**Research on Balanceable Path planning Method for Mobile Wireless Sensor Network**

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**Abstract.** Path planning problem of low cost effective sweep coverage for mobile wireless sensor network (MWSN) is one MTSP problem and the number of mobile nodes is the number of travel sales man in the MTSP problem. To keep the balance of moving path for each mobile node in sweep coverage of MWSN, features of mobile node’s burden are discussed and balance factor are presented to measure the balance of load for sweep coverage in this paper. Fast balance factor is proposed for evolutionary computation algorithms based path planning. Experimental results show that the balance of moving path planed by our proposed method is better.

**Introduction**

In sweep coverage [1-3] of mobile wireless sensor network (MWSN) [1], each mobile node moves along one point of interesting sequence as its moving path [1][2]. In sweep coverage of MWSN, moving path for each mobile node should be planed rationally. The path plan problem for mobile nodes in low cost sweep coverage is one multiple travel salesman problem (MTSP)[1] with the maximum visiting deadline time T as constrains[3][4].

To measure the difference of mobile node on cost, balance factor is defined in this paper. With balance factor, fitness function of evolutionary computation algorithms such as genetic algorithm [5] can be designed when the path planning problem of sweep coverage is solved by evolutionary computation algorithms. In the following, balance factor for path planning of sweep coverage is discussed at section2. And fitness function based on balance factor for evolutionary computation algorithms is given at section3. Experimental results are shown at section4. Conclusion and future work are given at section5.

**Loads in Sweep Coverage**

Let \( P = \{P_i \in \Omega \subseteq R^2, i = 1, 2 \cdots n\} \) be set for point of interesting (POI) and \( S = \{s_i, i = 1, 2 \cdots m\} \) be the set of all mobile nodes in MWSN. And let \( P P_j = \{P_{j1}, P_{j2} \cdots P_{js}\} \) be the moving path of mobile node \( s_j \in S \) in one low cost effective sweep coverage. Because the sweep coverage is effective, \( P = \bigcup_{j=1}^{m} PP_j \), \( PP_i \cap PP_j = \emptyset \), and \( P_{j1} = P_{js} \) where \( 1 \leq j \leq m \). And because the sweep coverage is also low cost, the moving path for each mobile node in sweep coverage of MWN is one Hamilton loop.

In MWSN, there are 3 kind actions of mobile nodes for their behavior. The first is moving action which is the moving behavior of one mobile node from one POI to another adjacent POI. The second is information sampling action which is the information sampling behavior of one mobile node near one POI. The third is other auxiliary action which is some other behaviors of one mobile node. Because there are some loads for the happening of each kind action, some cost should be paid for the maintenance of sweep coverage by MWSN. Because each kind of action of one mobile node
is happening during the sweep process which the mobile node is moving along its moving path in
sweep coverage, loads of one mobile node is related to its moving path. Let PP_j=<P_{j1}, P_{j2}...P_{jk}> be
the moving path of mobile node s_j in one low cost effective sweep coverage and let mLoad(i,j)≥0 be
the moving action load of one mobile node when the mobile node moves from POI P_i to POI P_j,
sLoad(i)≥0 be the information sampling load when the mobile node samples data near one POI,
oLoad(i)≥0 be the loads for other auxiliary action of one mobile node. Let Lm, Ls and Lo be the
summation of loads for moving action, information sampling action and other auxiliary action of
one mobile node when the mobile node moves along its moving path. If Load is the summation of
all load of mobile node s_i along moving path PP_j, some equations can be defined as following.

\[
Lm(PP_j) = \sum_{i=j_1}^{i=j_k} mLoad(i,i+1) \quad (1)
\]

\[
Ls(PP_j) = \sum_{i=j_1}^{i=j_k} sLoad(i) \quad (2)
\]

\[
Lo (PP_j) = \sum_{i=j_1}^{i=j_k} oLost(i) \quad (3)
\]

\[
Load(s_i,PP_j) = \begin{pmatrix}
c_1(s_i) \\
c_2(s_i) \\
c_3(s_i)
\end{pmatrix}
\begin{pmatrix}
Lm(PP_j) \\
Ls(PP_j) \\
Lo(PP_j)
\end{pmatrix} \quad (4)
\]

\[
B^*(L) = \frac{\max(L) - \min(L)}{\max(L)} \quad (6)
\]

In equation (6), c_1(s_i), c_2(s_i) and c_3(s_i) are coefficients for moving action load, information
sampling action load and other auxiliary action of mobile node s_i. In equation (4), c_1(s_i)≥0, c_2(s_i)≥0
and c_3(s_i)≥0.

In sweep coverage of MWSN, if more POIs are in moving path for one mobile node, load of
the mobile node is greater. Furthermore, if the length of moving path for one mobile node is longer, the
load of the mobile node is greater.

If structure, function and life-span of each mobile node in a MWSN are homothetic, each load
coefficients is independent of mobile node. With this assumption, c_1(s_i), c_2(s_i) and c_3(s_i) in
equation(4) can be denoted as c_1, c_2 and c_3 and equation(4) can be simplified as equation(5). In
equation(5), c_1≥0, c_2≥0, c_3≥0.

Because Lm is caused by mechanical motion meanwhile Ls and Lo are mainly caused by
electronic operation, Lm is the main parts of load of one mobile node in sweep coverage. If any
load caused by electronic operation is ignored, only Lm need to be considered when the load of one
mobile node is calculated according to equation (4) or equation (5).

