0.4 & 0.45 & 0.3 & 0.4 & 0.2 \\ 0.2 & 0.35 & 0.45 & 0.25 & 0.3 \\ 0.4 & 0.2 & 0.25 & 0.35 & 0.5 \end{bmatrix}$$

Then the cost matrix is:

$$Z = \begin{bmatrix} 0.6 & 0.55 & 0.7 & 0.6 & 0.8 \\ 0.8 & 0.65 & 0.55 & 0.75 & 0.7 \\ 0.6 & 0.8 & 0.75 & 0.65 & 0.5 \end{bmatrix}$$

Suppose the free frequency band are  $2 \sim 18MHz$ ,  $20MHz \sim 27MHz$ ,  $31MHz \sim 45MHz$ . And the frequency band needed is  $6MHz$ ,  $7MHz$ ,  $10MHz$ ,  $6MHz$ ,  $8MHz$ .

TABLE I. MATRIX DATE

$A_i \backslash B_j$	$B_1$	$B_2$	$B_3$	$B_4$	$B_5$	$a_i$
$A_1$	0.6	0.55	0.7	0.6	0.8	16
$A_2$	0.8	0.65	0.55	0.75	0.7	7
$A_3$	0.6	0.8	0.75	0.65	0.5	14
$b_j$	6	7	10	6	8	

where  $A_i$  is the  $i$ th spectrum, and  $a_i$  is the frequency band of  $A_i$ ,  $B_j$  is the  $j$ th equipment, and  $b_j$  is the frequency band of  $B_j$  needed. Every check corresponds to  $z_{ij}$ . First, we use

northwest corner method to get, the initial solution. The calculate result is  $(x_{11}x_{12}x_{13}x_{23}x_{33}x_{34}x_{35}) = (6,7,3,7,0,6,8)$ . The objective function value is  $f=21.3$ . Set the initial solution into table 2. Calculate the  $\omega_i$  and  $v_j$ , set them into the left column and the first line. Then calculate  $z_{ij} - c_{ij}$ . The reduced cost of basic variable is 0.

TABLE II. MAX REDUCED

	$v_j$	0.6	0.55	0.7	0.6	0.45	
$\omega_i$	$A_i \backslash B_j$	$B_1$	$B_2$	$B_3$	$B_4$	$B_5$	$a_i$
0	$A_1$	0	0	0	0	-0.35	16
-0.15	$A_2$	-0.35	-0.25	0	-0.3	-0.4	7
0.05	$A_3$	0.05	-0.2	0	0	0	14
	$b_j$	6	7	10	6	8	

On table 2, the max reduced cost is  $z_{31} - c_{31} = 0.05$ . It does not reach the optimal result. Then we use the closed-lope method to improve the initial solution. Take the closed-lope  $x_{11}x_{31}x_{14}x_{34}$ , let the adjustment amount be  $\theta$ . To maintain the feasibility, let  $x_{31} = \theta \geq 0$ ,  $x_{34} = 6 - \theta \geq 0$ ,  $x_{11} = 6 - \theta \geq 0$ ,  $x_{14} = \theta \geq 0$ , get  $\theta = 6$ . The new basic variable is  $(x_{12}x_{13}x_{14}x_{23}x_{31}x_{33}x_{35}) = (7,3,6,7,6,0,8)$ . The objective function value is  $f=21$ . Then calculate  $z_{ij} - c_{ij}$ . The result shows that whole reduced costs are negative or zero. So we have get the best result as follows:  $B_1: 2MHz \sim 8MHz$ ,  $B_2: 8MHz \sim 15MHz$ ,  $B_3: 15MHz \sim 18MHz$ ,  $B_4: 31MHz \sim 37MHz$ ,  $B_5: 37MHz \sim 45MHz$ .

#### B. Similarity Retrieval Algorithm Model Based on CBR

The similarity retrieval flow based on CBR is described by picture2:

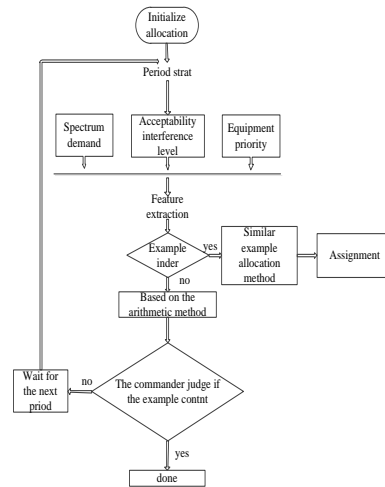


FIGURE I. SIMILARITY RETRIEVAL FLOW BASED ON CBR

The process is: let the spectrum assignment be new example, and get the feature extraction. Then we check the CBR library. If there is similar scene, we get the auxiliary decision to report to the commander; otherwise, use the suggested arithmetic to get the solution [5]. First, we calculate the relative distance between new scene and the example of CBR library

$$d(V_r', V_r^i) = \left| \frac{V_r' - V_r^i}{V_r'} \right| \quad (9)$$

where  $V_r'$  and  $V_r^i$  are  $r$ th characteristic value of  $i$ th example. The characteristic value of this paper is  $z_{ij}$ . Then calculate the similarity between  $V'$  and  $V^i$

$$SD(V', V^i) = 1 - \sum_{r=1}^n \omega_r \cdot d(V', V^i) \quad (10)$$

The new scene and the example of CBR library are similar when the similarity Approach 1[6]. We can set the threshold [7]. (For example, set the threshold be 0.9). When the similarity between  $V'$  and  $V^i$  bigger than 0.9, we can get the auxiliary decision to report to the commander[8].

#### IV. CONCLUSION

In this paper, we analysis the spectrum allocation method. A mathematical model used in spectrum assignment is developed. We build the mathematical model and combine the table dispatching method and the auxiliary decision to solve the allocation question. The results show the performance improvements of the proposed algorithms. So it has very important practical significance.

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