Abstract— This work proposes a Dynamic Bandwidth Allocation (DBA) scheme for next-generation OFDMA-PON to accommodate wireless signals. We transform DBA into a multi-objective optimization problem, and Non-dominated Sorting Genetic Algorithm is applied to get best-fitted individuals for each Optical Network Unit (ONU) to achieve low delay and fairness.

Keywords—Passive Optical Networks; Dynamic Bandwidth Allocation; Genetic Algorithm

I. INTRODUCTION

Passive Optical Network (PON) provides a point-to-multipoint solution to satisfy the increasing demand on capacity in access networks, i.e., between service provider central offices (COs) and customer sites. A PON consists of an optical line terminal (OLT) located at the provider CO and a number of optical network units (ONUs) at the customer premises [1].

Some candidates for next-generation PON stand out, including Time Division Multiple Access-based (TDMA-based) 10Gigabit-PON (10G-PON), 10Gigabit Ethernet-PON (10GE-PON) and Wavelength Division Multiplexing-PON (WDM-PON) [2], as well as Orthogonal Frequency Division Multiple Access-PON (OFDMA-PON) [3]. However, migration to these new technologies has raised a number of challenges.

Current commercial PONs adopts centralized medium access control (MAC) to govern downstream and upstream data among multiple ONUs. To arbitrate bandwidth allocation for upstream transmission, dynamically bandwidth allocation (DBA) algorithm is required.

The most outstanding DBA, Interleaved Polling With Adaptive Cycle Time (IPACT) [4], is noted as the founder of DBA design. To provide differentiated services and guaranteed QoS, Bandwidth Guaranteed Polling (BGP) mechanism [5] is proposed to equally divide bandwidth into several parts and be allocated to ONUs with higher priority according to service-level agreement (SLA). However, equal bandwidth division may result in data fragmentation, which leads to extra guard band, and decrease throughput and bandwidth utilization.

In order to increase bandwidth utilization and share optical wavelength elastically, dynamic wavelength and bandwidth allocation (DWBA) algorithm [6] is proposed, which assumes that each ONU can switch wavelength in upstream channel at millisecond level. However, it is expensive to switch wavelength at millisecond level in TDMA-PON. Orthogonal Frequency Division Multiplexing (OFDM) technology uses multiple carriers overlapped orthogonally in the frequency domain, resulting in higher spectral efficiency. Individual subcarriers can be allocated to different ONUs in OFDMA-PON, to achieve two-dimensional time-frequency bandwidth map at much finer granularity compared with TDMA-PON and WDM-PON.

Ref. [7] proposed two MAC agreements, dynamic circuit transmission (DCT) and fixed burst transmission (FBT) for OFDMA-PON. DCT is only suitable for non-bursty traffic, while FBT does not provide satisfactory QoS performance since the scheduling algorithm is based on a simple round-robin strategy. In [8], a set of subcarriers assigned to each "virtual PONs". However, this design works in pure TDMA manner and will not fit in architecture presented in [9].

We in this work propose a feasible and fast bandwidth allocation schemes for next-generation OFDMA-PON. We model the complex DBA into a multi-objective optimization problem with QoS of mean delay and fairness as two objectives. Non-dominated Sorting Genetic Algorithm (NSGA) [10, 11] is used to solve the problem.

The remainder of this paper is organized as follows. In section II, we present the architecture of OFDMA-PON and elaborate on how the system works. In section III, we state the inherent DBA problem for the OFDMA-PON architecture. In section IV, we adopt NSGA to promote QoS and fairness among ONUs and delineate the proposed dynamic bandwidth allocation scheme. In section V, algorithm performance is analyzed according to simulation results. In section VI, conclusions are remarked.

II. OFDMA-PON ARCHITECTURE

The bandwidth allocation design is based on the OFDMA-PON architecture shown in Fig.1, where Optical Line Terminal (OLT) is connected to multiple remote ONUs through the Optical Distribution Node (ODN). The ODN is composed of a set of optical circulators to direct signals among ONUs and OLT.
While TQi and TQCi represent the remaining transmit quota endowed transmit quota and capacity by OLT, respectively. and capacity after previous cycle. \( \lambda_u \) and \( \lambda_d \) represent number of packets waiting for transmission in downstream and upstream, for downstream and upstream signal quality of transmission. Interference (OBI) in the trunk fiber thus to maintain the standard deviation of mean delay among all ONUs to measure fairness. While monitoring network traffic, TQ and TQC may be adjusted to let ONUs share mean delay as small and equal as possible, to achieve better QoS and fairness. According to this design, when upstream ONUs have large number of packets to be send, TQC take the role of limiting burst packets number. Once the quota is used up, TQ has to be accumulated. We set higher TQ or TQC on downstream ONUs to increase their chances of sending packets, so to reduce mean delay.