In sweep coverage of MWSN, effective sweep coverage means that each POI is visited by at
least one mobile node along its moving path before stop time. Let PP_i be the moving path of
mobile node s_i and L_i be the abbreviation of Load(s_i, PP_i). If \( L = \{L_i \mid i=1,2...m\} \) is the load
set for mobile node set S={s_i | i=1,2...m} in sweep coverage, \( E(L) = \frac{1}{m} \sum_{j=1}^{m} L_j \) is the mean load of mobile
node in sweep coverage and \( D(L) = \frac{1}{m} \sum_{j=1}^{m} (L_j - E(L))^2 \) is the variance for mobile node's load. D(L)
can be used to measure whether load of each mobile node is balanceable.

**Definition1:** Let S={s_i, i=1,2...m} be the mobile node set for sweep coverage of MWSN and
$L = \{L_i \mid i=1,2,\ldots,m\}$ be the load set for each mobile node. If $d_{ij} = |L_i - L_j|$ where $i, j = 1,2,\ldots,m$, $B(L) = \frac{1}{m^2} \sum_{i=1}^{m} \sum_{j=1}^{m} d_{ij}$ is the balance factor for sweep coverage of MWSN.

For balance factor defined at definition 1, three conclusions as following can be proved. Firstly, $B(L) \geq 0$. Secondly, $B(L) = 0$ if the load of each mobile node is same. Thirdly, if difference for load of each mobile node is greater/less, $B(L)$ is greater/less. Same conclusions can be proved for $B^*(L)$ defined at equation (6). It is clearly that load of mobile node in sweep coverage of MWSN is more balanceable if the value of $B(L)$ or $B^*(L)$ is more less.

If there are $m$ mobile nodes in sweep coverage of MWSN, the time complexity of $B(L)$ computing should be $O(m^2)$ according to equation (4). On the other hand, because $B^*(L)$ defined by equation (6) has same characteristics with $B(L)$ on the measuring of balance for sweep coverage, $B^*(L)$ can be treated as one kind of balance factor for sweep coverage. And because the time complexity of $B^*(L)$ is $O(m)$ when there are $m$ mobile nodes in sweep coverage, $B^*(L)$ is the fast balance factor for sweep coverage of MWSN. It is obvious that $B^*(L) \in [0,1]$. And more less the value of $B^*(L)$ is, more balanceable of the sweep coverage on mobile node’s loads is.

**Balance Factor Based Fitness Function for Evolutionary Computation Algorithms**

In fact, the balance status of mobile node’s load in sweep coverage of MWSN can be measured by $D(L)$ which is the variance of load sequence $L = \{L_i \mid i=1,2,\ldots,m\}$ for all $m$ mobile nodes in sweep coverage. Because $D(L)$ is equivalent to balance factor $B(L)$ which is defined at definition 1, $B(L)$ is the quantitative indicator for balance status of mobile node’s load in sweep coverage of MWSN. Because $B^*(L)$ defined by equation (6) has same characteristic with $B(L)$ on the measuring of balance status of sweep coverage, $B^*(L)$ can be used to measure the balance status of sweep coverage. And because the time complexity of $B^*(L)$ is $O(m)$ which is less either than time complexity of $B(L)$ or than time complexity of $D(L)$, balance status of sweep coverage measured by $B^*(L)$ can be computed quickly.

**Algorithm 1:** $B^*(L)$ based fitness function of evolutionary computation algorithms for the solving of multiple travel salesman problem

**Input:** pathCode, moving path sequence for all mobile nodes; distance matrix $D=(d_{ij})_{n \times n}$ where $d_{ij}$ is the distance from P$_i$ to P$_j$; $m$, the number of travel salesman

**Output:** $f$, the fitness value based on pathCode

1) Part sequence pathCode into $m$ segments with pathCode$[n+1]$, pathCode$[n+2]$ … pathCode$[n+m-1]$ as segmentation points. Each segment is denoted as PP$_i$ which is one POI sequence, $i=1,2,\ldots,m$.

2) $L = \Phi$

3) for $i=1$ to $m$ step by 1

4) calculate $L_i$, the load of $i$th mobile node according to $D$ and equation (5).

5) $L = L \cup L_i$

6) end for

7) $f = \frac{\text{max}(L) - \text{min}(L)}{\text{max}(L)}$

In algorithm 1, pathCode is treated as one array with $n+m-1$ element where $m$ is the number of travel salesman and $n$ is the number of POI. And in MTSP based path planning for sweep coverage of MWSN, the number of travel salesman is the number of mobile nodes in sweep coverage of MWSN. Element in each pathCode[i], $i=1,2,\ldots,n$, is the ID of one POI and pathCode[1…n] is one permutations of all $n$ POIs. Because pathCode is the record for the moving path of each travel salesman, pathCode[1…n] should be parted into $m$ segments with pathCode[n+1], pathCode[n+2] … pathCode[n+m-1] as segmentation points and PP$_i$, the $i$th segment is the travel POI sequence for the $i$th travel salesman, $i=1,2,\ldots,m$. 

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Experimental Results and Analysis

In our experiment, moving path among some POIs in 10x10 area for each mobile nodes in sweep coverage of MWSN is planned. Genetic algorithm is used to solve MTSP problem and the fitness function for genetic algorithm is implemented according to algorithm1. In the implementation of genetic algorithm, the number of population is 80; the crossover probability is 0.01 and the mutation probability 0.001.

The balance status of path planning for sweep coverage with 2 mobile nodes among 100 POIs are shown at fig1. In fig1, B is balance factor and $B^*$ is fast balance factor. It is obvious that the balance of moving path with fast balance factor is good.

Conclusion

The longevity of mobile nodes is depended on load of each mobile node and the longevity of mobile wireless sensor network is depended on whether loads of all mobile nodes are balanceable. In this paper, balance factor is introduced to plan moving path for all mobile nodes with the balance of loads as constrains. To estimate the balance status of moving path quickly, fast balance factor is defined in this paper too. With fast balance factor, balanceable moving path of each mobile node can planned with evolutionary computation algorithms quickly.

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Reference