In this architecture, as illustrated in Fig.2, upstream ONUs has no knowledge of bandwidth requirement from downstream ONUs. Therefore, the direct way is to compare mean delay between two adjacent ONUs. For instance, if mean delay(2) for ONU-2 is less than mean delay(1) for ONU-1, then we should decrease TQ or TBS of ONU-2 until mean delay(1) is equal to mean delay(2). By this way, mean delay of downstream ONUs can be gradually equalized to achieve mean delay(1) and fairness can be achieved at the same time. However, this manner is not feasible because it takes much delay of downstream ONUs can be gradually equalized to achieve better QoS and fairness.

III. NSGA BASED DBA ALGORITHM

We firstly define two factors, i.e., cycle and bandwidth unit to describe our DBA design. One cycle is the time scale of a round of upstream transmission by all ONUs. The bandwidth unit is one OFDM sub-carrier, which is the minimal resource one ONU can get in a certain cycle. The downstream ONUs will suffer more time delay without careful designing.

Two parameters are introduced, i.e., Transmit Quota Capacity (TQC) and Transmit Quota (TQ). TQC is volume of virtual buffer for each ONU to limit maximum burst length. TQ is the access rate for ONUs to send its packets in each cycle. The higher TQC is, the larger burst of packets an ONU can transmit. Below is illustration of TQC and TQ cooperation.

**Step 1:** OLT provides totally K sub-carriers available in a cycle. ONU-i starts to transmit. RSCi represents number of Remaining Sub-carriers, obviously, \( \text{RSC}_i = K \). Pkt i represents number of packets waiting for transmission in ONU-i. Hence, number of packets needing to be sent is determined by expression \( \min \{ TQ_i, RSC_i, \text{pkt}_{-i} \} \). Then do

\[
RSC_{i+1} = \text{RSC}_i + \min \{ TQ_i, RSC_i, \text{pkt}_{-i} \} - 1
\]

\[
TQ_i = TQ_i - \min \{ TQ_i, RSC_i, \text{pkt}_{-i} \}
\]

**Step 2:** When all the subcarriers are used up or all ONUs finish transmission, ONU-N send all packets upstream to OLT, and then cycle ends.

To assess QoS, we define delay as the time duration one packet waits in ONU. If one packet arrives at a certain ONU at cycle \( T_1 \), and is transmitted at cycle \( T_2 \), the delay of the packet is \( T_2 - T_1 \). Hence we have the mean delay for ONU-i:

\[
\text{mean delay}(i) = \frac{\sum \text{delay}(i)}{\# \text{of packets sent}}
\]

We use mean delay of each ONU to measure QoS and the standard deviation of mean delay among all ONUs to measure fairness. We use mean delay of each ONU to measure QoS and the standard deviation of mean delay among all ONUs to measure fairness. While monitoring network traffic, TQ and TQC may be adjusted to let ONUs share mean delay as small and equal as possible, to achieve better QoS and fairness. According to this design, when upstream ONUs have large number of packets to be send, TQC take the role of limiting burst packets number. Once the quota is used up, TQ has to be accumulated. We set higher TQ or TQC on downstream ONUs to increase their chances of sending packets, so to reduce mean delay.

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Proposed by Deb, K in [10, 11], Non-dominated Sorting Genetic Algorithm (NSGA) is one method to solve multi-objective optimization problem. In our DBA design, we firstly map TQ and TQC from decision space to objective space by means of mapping function. Then, we map TQ and TQC from objective space to decision space by means of inverse mapping function. Finally, we use NSGA to determine \( \min \{ TQ, TQC \} \). Then do

\[
RSC_{i+1} = \text{RSC}_i + \min \{ TQ_i, RSC_i, \text{pkt}_{-i} \} - 1
\]

\[
TQ_i = TQ_i - \min \{ TQ_i, RSC_i, \text{pkt}_{-i} \}
\]
space, where NSGA works. To be noted, mean delay of ONU-\( i \)- is entirely dependent on TQ and TQC of ONU-\( i \) itself, as well as TQs and TQCs of all preceding ONUs. Here, mapping function, also named objective function can be expressed as a function of parameters TQ and TQC, i.e.,

\[ \text{mean}_i\text{delay}(i) = f(TQ_i, \ldots, TQ_{i-1}, TQC_i, \ldots, TQC_{i-1}, TQC_i) \]

In our DBA design, TQ and TQC of each ONU are taken as genes to run NSGA. Via NSGA computation, new best-fitted genes are found out and broadcasted to all ONUs, until specified generations are done or no more improvement can be achieved. The detailed NSGA based DBA is demonstrated in Fig.3.

In NSGA, two fitness functions on QoS and fairness needed to meet our DBA requirements.

To measure QoS, we put forward the fitness function 1 as:

\[ f_1 = \frac{\sum_{i=1}^{N} \mu_i}{N} \]

\( N \) is number of ONU, \( \mu_i \) is the mean delay of ONU-\( i \). Fitness function 1 is the average mean-delay of all ONUs, the smaller its numerical value is, the less delay ONUs suffer, and the larger network throughput will be. To measure fairness, we put forward the fitness function 2 as:

\[ f_2 = \frac{\sum_{i=1}^{10} (\mu_i - \bar{\mu})^2 + \sum_{j=11}^{N} (\mu_j - \bar{\mu})^2}{\mu_0} \]

\( \bar{\mu}_0 \) represents the mean delay of the first 10 upstream ONUs. Fitness function 2 is standard deviation of mean delay among all ONUs and the first 10 upstream ONUs. The mean delay of first 10 upstream ONUs is equally the same, and we add weight to last 10 ONUs to handle the mean delay unfairness. The smaller its numerical value is, the greater chances the curve will be, which means greater fairness.

IV. SIMULATION AND ANALYSIS

The simulation investigates the mean delay and delay fairness with respect to various TQC setting. The reason for using TQC instead of TQ is two-fold. First, TQC is an integer, which is simple to adjust. In addition, as we analyzed above, system performance is as sensitive to TQC settings as to TQ. In the simulation, the PON system has \( N=32 \) ONUs operating at 10Gb/s, and all ONUs share a total of 512 OFDM data sub-channel slots. Each OFDM slot is 16 bits long.

In the first simulation, we set traffic load to 0.9, burst to 8.0, fix TQ to 16.0, and then adjust parameter TQC, so that all ONUs are with the same mean delay. On the simulation result shows in Fig.4, we find two problems, (1) It has limitation to manually adjust TQC on fixed TQ, especially when mean delay has dropped down to 5ms or so, because the range of TQC is too distributive to be controlled. (2) It is even impossible to dynamically allocate OFDM-frames on varying traffic.

In the second simulation, we apply NAGA to find out best fitted (TQ, TQC) settings. Fig.4 illustrates that the curve is exponential shape alike, so we express TQC using exponential function. Input variables are TQ=16.0 for all the ONUs,

\[ TQC_i = \exp(a \times i + b) + \exp(c \times i + d) + e \]

Other simulation environment keeps the same as in first simulation.

Fig.5 is pareto front of the generated 60 pairs (\( f_1, f_2 \)) combination. As it can be observed, trade-off exists between mean delay and ONU fairness. The larger mean delay is, the greater fairness ONU achieves, and vise versa. We select three typical (\( f_1, f_2 \)) combination as illustrated in Fig.6, which indicates that mean delay for upstream ONUs drops at end ONUs. The reasons behind is that we add increasing weights to last 10 ONUs to reduce mean delay.
V. CONCLUSIONS

In this paper, we propose an optimal and efficient dynamic bandwidth allocation (DBA) for next-generation OFDMA-PON. In the DBA, we apply Non-dominated Sorting Genetic Algorithm (NSGA) to design a TQ-TQC based DBA scheme to dynamically return the optimal TQ and TQC values for all ONUs. From the simulation results, the DBA design can satisfy the required time delay and ONU fairness under varying traffic conditions.

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